

# Publications

## List of Papers Published

1. Deka, D. and Sen, S. A new transformation free generalized (5,5)HOC discretization of transient Navier-Stokes/Boussinesq equations on nonuniform grids. *International Journal of Heat and Mass Transfer*, 171: 120821, 2021.
2. Deka, D. and Sen, S. Compact higher order discretization of 3D generalized convection diffusion equation with variable coefficients in nonuniform grids. *Applied Mathematics and Computation*, 413: 126652, 2022.

## List of Papers under Preparation

1. Deka, D. and Sen, S. A new transient higher order compact scheme for computation of flow and heat transfer on nonuniform polar grids.

## List of Conference Presentations

1. “Transformation-free compact high order Navier-Stokes equation solver on nonuniform grid” in *International Conference on Advances in Mathematics, Science and Technology (ICAMST)-2020*, Department of Mathematics, Rajiv Gandhi University, September 1-4, 2020.
2. “Numerical simulations of interior and exterior flow problems for  $Re$  value beyond Hopf bifurcation” in *International Conference on Present Scenario of Mathematical Sciences (ICPSMS)-2020*, Department of Mathematics, Karnatak University’s Karnatak Arts College, Dharwad, September 12-13, 2022.

3. “Numerical study of heat transfer in annulus using higher order compact schemes” in *National Seminar on Recent Development in Science and Technology (NSRDST-2024)*, Department of Chemistry, Karimganj College, Karimganj, February 17-18, 2024.

# Bibliography

- [1] Ambreen, T. and Kim, M. H. Flow and heat transfer characteristics over a square cylinder with corner modifications. *International Journal of Heat and Mass Transfer*, 117:50–57, 2018.
- [2] Ananthakrishnaniah, U., Manohar, R., and Stephenson, J. W. High-order methods for elliptic equations with variable coefficients. *Numerical Methods for Partial Differential Equations*, 3:219–227, 1987.
- [3] Ananthakrishnaniah, U., Manohar, R., and Stephenson, J. W. Fourth-order finite difference methods for three-dimensional general linear elliptic problems with variable coefficients. *Numerical Methods for Partial Differential Equations*, 3:229–240, 1987.
- [4] Aziz, I., Siraj-ul-Islam, and Asif, M. Haar wavelet collocation method for three-dimensional elliptic partial differential equations. *Computers and Mathematics with Applications*, 73:2023–2034, 2017.
- [5] Batchelor, G. K. *An Introduction to Fluid Dynamics*, Volume 1. Cambridge University Press, Cambridge, 2005.
- [6] Berthelsen, P. A. and Faltinsen, O. M. A local directional ghost cell approach for incompressible viscous flow problems with irregular boundaries. *Journal of Computational Physics*, 227:4354–4397, 2008.
- [7] Bharti, R. P., Chhabra, R., and Eswaran, V. A numerical study of the steady

- forced convection heat transfer from an unconfined circular cylinder. *Heat and Mass Transfer*, 43:639–648, 2007.
- [8] Blasius, H. Grenzschichten in flüssigkeiten mit kleiner reibung. *Zeitschrift für Angewandte Mathematik und Physik*, 56:1–37, 1908.
- [9] Borges, L. and Daripa, P. A fast parallel algorithm for the Poisson equation on a disk. *Journal of Computational Physics*, 169:151–192, 2001.
- [10] Bouard, R. and Coutanceau, M. The early stage development of the wake behind an impulsively started cylinder for  $40 < Re < 10^4$ . *Journal of Fluids Mechanics*, 101(3):583–607, 1980.
- [11] Bouaziz, M., Kessentini, S., and Turki, S. Numerical prediction of flow and heat transfer of power-law fluids in a plane channel with a built-in heated square cylinder. *International Journal of Heat and Mass Transfer*, 53:5420–5429, 2010.
- [12] Breuer, M. Large eddy simulation of the subcritical flow past a circular cylinder: numerical and modeling aspects. *International Journal for Numerical Methods in Fluids*, 28:1281–1302, 1998.
- [13] Breuer, M., Bernsdorf, J., Zeiser, T., and Durst, F. Accurate computations of the laminar flow past a square cylinder based on two different methods: lattice-Boltzmann and finite-volume. *International Journal of Heat and Fluid Flow*, 21:186–196, 2000.
- [14] Bruneau, C. H. and Saad, M. The 2D lid-driven cavity problem revisited. *Computers and Fluids*, 35:326–348, 2006.
- [15] Cao, S. L., Sun, X., Zhang, J. Z., and Zhang, Y. X. Forced convection heat transfer around a circular cylinder in laminar flow: An insight from Lagrangian coherent structures. *Physics of Fluids*, 33:067104, 2021.
- [16] Chen, G. Q., Gao, Z., and Yang, Z. F. A perturbational  $h^4$  exponential finite difference scheme for convection diffusion equation. *Journal of Computational Physics*, 104:129–139, 1993.

- [17] Chen, Z., Shu, C., Yang, L. M., Zhao, X., and Liu, N. Y. Immersed boundary–simplified thermal lattice Boltzmann method for incompressible thermal flows. *Physics of Fluids*, 32:013605, 2020.
- [18] Cheng, C. H. and Hong, J. L. Numerical prediction of lock-on effect on convective heat transfer from a transversely oscillating circular cylinder. *International Journal of Heat and Fluid Flow*, 40(8):1825–1834, 1997.
- [19] Churchill, S. W. and Bernstein, M. A correlating equation for forced convection from gases and liquids to a circular cylinder in crossflow. *ASME. Journal of Heat Transfer*, 99(2):300–306, 1977.
- [20] Ciment, M., Leventhal, S. H., and Weinberg, B. C. The operator compact implicit method for parabolic equations. *Journal of Computational Physics*, 28:135–166, 1978.
- [21] Collins, W. M. and Dennis, S. C. R. Flow past an impulsively started circular cylinder. *Journal of Fluid Mechanics*, 60(1):105–127, 1973.
- [22] Contrino, D., Lallemand, P., Asinari, P., and Luo, L. S. Lattice-Boltzmann simulations of the thermally driven 2D square cavity at high Rayleigh numbers. *Journal of Computational Physics*, 275:257–272, 2014.
- [23] Coutanceau, M. and Bouard, R. Experimental determination of the main features of the viscous flow in the wake of a circular cylinder in uniform translation. Part 1. Steady flow. *Journal of Fluids Mechanics*, 79:231–256, 1977.
- [24] Coutanceau, M. and Bouard, R. Experimental determination of the main features of the viscous flow in the wake of a circular cylinder in uniform translation. Part 2. Unsteady flow. *Journal of Fluids Mechanics*, 79:257–272, 1977.
- [25] Crawford, L. and Lemlich, R. Natural convection in horizontal concentric cylindrical annuli. *Industrial & Engineering Chemistry fundamentals*, 1:260–264, 1962.
- [26] Das, P., Pandit, S. K., and Ray, R. K. A new perspective of higher order compact nonuniform padé approximation based finite difference scheme for

- solving incompressible flows directly on polar grids. *Computers and Fluids*, 254:105793, 2023.
- [27] De Vahl Davis, G. Natural convection of air in a square cavity: a benchmark numerical solution. *International Journal for Numerical Methods in Fluids*, 3: 249–264, 1983.
- [28] Dehghan, M. Numerical solution of the three-dimensional advection-diffusion equation. *Applied Mathematics and Computation*, 150:5–19, 2004.
- [29] Dehghan, M. and Molavi-Arabshahi, S. M. A simple form for the fourth order difference method for 3-D elliptic equations. *Applied Mathematics and Computation*, 184:589–598, 2007.
- [30] Deka, D. and Sen, S. A new transformation free generalized (5,5)HOC discretization of transient Navier-Stokes/Boussinesq equations on nonuniform grids. *International Journal of Heat and Mass Transfer*, 171:120821, 2021.
- [31] Dennis, S. C. R. and Chang, G. Z. Numerical solution for steady flow past a circular cylinder at Reynolds numbers up to 100. *Journal of Fluid Mechanics*, 42(3):471–489, 1970.
- [32] Dennis, S. C. R. and Hudson, J. D. Compact  $h^4$  finite-difference approximations to operators on Navier-Stokes type. *Journal of Computational Physics*, 85:390–416, 1989.
- [33] Dennis, S. C. R. and Hudson, J. D. Compact finite difference approximation to operators of Navier-Stokes type. *Journal of Computational Physics*, 85: 390–416, 1989.
- [34] Dennis, S. C. R., Hudson, J. D., and Smith, N. Steady laminar forced convection from a circular cylinder at low Reynolds numbers. *Physics of Fluids*, 11: 933–940, 1968.
- [35] Dhiman, A. K., Chabra, R. P., and Eswaran, V. Flow and heat transfer across a confined square cylinder in the steady flow regime: Effect of Peclet number. *International Journal of Heat and Mass Transfer*, 48:4598–4614, 2005.

- [36] Dhiman, A. K., Chabra, R. P., Sharma, A., and Eswaran, V. Effects of Reynolds and Prandtl numbers on heat transfer across a square cylinder in the steady flow regime. *Numerical Heat Transfer, Part A*, 49:717–731, 2006.
- [37] Düring, B. and Fournié, M. High-order compact finite difference scheme for option pricing in stochastic volatility models. *Journal of Computational and Applied Mathematics*, 236:4462–4473, 2012.
- [38] Dutta, S., Kumar, P., and Kalita, J. C. Streamfunction-velocity computation of natural convection around heated bodies placed in a square enclosure. *International Journal of Heat and Mass Transfer*, 152:119550, 2020.
- [39] Fan, P. The standard upwind compact difference schemes for incompressible flow simulations. *Journal of Computational Physics*, 322:74–112, 2016.
- [40] Fornberg, B. A numerical study of steady viscous flow past a circular cylinder. *Journal of Fluid Mechanics*, 98(4):819–855, 1980.
- [41] Fornberg, B. Steady viscous flow past a circular cylinder up to Reynolds number 600. *Journal of Computational Physics*, 61:297–320, 1985.
- [42] Fournié, M. and Karaa, S. Iterative methods and high-order difference schemes for 2D elliptic problems with mixed derivative. *Journal of Applied Mathematics and Computing*, 22:349–363, 2006.
- [43] Franke, R., Rodi, W., and Schönung, B. Numerical calculation of laminar vortex-shedding flow past cylinder. *Journal of Wind Engineering and Industrial Aerodynamics*, 35:237–257, 1990.
- [44] Friehe, C. A. Vortex shedding from cylinders at low Reynolds numbers. *Journal of Fluids Mechanics*, 100:237–241, 1980.
- [45] Fuchs, L. and Tillmark, N. Numerical and experimental study of driven flow in a polar cavity. *International Journal for Numerical Methods in FLuids*, 5: 311–329, 1985.

- [46] Gamet, L., Ducros, F., Nicoud, F., and Poinso, T. Compact finite difference schemes on non-uniform meshes. Application to direct numerical simulations of compressible flows. *International Journal for Numerical Methods in Fluids*, 29:159–191, 1999.
- [47] Ge, L. and Zhang, J. High accuracy iterative solution of convection diffusion equation with boundary layers on nonuniform grids. *Journal of Computational Physics*, 171:560–578, 2001.
- [48] Ge, L. and Zhang, J. Symbolic computation of high order compact difference schemes for three dimensional linear elliptic partial differential equations with variable coefficients. *Journal of Computational and Applied Mathematics*, 143:9–27, 2002.
- [49] Ge, Y. Multigrid method and fourth-order compact difference discretization scheme with unequal meshsizes for 3D Poisson equation. *Journal of Computational Physics*, 229:6381–6391, 2010.
- [50] Ge, Y., Tian, Z. F., and Zhang, J. An exponential high-order compact ADI method for 3D unsteady convection-diffusion problems. *Numerical Methods for Partial Differential Equations*, 29:186–205, 2012.
- [51] Ge, Y., Cao, F., and Zhang, J. A transformation-free HOC scheme and multigrid method for solving the 3D Poisson equation on nonuniform grids. *Journal of Computational Physics*, 234:199–216, 2013.
- [52] Ghia, U., Ghia, K. N., and Shin, C. T. High-Re solutions for incompressible flow using the Navier-Stokes equations and a multigrid method. *Journal of Computational Physics*, 48:387–411, 1982.
- [53] Goldstein, S. and Rosenhead, L. Boundary layer growth. *Mathematical Proceedings of the Cambridge Philosophical Society*, 32:392–401, 1936.
- [54] Gupta, M. M. and Kalita, J. C. A new paradigm for solving Navier–Stokes equations: streamfunction-velocity formulation. *Journal of Computational Physics*, 207:52–68, 2005.



- [55] Gupta, M. M. and Kouatchou, J. Symbolic derivation of finite difference approximations for the three-dimensional Poisson equation. *Numerical Methods for Partial Differential Equations*, 18(5):593–606, 1998.
- [56] Gupta, M. M. and Zhang, J. High accuracy multigrid solution of the 3D convection-diffusion equation. *Applied Mathematics and Computation*, 113: 249–274, 2000.
- [57] Gupta, M. M., Manohar, R. P., and Stephenson, J. W. A single cell high order scheme for the convection-diffusion equation with variable coefficients. *International Journal for Numerical Methods in Fluids*, 4:641–651, 1984.
- [58] He, X. and Doolen, G. Lattice Boltzmann method on curvilinear coordinate system: flow around a circular cylinder. *Journal of Computational Physics*, 134:306–315, 1997.
- [59] Hirota, I. and Miyakoda, K. Numerical solution of Kármán vortex street behind a circular cylinder. *Journal of the Meteorological Society of Japan*, 43(1):30–41, 1965.
- [60] Hirsh, R. S. Higher order accurate difference solutions of fluid mechanics problems by a compact differencing technique. *Journal of Computational Physics*, 19:90–109, 1975.
- [61] Hoffman, J. D. *Numerical methods for Engineers and Scientists*. McGraw-Hill, Inc., Singapore, 1993.
- [62] Honji, H. and Taneda, S. Unsteady flow past a circular cylinder. *Journal of the Physical Society of Japan*, 27:1668–1677, 1969.
- [63] Hou, S., Zou, Q., Chen, S., Doolen, G., and Cogley, A. Simulation of cavity flow by the Lattice Boltzmann method. *Journal of Computational Physics*, 118:329–347, 1995.
- [64] in't Hout, K. J. and Foulon, S. ADI finite difference schemes for option pricing in the Heston model with correlation. *International Journal of Numerical Analysis and Modelling*, 7:303–320, 2010.

- [65] in't Hout, K. J. and Welfert, B. D. Stability of ADI schemes applied to convection-diffusion equations with mixed derivative terms. *Applied Numerical Mathematics*, 57:19–35, 2007.
- [66] in't Hout, K. J. and Wyns, M. Convergence of the Modified Craig-Sneyd scheme for two-dimensional convection-diffusion equations with mixed derivative term. *Journal of Computational and Applied Mathematics*, 296:170–180, 2016.
- [67] Iyengar, S. R. K. and Manohar, R. High order difference methods for Heat equation in polar cylindrical coordinates. *Journal of Computational Physics*, 77:425–438, 1988.
- [68] Jain, M. K., Jain, R. K., and Krishna, M. A fourth-order difference scheme for quasilinear Poisson equation in Polar co-ordinates. *Communications in Numerical Methods in Engineering*, 10:791–797, 1994.
- [69] Kalita, J. C. and Ray, R. K. A transformation-free HOC scheme for incompressible viscous flows past an impulsively started circular cylinder. *Journal of Computational Physics*, 228:5207–5236, 2009.
- [70] Kalita, J. C. and Sen, S. The (9,5) HOC formulation for the transient Navier-Stokes equation in primitive variable. *International Journal for Numerical Methods in Fluids*, 55:387–406, 2007.
- [71] Kalita, J. C. and Sen, S. Triggering asymmetry for flow past circular cylinder at low Reynolds numbers. *Computers and Fluids*, 59:44–60, 2012.
- [72] Kalita, J. C. and Sen, S. The biharmonic approach for unsteady flow past an impulsively started circular cylinder. *Computers and Fluids*, 59:44–60, 2012.
- [73] Kalita, J. C. and Sen, S. Unsteady separation leading to secondary and tertiary vortex dynamics: The sub- $\alpha$ - and sub- $\beta$ - phenomena. *Journal of Fluids Mechanics*, 730:19–51, 2013.
- [74] Kalita, J. C. and Sen, S.  $\alpha$ - $\beta$ -phenomena in the post-symmetry break for the flow past a circular cylinder. *Physics of Fluids*, 29:033603, 2017.

- [75] Kalita, J. C., Dalal, D. C., and Dass, A. K. Fully compact higher-order computation of steady-state natural convection in a square cavity. *Physical Review E.*, 64-066703:1–13, 2001.
- [76] Kalita, J. C., Dalal, D. C., and Dass, A. K. A class of higher order compact schemes for the unsteady two-dimensional convection-diffusion equation with variable convection coefficients. *International Journal for Numerical Methods in Fluids*, 38:1111–1131, 2002.
- [77] Kalita, J. C., Dass, A. K., and Dalal, D. C. A transformation-free HOC scheme for steady convection-diffusion on non-uniform grids. *International Journal for Numerical Methods in Fluids*, 44:33–53, 2004.
- [78] Kalita, J. C., Dass, A. K., and Nidhi, N. An efficient transient Navier-Stokes solver on compact nonuniform space grids. *Journal of Computational and Applied Mathematics*, 214:148–162, 2008.
- [79] Karaa, S. A high-order compact ADI method for solving three-dimensional unsteady convection-diffusion problems. *Numerical Methods for Partial Differential Equations*, 22:983–993, 2006.
- [80] Karaa, S. High-order difference schemes for 2D elliptic and parabolic problems with mixed derivatives. *Numerical Methods for Partial Differential Equations*, 23:366–378, 2007.
- [81] Karaa, S. and Othman, M. Two-level compact implicit schemes for three-dimensional parabolic problems. *Computers and Mathematics with Applications*, 58:257–263, 2009.
- [82] Kawaguti, M. Numerical solution of the Navier-Stokes equations for the flow around a circular cylinder at Reynolds number 40. *Journal of the Physical Society of Japan*, 8:747–757, 1953.
- [83] Kelly, C. T. *Iterative methods for Linear and Nonlinear Equations*. SIAM Publications, Philadelphia, 1995.

- [84] Koumoutsakos, P. and Leonard, A. High-resolution simulations of the flow around an impulsively started cylinder using vortex methods. *Journal of Fluid Mechanics*, 296:1–38, 1995.
- [85] Kuehn, T. H. and Goldstein, R. J. An experimental and theoretical study of natural convection in the annulus between horizontal concentric cylinders. *Journal of Fluid Mechanics*, 74(4):695–719, 1976.
- [86] Kumar, P. and Kalita, J. C. A transformation-free  $\psi - v$  formulation of the Navier–Stokes equations on compact nonuniform grids. *Journal of Computational and Applied Mathematics*, 353:292–317, 2019.
- [87] Kumar, P. and Kalita, J. C. A comprehensive study of secondary and tertiary vortex phenomena of flow past a circular cylinder: A cartesian grid approach. *Physics of Fluids*, 33:053608, 2021.
- [88] Lai, M. C. A simple compact fourth-order Poisson solver on polar geometry. *Journal of Computational Physics*, 182:337–345, 2002.
- [89] Lai, M. C. and Wang, W. C. Fast direct solvers for Poisson equation on 2D polar and spherical geometries. *Numerical Methods for Partial Differential Equations*, 18(1):56–68, 2001.
- [90] Lange, C., Durst, F., and Breuer, M. Momentum and heat transfer from cylinders in laminar crossflow at  $10^4 \leq Re \leq 200$ . *International Journal of Heat and Mass Transfer*, 41:3409–3430, 1998.
- [91] Lankadasu, A. and Vengadesan, S. Shear effect on square cylinder wake transition characteristics. *International Journal for Numerical Methods in Fluids*, 67:1112–1134, 2010.
- [92] Le, D. V., Khoo, B. C., and Peraire, J. An immersed interface method for viscous incompressible flows involving rigid and flexible boundaries. *Journal of Computational Physics*, 220:109–138, 2006.
- [93] Lee, D. and Tsuei, Y. M. A hybrid adaptive gridding procedure for recirculating fluid flow problem. *Journal of Computational Physics*, 108:122–141, 1993.

- [94] Lee, S. T., Liu, J., and Sun, H. W. Combined compact difference scheme for linear second-order partial differential equations with mixed derivative. *Journal of Computational and Applied Mathematics*, 264:23–37, 2014.
- [95] Lele, S. K. Compact finite difference schemes with spectral-like resolution. *Journal of Computational Physics*, 103:16–42, 1992.
- [96] Li, M., Tang, T., and Fornberg, B. A compact fourth-order finite difference scheme for the incompressible Navier-Stokes equations. *International Journal for Numerical Methods in Fluids*, 20:1137–1151, 1995.
- [97] Lin, J. and Reutskiy, S. A cubic B-spline semi-analytical algorithm for simulation of 3D steady-state convection-diffusion-reaction problems. *Applied Mathematics and Computation*, 371:124–944, 2020.
- [98] Loc, T. P. Numerical analysis of unsteady secondary vortices generated by an impulsively started circular cylinder. *Journal of Fluid Mechanics*, 100:111–128, 1980.
- [99] Loc, T. P. and Bouard, R. Numerical solution of the early stage of the unsteady viscous flow around a circular cylinder: A comparison with experimental visualization and measurements. *Journal of Fluid Mechanics*, 160:93–117, 1985.
- [100] Ma, T. . and Ge, Y. A blended compact difference (BCD) method for solving 3D convection-diffusion problems with variable coefficients. *International Journal of Computational Methods*, 17(6):1950022, 2020.
- [101] Ma, Y. and Ge, Y. A high order finite difference method with Richardson extrapolation for 3D convection diffusion equation. *Applied Mathematics and Computation*, 215:3408–3417, 2010.
- [102] Mack, L. R. and Bishop, E. H. Natural convection between horizontal concentric cylinders for low Rayleigh numbers. *Quarterly Journal of Mechanics and Applied Mathematics*, 21:223–241, 1968.

- [103] Mohamed, N., Mohamed, S. A., and Seddek, L. F. Exponential higher-order compact scheme for 3D steady convection-diffusion problem. *Applied Mathematics and Computation*, 232:1046–1061, 2014.
- [104] Mohanty, R. and Dey, S. Single-cell fourth-order difference approximations for  $u_x$ ,  $u_y$  and  $u_z$  of the three-dimensional quasi-linear elliptic equation. *Numerical Methods for Partial Differential Equations*, 16:417–425, 2000.
- [105] Mohanty, R. and Setia, N. A new high order compact off-step discretization for the system of 3D quasi-linear elliptic partial differential equations. *Applied Mathematical Modelling*, 37:6870–6883, 2013.
- [106] Mohanty, R. and Singh, S. A new nighly accurate discretization for three-dimensional singularly perturbed nonlinear elliptic partial differential equations. *Numerical Methods for Partial Differential Equations*, 22:1379–1395, 2006.
- [107] Mohanty, R. K. Fourth order finite difference methods for the system of 2-D nonlinear elliptic equations with variable coefficients. *International Journal for Computer Mathematics*, 46:195–206, 1992.
- [108] Mohanty, R. K. and Jain, M. K. Technical note: the numerical solution of the system of 3-D nonlinear elliptic equations with mixed derivatives and variable coefficients using fourth-order difference methods. *Numerical Methods for Partial Differential Equations*, 11:187–197, 1995.
- [109] Momose, K. and Kimoto, H. Forced convection heat transfer from a heated circular cylinder with arbitrary surface temperature distributions. *Heat Transfer—Asian Research*, 28(6):484–499, 1999.
- [110] Niu, X., Shu, C., Chew, Y., and Peng, Y. A momentum exchange-based immersed boundary-lattice boltzmann method for simulating incompressible viscous flows. *Physics Letters A*, 354:173–182, 2006.
- [111] Niu, X. D., Chew, Y. T., and Shu, C. Simulation of flows around an impulsively started circular cylinder by Taylor series expansion-and least squares-based

- lattice Boltzmann method. *Journal of Computational Physics*, 188:176–193, 2003.
- [112] Norberg, C. An experimental investigation of the flow around a circular cylinder: influence of aspect ratio. *Journal of Fluid Mechanics*, 258:287–316, 1994.
- [113] Noye, B. J. and Tan, H. H. A third-order semi-implicit finite difference method for solving the one-dimensional convection-diffusion equation. *International Journal for Numerical Methods in Engineering*, 26:1615–1629, 1988.
- [114] Paliwal, B., Sharma, A., Chhabra, R., and Eswaran, V. Power law fluid flow past a square cylinder: momentum and heat transfer characteristics. *Chemical Engineering Science*, 58:5315–5329, 2003.
- [115] Pandit, S. K. On the use of compact streamfunction-velocity formulation of steady Navier-Stokes equations on geometries beyond rectangular. *Journal of Scientific Computing*, 36:219–242, 2008.
- [116] Pandit, S. K. and Chattopadhyay, A. A robust higher order compact scheme for solving general second order partial differential equation with derivative source terms on nonuniform curvilinear meshes. *Computers and Mathematics with Applications*, 74:1414–1434, 2017.
- [117] Pandit, S. K., Kalita, J. C., and Dalal, D. C. A transient higher order compact scheme for incompressible viscous flows on geometries beyond rectangular. *Journal of Computational Physics*, 225:1100–1124, 2007.
- [118] Pandit, S. K., Kalita, J. C., and Dalal, D. C. A fourth-order accurate compact scheme for the solution of steady Navier-Stokes equations on non-uniform grids. *Computers and Fluids*, 37:121–134, 2008.
- [119] Payne, R. B. Calculations of unsteady viscous flow past a circular cylinder. *Journal of Fluid Mechanics*, 4(1):81–86, 1958.
- [120] Pillai, A. C. R. Fourth-order exponential finite difference methods for boundary value problems of convective diffusion type. *International Journal for Numerical Methods in Fluids*, 37:87–106, 2001.

- [121] Powe, R. E., Carley, C. T., and Carruth, S. L. A numerical solution for natural convection in cylindrical annuli. *Journal of Heat Transfer*, 92(12): 210–220, 1971.
- [122] Quéré, P. L. Accurate solutions to the square thermally driven cavity at high Rayleigh number. *Computers Fluids*, 20:29–41, 1991.
- [123] Ray, R. K. and Kalita, J. C. A transformation-free HOC scheme for incompressible viscous flows on nonuniform polar grids. *International Journal for Numerical Methods in Fluids*, 62:683–708, 2010.
- [124] Reutskiy, S. and Lin, J. A RBF-based technique for 3D convection-diffusion-reaction problems in an anisotropic inhomogeneous medium. *Computers and Mathematics with Application*, 79:1875–1888, 2020.
- [125] Roshko, A. Experiments on the flow past a circular cylinder at very high Reynolds number. *Journal of Fluids Mechanics*, 10(3):345–356, 1961.
- [126] Sanyasiraju, Y. V. S. S. and Manjula, V. Flow past an impulsively started circular cylinder using a higher-order semicompact scheme. *Physical Review E*, 72:016709, 2005.
- [127] Sanyasiraju, Y. V. S. S. and Mishra, N. Spectral resolutioned exponential compact higher order scheme (SRECHOS) for convection-diffusion equations. *Computer Methods in Applied Mechanics and Engineering*, 197:4737–4744, 2008.
- [128] Schuh, H. Calculation of unsteady boundary layers in two dimensional laminar flow. *Zeitschr. f. Flugwiss*, 1:122–131, 1953.
- [129] Sen, S. *Compact biharmonic computation of the Navier-Stokes equations: Extension to complex flows*. PhD thesis, 2012.
- [130] Sen, S. A new family of (5,5)CC-4OC schemes applicable for unsteady Navier-Stokes equations. *Journal of Computational Physics*, 251:251–271, 2013.
- [131] Sen, S. Fourth order compact schemes for variable coefficients parabolic problems with mixed derivatives. *Computers and Fluids*, 134-135:81–89, 2016.



- [132] Sen, S. and Kalita, J. C. A 4OEC scheme for the biharmonic steady Navier-Stokes equation in non-rectangular domains. *Computer Physics Communications*, 196:113–133, 2015.
- [133] Sen, S., Mittal, S., and Biswas, G. Flow past a square cylinder at low Reynolds numbers. *International Journal for Numerical Methods in Fluids*, 67:1160–1174, 2011.
- [134] Sen, S., Kalita, J. C., and Gupta, M. M. A robust implicit compact scheme for two-dimensional unsteady flows with a biharmonic stream function formulation. *Computers and Fluids*, 84:141–163, 2013.
- [135] Sengupta, T. K. and Sengupta, A. A new alternating bi-diagonal compact scheme for non-uniform grids. *Journal of Computational Physics*, 310:1–25, 2016.
- [136] Sengupta, T. K., Bhaumik, S., and Shameem, U. A new compact difference scheme for second derivative in non-uniform grid expressed in self-adjoint form. *Journal of Computational Physics*, 230:1822–1848, 2011.
- [137] Shahraki, F. Modeling of buoyancy-driven flow and heat transfer for air in a horizontal annulus: effects of vertical eccentricity and temperature-dependent properties. *Numerical Heat Transfer, Part A*, 42:603–621, 2002.
- [138] Sharma, A. and Eswaran, V. Heat and fluid across a square cylinder in the two-dimensional laminar flow regime. *Numerical Heat Transfer, Part A*, 45:247–269, 2004.
- [139] Sharma, N., Sengupta, A., Rajpoot, M., Samuel, R. J., and Sengupta, T. K. Hybrid sixth order spatial discretization scheme for non-uniform cartesian grids. *Computers and Fluids*, 157:208–231, 2017.
- [140] Shi, Y., Zhao, T. S., and Guo, Z. L. Finite difference-based lattice Boltzmann simulation of natural convection heat transfer in a horizontal concentric annulus. *Computers and Fluids*, 35:1–15, 2006.

- [141] Shi, Z., Cao, Y., and Chen, Q. Solving 2D and 3D Poisson equations and biharmonic equations by the Haar wavelet method. *Applied Mathematical Modelling*, 36:5143–5161, 2012.
- [142] Shukla, R. K. and Zhong, X. Derivation of high-order compact finite difference schemes for non-uniform grid using polynomial interpolation. *Journal of Computational Physics*, 204:404–429, 2005.
- [143] Shukla, R. K., Tatineni, M., and Zhong, X. Very high-order compact finite difference schemes on non-uniform grids for incompressible Navier-Stokes equation. *Journal of Computational Physics*, 224:1064–1094, 2007.
- [144] Silva, A. L. F. L. E., Silveira-Neto, A., and Damasceno, J. J. R. Numerical simulation of two-dimensional flows over a circular cylinder using the immersed boundary method. *Journal of Computational Physics*, 189(2):351–370, 2003.
- [145] Soares, A., Ferreira, J., and Chhabra, R. Flow and forced convection heat transfer in crossflow of non-Newtonian fluids over a circular cylinder. *Industrial & Engineering Chemistry Research*, 44:5815–5827, 2005.
- [146] Sohankar, A., Norberg, C., and Davidson, L. Low-Reynolds-number flow around a square cylinder at incidence: study of blockage, onset of vortex shedding and outlet boundary condition. *International Journal for Numerical Methods in Fluids*, 26:39–56, 1998.
- [147] Sparrow, E. M., Abraham, J. P., and Tong, J. C. Archival correlations for average heat transfer coefficients for non-circular and circular cylinders and for spheres in cross-flow. *International Journal of Heat and Mass Transfer*, 47:5285–5296, 2004.
- [148] Spatz, W. F. and Carey, G. F. High-order compact scheme for the steady stream-function vorticity equations. *International Journal for Numerical Methods in Engineering*, 38:3497–3612, 1995.
- [149] Spatz, W. F. and Carey, G. F. A high-order compact formulation for the 3D

- Poisson equation. *Numerical Methods for Partial Difference Equations*, 12: 235–243, 1996.
- [150] Spotz, W. F. and Carey, G. F. Formulation and experiments with high-order compact schemes for nonuniform grids. *International Journal of Numerical Methods for Heat and Fluid Flow*, 8:288–303, 1998.
- [151] Spotz, W. F. and Carey, G. F. Extension of high-order compact schemes to time-dependent problems. *Numerical Methods for Partial Differential Equations*, 17:657–672, 2001.
- [152] Sutmann, G. and Steffen, B. High-order compact solvers for the three-dimensional Poisson equation. *Journal of Computational and Applied Mathematics*, 187:142–170, 2006.
- [153] Taneda, S. Visualization of separating stokes flows. *Journal of the Physical Society of Japan*, 46(6):1935–1942, 1979.
- [154] Thom, A. S. The flow past circular cylinders at low speeds. *Proceedings of The Royal Society A: Mathematical, Physical and Engineering Sciences*, 141: 651–669, 1933.
- [155] Thoman, D. C. and Szewczyk, A. A. Time-dependent viscous flow over a circular cylinder. *Physics of Fluids*, 12:II-76–II-86, 1969.
- [156] Tian, F., Ge, Y. B., and Tian, Z. F. Exponential high-order compact finite difference method for convection-dominated diffusion problems on nonuniform grids. *Numerical Heat Transfer, Part B: Fundamentals*, 75:145–177, 2019.
- [157] Tian, Z. and Ge, Y. A fourth-order compact finite-difference scheme for the steady stream function-vorticity formulation of the Navier-Stokes/Boussinesq equations. *International Journal for Numerical Methods in Fluids*, 41:495–518, 2003.
- [158] Tian, Z. F. and Dai, S. Q. High-order compact exponential finite difference methods for convection-diffusion type problems. *Journal of Computational Physics*, 220:952–974, 2007.

- [159] Tian, Z. F. and Ge, Y. B. A fourth-order compact ADI method for solving two-dimensional unsteady convection-diffusion problems. *Journal of Computational and Applied Mathematics*, 198:268–286, 2007.
- [160] Tian, Z. F. and Yu, P. X. A high-order exponential scheme for solving 1D unsteady convection-diffusion equations. *Journal of Computational and Applied Mathematics*, 235:2477–2491, 2011.
- [161] Tritton, D. J. Experiments on the flow past a circular cylinder at low Reynolds numbers. *Journal of Fluids Mechanics*, 6:547–567, 1959.
- [162] Tsui, Y. T. and Tremblay, B. On transient natural convection heat transfer in the annulus between concentric, horizontal cylinders with isothermal surfaces. *Internatioanl Journal Heat and Mass Transfer*, 27(1):103–111, 1984.
- [163] Vanka, S. P. Block-implicit multigrid solution of Navier-Stokes equation in primitive variables. *Journal of Computational Physics*, 65:138–158, 1986.
- [164] Wang, C. Y. The flow past a circular cylinder which is started impulsively from rest. *Journal of Mathematics and Physics*, 46:195–202, 1967.
- [165] Wang, J., Zhong, W., and Zhang, J. A general meshsize fourth-order compact difference discretization scheme for 3D Poisson equation. *Applied Mathematics and Computation*, 183:804–812, 2006.
- [166] Wang, Y. and Zhang, J. High accuracy and scalable multiscale multigrid computation for 3D convection diffusion equation. *Journal of Computational and Applied Mathematics*, 234:3496–3506, 2010.
- [167] Wang, Z., Fan, J., and Cen, K. Immersed boundary method for the simulation of 2d viscous flow based on vorticity-velocity formulations. *Journal of Computational Physics*, 228:1504–1520, 2009.
- [168] Watson, E. J. Boundary-layer growth. *Proceedings of the Royal Society of London (A)*, 231:104–116, 1955.

- [169] Williamson, C. H. K. Oblique and parallel modes of vortex shedding in the wake of a circular cylinder at low Reynolds numbers. *Journal of Fluids Mechanics*, 206:579–627, 1989.
- [170] Williamson, C. H. K. Vortex dynamics in the cylinder wake. *Annual Review of Fluid Mechanics*, 28:477–539, 1996.
- [171] Wu, J. and Shu, C. Implicit velocity correction-based immersed boundary lattice Boltzmann method and its applications. *Journal of Computational Physics*, 228:1963–1979, 2009.
- [172] Wundt, H. Wachstum der laminaren grenzschicht an schrag angestromten zylindern bei anfahrt aua der ruhe. *Ingenieur-Archiv Berlin*, 23:212, 1955.
- [173] Xu, A., Shi, L., and Zhao, T. S. Accelerated lattice Boltzmann simulation using GPU and OpenACC with data management. *International Journal of Heat and Mass Transfer*, 109:577–588, 2017.
- [174] Yang, X. and Kong, S. C. Numerical study of natural convection in a horizontal concentric annulus using smoothed particle hydrodynamics. *Engineering Analysis with Boundary Elements*, 102:11–20, 2019.
- [175] Yu, P. X. and Tian, Z. F. A compact streamfunction-velocity scheme on nonuniform grids for the 2D steady incompressible Navier-Stokes equation. *Computers and Mathematics with Applications*, 66:1192–1212, 2013.
- [176] Yu, P. X. and Tian, Z. F. A compact scheme for the streamfunction-velocity formulation of the 2d steady incompressible navier-stokes equations in polar coordinaes. *Journal of Scientific Computing*, 56:165–189, 2013.
- [177] Zdravkovich, M. M. *Flow Around Circular Cylinders: Fundamentals*, Volume 1. Oxford University Press, New York, 1997.
- [178] Zdravkovich, M. M. *Flow Around Circular Cylinders: Applications*, Volume 1. Oxford University Press, New York, 2003.

- [179] Zhang, J. An explicit fourth-order compact finite difference scheme for three-dimensional convection-diffusion equation. *Communications in Numerical Methods in Engineering*, 14:209–218, 1998.
- [180] Zhang, J. Fast and high accuracy multigrid solution of the three dimensional Poisson equation. *Journal of Computational Physics*, 143:449–461, 1998.
- [181] Zhang, J., Ge, L., and Gupta, M. M. Fourth order compact difference scheme for 3D convection diffusion equation with boundary layers on nonuniform grids. *Neural, Parallel and Scientific Computing*, 8:373–392, 2000.
- [182] Zhang, J., Ge, L., and Kouatchou, J. A two colorable fourth-order compact difference scheme and parallel iterative solution of the 3D convection diffusion equation. *Mathematics and Computers in Simulation*, 54:65–80, 2000.
- [183] Zhang, N., Zheng, Z. C., and Eckels, S. Study of heat-transfer on the surface of a circular cylinder in flow using an immersed-boundary method. *International Journal of Heat and Fluid Flow*, 29:1558–1566, 2008.
- [184] Zhang, W. and Yang, X. SPH modeling of natural convection in horizontal annuli. *Acta Mechanica Sinica*, 39:322093, 2023.
- [185] Zhao, B. and Tian, Z. High-resolution high-order upwind compact scheme-based numerical computation of natural convection flows in a square cavity. *International Journal of Heat and Mass Transfer*, 98:313–328, 2016.
- [186] Zhong, X. High-order finite-difference schemes for numerical simulation of hypersonic boundary-layer transition. *Journal of Computational Physics*, 144:662–709, 1998.
- [187] Zhuang, Y. and Sun, X. H. A high-order fast direct solver for singular Poisson equations. *Journal of Computational Physics*, 171:79–94, 2001.

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### Abstract

A class of compact finite difference schemes has been developed on nonuniform grids to tackle the convection-diffusion equation (CDE). A nonuniform grid has the leverage of clustering grids in higher-gradient regions and spreading out grid lines at other places, thereby making the computation less expensive. Contrary to the schemes available in the literature, the present schemes are obtained from using any kind of coordinate transformation to resolve nonuniform grids. The content of the present work can be divided into three parts. In the first part, a compact discretization of generalized 3D CDE on nonuniform grids is presented. This work on nonuniform grids consider presence of cross-derivative terms and the discretization uses only nineteen-point stencil. Extension of this newly proposed discretization to semi-linear and convection-diffusion-reaction problems is seen to be straightforward and this inherent advantage is thoroughly exploited. The scheme is found to be efficient in capturing boundary layers and preserve the nonoscillatory property of the solution. The proposed method is tested using several benchmark linear and nonlinear problems from the literature. Additionally, problems with sharp gradients are solved. These diverse numerical examples demonstrate the accuracy and efficiency of the scheme proposed. Further, the numerical rate of convergence is seen to approach four confirming theoretical estimation.

The second part of the work pertains to the implicit compact discretization of the Navier-Stokes (N-S) equations on nonuniform grids. Subsequently, the discretization is used to approximate the Boussinesq equation as well. This newly developed scheme is based on a comparatively smaller five-point stencil and leads to an algebraic system of equations with constant coefficients. The scheme carries the flow variable and its gradients as unknowns and is seen to report back



# NONUNIFORM PADE BASED COMPACT SCHEMES FOR FLUID AND HEAT FLOW PROBLEMS: DEVELOPMENT AND APPLICATION

*by* DHARMARAJ DEKA

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