

DECLARATION BY THE CANDIDATE

I, Animesh Barman, hereby declare that the subject matter in this thesis entitled, **"Phenomenology of Neutrino Masses and Mixing with Discrete Flavour Symmetry in the context of the latest neutrino oscillation data."**, is a presentation of my original research work. Whenever contributions of others are involved, every effort is made to indicate this clearly, with due reference to the literature and acknowledgment of collaborative research and discussions.

The work is original and has not been submitted earlier as a whole or in part for a degree or diploma at this or any other Institution or University.

This thesis is being submitted to the Tezpur University for the degree of Doctor of Philosophy in Physics.

Place: Tezpur

Date: 17-04-2025



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No part of this thesis have been submitted elsewhere for award of any other degree.

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LIST OF PUBLICATIONS

- [Animesh Barman\(Tezpur U.\)](#), Ng. K. Francis(Tezpur U.), Bikash Thapa(Tezpur U.), Ankur Nath(Tezpur U.), "Nonzero θ_{13} , CP-violation and neutrinoless double beta decay for neutrino mixing in the $A_4 \times Z_2 \times Z_3$ flavor symmetry model", [Int.J.Mod.Phys.A 38 \(2023\) 02, 2350012](#)
- [Animesh Barman\(Tezpur U.\)](#), Ng.K. Francis, Hrishi Bora, "Neutrino Mixing Phenomenology: A_4 Discrete Flavor Symmetry with Type-I Seesaw Mechanism", [Modern Physics Letters A, Vol. 39, No. 7 \(2024\) 2350200](#)
- [Animesh Barman\(Tezpur U.\)](#), Ng.K. Francis, Hrishi Bora, "Neutrino Mixing Model in the context of $\Delta(27) \times Z_3$ Flavor Symmetry using Type-I Seesaw Mechanism", [Communicated to Modern Physics Letter A journal](#)
- Hrishi Bora(Tezpur U.), Ng.K. Francis(Tezpur U.),[Animesh Barman\(Tezpur U.\)](#), Bikash Thapa(Tezpur U.), Neutrino Mass Model in the Context of $\Delta_{54} \times Z_2 \times Z_3 \times Z_4$ Flavor Symmetries with Inverse Seesaw Mechanism, [Phys.Lett.B 848 \(2024\) 138329](#)
- Hrishi Bora(Tezpur U.), Ng.K. Francis(Tezpur U.),[Animesh Barman\(Tezpur U.\)](#), Bikash Thapa(Tezpur U.), Majorana neutrinos in Inverse Seesaw and $\Delta(54)$ Flavor Models, [International Journal of Modern Physics A, Vol. 39, Nos. 15 and 16 \(2024\) 2450066](#)

BOOK CHAPTER

- [Animesh Barman\(Tezpur U.\)](#), Ng. K. Francis(Tezpur U.), Bikash Thapa(Tezpur U.), Bichitra Bijay Boruah(Tezpur U.), Ankur Nath(Tezpur U.), "Nonzero θ_{13} and Neutrinoless Double Beta Decay for neutrino mixing and A_4 discrete flavor symmetries" published in "[Advances in Physics and its Applications](#)", Duliajan College, Duliajan, Dibrugarh, Assam, India, November 26-27, 2021
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- Hrishi Bora(Tezpur U.), Ng. K. Francis(Tezpur U.) and [Animesh Barman\(Tezpur U.\)](#), and " Δ_{54} flavor model for Dirac neutrinos: inverse seesaw" to be published in [PANE-2022](#), Manipur University, Manipur, India, November, 08-10, 2022

PAPER PRESENTED IN WORKSHOP / CONFERENCE

- [Animesh Barman\(Tezpur U.\)](#) and Ng. K. Francis(Tezpur U.), "Non-zero θ_{13} and Neutrinoless Double Beta Decay for neutrino mixing and A_4 discrete flavor symmetries"- paper presentation in an International Conference on "Advances in Physics and its Applications (APA-2021)", Duliajan College, Duliajan, Dibrugarh, Assam, India, November 26-27, 2021
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Declaraton

The work in this thesis is based on research carried out at the Institute of Tezpur University, Department of Physics, Tezpur, Assam, India. No part of this thesis has been submitted elsewhere for any other degree or qualification and it is all my own work unless referenced to the contrary in the text.

Animesh Barman

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Abbreviations

Abbreviation	Meaning
SM	Standard Model
CP	Charge-Parity
BSM	Beyond Standard Model
LHC	Large Hadron Collider
keV	Kilo Electron Volt
PMNS	Pontecorvo–Maki–Nakagawa–Sakata
CKM	Cabibbo–Kobayashi–Maskawa
MSW	Mikheyev-Smirnov-Wolfenstein
SAGE	Soviet–American Gallium Experiment
GALLEX	Gallium Experiment
GUT	Grand Unified Theory
KamLAND-Zen	Kamioka Liquid Scintillator Anti- Neutrino Detector-Xenon
LSND	Liquid Scintillator Neutrino Ditector
MiniBOONE	Mini Booster Neutrino Experiment
MINOS	Main Injector Neutrino Oscillation Search
BNL	Brookhaven national laboratory
TBM	Tri-bimaximal Mixing
HM	Hexagonal Mixing
GRM Golden Ratio Mixing	
WMAP	Wilkinson Mass Anisotropy Probe
eV	Electron Volt
TeV	Tera Electron Volt

VEV	Vacuum Expectation Value
NH	Normal Hierarchy
NO	Normal Ordering
IH	Inverted Hierarchy
IO	Inverted Ordering
B+L	Baryon+Lepton
CERN	European Organization for Nuclear Research
LEP	The Large Electron-Positron Collider
ISS	Inverse Seesaw
NDBD($0\beta\beta\nu$)	Neutrinoless double beta decay
DM	Dark Matter
BAU	Baryon Asymmetry of Universe
BBN	Big Bang Nucleosynthesis
CMB	Cosmic microwave background
LNV	Lepton Number Violation
LFV	Lepton Flavour Violation
DW	Dodelson-Widrow

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