

DECLARATION BY THE CANDIDATE

I, Pranjal Talukdar, hereby declare that the subject matter in this thesis entitled,

'Contributions to identities for the Rogers-Ramanujan continued frac-

tion, arithmetic properties of certain restricted partition functions, and

the least r-gaps in partitions' is the record of work done by me, that the con-

tents of this thesis did not form basis of the award of any previous degree to me

or to the best of my knowledge to anybody else, and that the thesis has not been

submitted by me for any research degree in any other university/institute.

This thesis is being submitted to the Tezpur University for the degree of Doctor

of Philosophy in Mathematical Sciences.

Date:

Place: Tezpur, Assam, India

Signature of the Candidate

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This is to certify that the thesis entitled, 'Contributions to identities for the Rogers-Ramanujan continued fraction, arithmetic properties of certain restricted partition functions, and the least r-gaps in partitions' submitted to the School of Sciences of Tezpur University in partial fulfilment for the award of the degree of Doctor of Philosophy in Mathematical Sciences is a record of research work carried out by Mr. Pranjal Talukdar under my supervision and guidance. All the help received by him from various sources have been duly acknowledged. No part of this thesis has been submitted elsewhere for award of any other degree.

Date:

Place: Tezpur, Assam, India

Nayandeep Deka Baruah

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Date: March 13, 2025

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Place: Tezpur, Assam, India

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Date: March 13, 2025

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