SIGN PATTERNS AND CONGRUENCES OF CERTAIN INFINITE PRODUCTS INVOLVING THE ROGERS-RAMANUJAN CONTINUED FRACTION, ARITHMETIC PROPERTIES OF SOME PARTITION FUNCTIONS, AND PARITY BIASES IN INTEGER PARTITIONS

A THESIS SUBMITTED IN PARTIAL FULFILMENT OF THE

REQUIREMENTS FOR AWARD OF THE DEGREE OF

DOCTOR OF PHILOSOPHY

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