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## Some Studies on

## Information Representation and Transmission

Thesus<br>submitted by

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under the gurdance of
Prof. S Nandi and Prof. M C Bora
. for the award of the degree DOCTOR OF PHILOSOPHY

Departiment of Computer Science
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## Certificate

This is to certify that the thesis cutitled " Some Studies on Information Representation and Transmission", submitted by Dhruba Kumar Bhattacharyya, a research scholar in the Department of Computer Science, Tezpur University, Tezpur, for the award of the degree of Doctor of Philosophy, is a record of an original research work carried out by him under our supervision and guidance. The thesis has fulfilled all requirements and in our opinion has reached the standard needed for submission. The results embodied in this thesis have not been submitted to any other University or Institute for the award of any degree or diploma.


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(D.K. Bhatorharey ya)


#### Abstract

The present thesis embodies a study of 3 -neighbourhood additive Cellular Automata (CA) behaviour and its applications in authentication and authenticated key exchange. Earlier works in the field of CA have been reviewed. Subsequently, characterization of Extended Neighbourhood CA (ENCA) (not explored by previous researchers) and its application in data encryption are presented. Various error control coding techniques for $t$-Error Correcting (EC)/d-Error Detecting (ED) and All Unidirectional Error Detecting (AUED) codes as well as Single error correcting (SEC)/Double error detecting (DED)/AUED codes have been reviewed. Two novel techniques, one for $t$ - $\mathrm{EC} / d$ ED/AUED codes and the other for SEC/DED/AUED codes respectively are presented. For efficient handling of multimedia data as well as for conceptual representation of any complex hypermedia domain, an existing data model, referred as Relationship Management Data Model (RMDM) has been analysed and subsequently modified. The modified RMDM has been implemented and the results are embodied in the present thesis. Further, it also introduces a user-friendly, three-layered image database system (IDS) architecture for handling complex queries over large repository of images. To assist in better understanding of the complex queries, the thesis also presents a visual semantic data model.


Keywords : Cellular Automata(CA), Extended Neighbourhood CA (ENCA), Authentication, Data encryption, Password-only Authenticated Key Exchange (PAKE), All Unidirectional Error Detection (AUED), Hypermedia, Relationship Management Data Model (RMDM), Image Database System (IDS), Visual Semantic Model (VSM).

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## Abbreviations Used

| CA | Cellular Automata |
| :--- | :--- |
| MACA | Multiple Attractor CA |
| NBCA | Null Boundary CA |
| PBCA | Periodic Bounday CA |
| ENCA | Extcndled Ncighbourhood CA |
| PCA | Programmable CA |
| CHA | Cellular based Hash Function |
| XNOR | Exclusive NOR |
| XOR | Exclusive OR |
| CPAKE | Cellular based Password-only Authenticated Kcy Exchange |
| SEC | Single Eiror Correcting |
| DED | Double Euor Contecting |
| AUED | All Unidirectional Error Detecting |
| ROM | Random Only Memory |
| VLSI | Vcry Large Scale Integrated Circuit |
| RMDM | Relationship Management Data Model |
| IDS | Image Database System |
| VSM | Visual Semantic Data Model |

## Chapter 1

## Introduction

In the last five decades of its existence, the modern computer has come a long way from doing just the basic number cıunching. In terms of computing power, small personal computers easily out-perform large main-frame machines of yester-years. In terms of the spread of functionality, we notice an ever increasing use of computer systems in data management. Advances in communication technologies have further fueled the use of information technology in distributed environment, whether it is for managing online transaction across a large distributed network, or in maintaining large databases often containing unstructured information including multi-media data. With this everincreasing growth of computer and communication technologies, the need for efficient and secure epresentation of data and its reliable transmission have become the basic necessities.

Secure representation of data for preventing the un-authorised interception is a lcgitimate necd of not only the government institutions including the defense scrvices in particular, but, also of the business sector and private individuals. Authentication, data security, digital signature and file security are the various elements that need to bo examined for protecting data in computer and distributed database systems from unauthonized disclosure and modification To solve the secmity problems in any distributed application, basically four kinds of mechanisms are used, such as pmovacy, authenticateon, antegrety and scalablzty. Privacy includes the desire to keep documents and communication secret, as well as to hide the very existence of certain kinds of infomation and to potect the identities of the paties communicaling with cach other. Authentication and integrity refer to the need to confim the identity of user, the anthenticity of messages and the integrity of messages or connections. Scalability mechanisms such as distribu-
tion centers and digital certificates, add another crucial aspect to the success of any such applications, because they help in creating systems that involve millions of users, transactions and documents. Among these four measuics, privacy and authentication problems are serious, and special care is nceded to design appropiate schemes for data security and for user as well as message authentication. Significant iescauch work has been catricd out over the past decade to investigate these two problems and several enciphering and authentication schemes [Denni82, Reupl86, Welsh88, Sebry89, Schnr96, Palch97] have been evolved. However, a study of these schemes has icvealed that - most of the existing enciphering schemes ane imptactical, mainly due to, either the use of a lage kry or the need of a ciphertext much larger than the plain-text. It appears that the time and icsource complexities of the existing authentication schemes are also significantly lange [Schnr96], which make the hardware implementation more complicated. From the analytical study of additive Cellular Automata (CA) it is observed that - the simple, ı egula stuucture-based features of $\mathrm{C} \Lambda$ can be utilized for designing secure and hardware efficient schemes for authentication and data encryption.

With the advancement in the convergence of computer and communication technologies, the demand for efficient and reliable digital data transmission and storage systems has also been increasing. This demand has been accelerated by the emergence of large-scale, high-speed data networks for exchange, processing and storage of digital information in the military, government and private spheres. In this background, a major concern of a researcher is to contiol the errors so that reliable reproduction of data can be obtained. Basically, the computer systems encomiter three classes of errors: symmetric, asymmetric and unzdreectronal. Among the various types of causes of errors, such as : transient, intermittent and permanent, it is seen that the transicnt cirors are icsponsible for mostly limited number of symmetric or multiple unidirectional errors. The intermittent faults cause limited mumber of errors, but the pemmanent faults may cause both symmettic as well as the unidirectional errors. In this context several error contiol codes have been proposed [Bosc82, Lin83, Wickr96, Bosc85, Nikol86, Lin88, Tao88, Blaum89, Rao89, Boinc90, Kundu90, Montg90, Nikol91, Bruck92, Basam94]. However, still there is a gıowing demand for construction of some simplified, storage-efficient, casily implementable symmetric error(s) correcting codes, which can also simultancously detect all Unidinectional errors.

Now-a-days, every new step torvads the advancement in technology centers around new ways to store, retuieve and taansmit various types of infomation. In the past
five years there has been growing interest in hypermedia design approaches [Garzo93a, Isakw95, Lange94]. There are many different problems the hypermedia designer has to deal with, since the combination of navigation though an intricate infomation space with the unstructured and dynamic nature of multimedia data poses new and complex problems that must be solved in a systematic and modular way. Each design activity in a design methodology should address difficult concerns at the proper stage and at the proper level of abstraction. To model the complex navigation patterns of any hypermedia application domain in a conceptual manner, the modelling tool should be rich enough from semantical point of vicw. From the current review, it is observed that RMDM [Isakw95] fulfills most of the criteria necessary for any complex, regular structure-based hypermedia applications.

Visual information is known to be a persuasive, intuitive and most expressive communication medium for humans. Its usefulness and usability have been incueasing widely with the advent of systems handling multimedia information in a variety of application aucas including natural sciences, military, industry and medicine. With the emerging technologics in high-speed communication networks and the presentation techniques, in particulat, there has been a great demand for high-quality information processing that requires a suitable Image Database Systems (IDS) architecture with efficient image indexing and ietrieval mechanisms Because of the large volume and difficultics in analyzing the contents of images, regardless of whether they are still images or video, however, it iemains to be an investigating problem to effectively store and retrieve them based on theria contents

In the backgromed of the above scenario, the peesent thesis has utilized the simple and regular structure of CAs for the design of one-way hash function, data encryption and password-based authenticated key exchange schemes. The thesis also includes constuction of two simple and lessen handwac-based enot conection and delechon sehemes Further, it also discusses two key issues and thei solutions relating to multimedia data modelling and image database processing The next section biefly ieports the majot contibutions of the previous researchers in these fields Subsequently, it presents the schemes designed and developed to provide better solutions to some of the well-known infonmation eppesentation and thansmission bottlenecks

### 1.1 Information Representation and Transmission

A brief review of the earlicr studies on various issucs relating to information representation and transmission is seported in this subsection. Some of the key issucs relevant to CA based applications, enor correction/detection, hypermedia application design, image database processing and retrieval are highlighted.

### 1.1.1 CA and Its Applications

J. von Neumanu [Ncuma66] first iniliated the study of Cellular Automata (CA) and he framed $\mathrm{C} \Lambda$ as a cellular space with self-reproducing configurations involving 5neighborhood cells, cach having 29 states. Subsequently, theory and application of CA have been developed in diverse arcas such as pattern rccognition, modelling, biological and physical systems, parallel computation ctc. Study of regular structure of C $\Lambda$ has drawn considerable attention in recont, years [Alady76, Tollo 77, Wolfi83, Wolfr84, Wolfr85a, Wolfi 85b]. However, it is not possible to characterize null boundary and hylbrid CAs with polynomial algebraic tools. Recently, a more versatile tool based on matrix algebıa [Das90b, Barde90, Das91] has been proposed to characterize 3-neighborbood additive CAs. Different applications of additive CAs have been invesligated [Palch97, Nandi94a, Mista92, P!̣ies86, Serra90, Das93] Major applications of 3-ncighborhood additive CA proposed so fir can be categorized as: (i) pseudo-random, pseudo-cxhaustive and deterministic patlem generation [Palch97, Nandi94a, Das93, Chowd92, Barde90], (ii) synthesis of ensily testable Finite Statc Machine (FSM) design [Palch97, Nandi94a, Chowrl92, Msta92], (iii) bata cnciyption [Palch97, Nandi94a], (iv) Euror Correcting Codes [Palch97, Chowf192], (v) Hashing [Palch97, Chowd92] and (vi) Signatur analysis [Palch97, Misra82, Sena90, Das90a, Das90b]. 'The analytical study of the simple and regular structuc of CA has motivated us to further investigate the $\mathrm{C} \Lambda$ behaviour and devolopuent of its applications in the various fields of ciyptography. Various developments in thee major areas of cryptography proposed so far are as follows

1. Nessage Authentication using one-way hash function [Demis2, Welsh88, Selny89, Schm96, Merkl90, Rivst92, NiST93, Rhece94, Simon92, Mencz97, Zheng93, Vaude95, Dobhr96, Dugrd90, Daemu93a, Dacmu93b, Schno91, Schno93].
2. Data Encryption [Dcuni82, Welsh88, Sebıy89, Schnr96, Palch97, Simon92, Menez97].
3. Authenticated key exchange [Scbry89, Schm96, Belvn92, Diffi79, Difli92, Belvn92, Gong93, Jabln96, Oorsc96, Simon92, Mcnez97, Meıkl79]

### 1.1.2 Symmetric Error Correction and All Unidirectional Error detection

Curient survey icveals that many faults in VLSI circuits (such as the faults that aflect addeess decoders, word-lines, power supplies and stuck-fault in a scial bus, faults in ROMs and RAMs etc) cause mostly, unidirectional errors. The number of symmetnic eroos is usually limited while the mumber of uniditectional enoms may be very large. In this background, sevelal erior control codes have been studicd [Bosc82, Lin83, Bosc85, Nikol86, Lin88, Tao88, Blaum89, Rao89, Boinc90, Kundu90, Montg90, Nikol91, Buck92, Basam94, Katti96a, Katti96b, Laih96]. It is felt that, construction of a haudware efficient, new class of symmetric error(s)correcting codes is very essential, which would be able to detect all uniditectional errors simultancously.

### 1.1.3 Hypermedia data Modelling

Data modelling is an cssential patt of any systematic and modularized hypermedia application development process. The modelling requirements for a hypermedia data model are different fion the ladıtional data models, paticularly from navigational point of view. A hypentedia data model should be capable enough in expressing the semantics of the multimedra object-rclationships including the navigational aspects Several hypertext and hypermedia data models have been studied from [1sakw95, Hofst93, Hnghe91, Tcory86, Halas94, Leget94, Schms93a, Schns93b, Stots80, Garzo93a, Gazo93b, Karme96, Bomel91] RMDM (Relationship Management Data Model) [5sakw95] is one of those models, which was proposed for any complex, icgular stucture-based hypemeda applicatoons it is ohserved that in the context of several modratedy complex hypemedi. domans, the afores, did model fails to expmess some of the situations in a conceptual manner. 'This has motivated us to further investigate RMDM to find the solutions necessaty to overenme the limitations detected so fat

### 1.1.4 Image Database Processing and Retrieval

Answering a useı-query in an image database system (IDS) typically requires correlation of digital data stored in different formats such as PCX, TIFF, GIFF, TARGA, BMP etc. Correlating these various picces of information at the physical level by pre-analysis is not an attractive option. For example, there could be thousands of image-objects that could be recognized in a scene, but linking all of these objects to relcvant textual or structured data would be very time consuming and un-rewarding process [Kashp95, Subra96]. It is believed that to support the conclation of all this information, it is necessary to represent, the iclevant digital data in semantzc level. In genctal, humans ate more capable than machines for abstracting information efficiently fiom images displayed on the computer This cnables them to correlate information at a higher semantic level with other forms of epresentations such as the symbolic iepeesentation of data in stutheured databases This conclation of infomation at a semantic level in an efficient manner, across different representations is lacking in the cxisting IDS architectures and has been characterized as a scinantic botule-neck [Kashp94, Kashp95, Subia96, Jain94]. Rescarchers have looked into this problem of designing a suitable metadata-based architecture, and some preliminary works have becu ıcported [Jain94, Gupta91, Chu94, Subra96, Klaus94]. It seems necossary to carry out further investigations on this problem of designing a suitable IDS architccture

### 1.2 Aim of Work

The main objective of the thesis is to explore $\mathrm{C} \Lambda$, find some new characterizations and its applications in ctyptography ' The thess has also amed to study the experesiveness of the existing hypermedia data, models from conceptualization point of view. Further, it is also aimed to develop a suitable a chitect,me for image database applications, in espective of its nature, type or scale-factors

The thesis reports chatacterization of some of the group and non-group Extended Neighborhood CAs (ENCAs) based on a matix algehaic tool. It has been shown that there exist E'oup ENCAs which sathsfy all the popentics of maximmm-lenghand nommaxmum length 3-ncighbonhoor additive group CAs Such maximum-length group CAs are uscful for genctation of high quality psende-random pattens [Nandi9ia]. It
has been shown that there exists a class of non-group ENCAs, which satisfy all the properties of TPMA CAs [Nandi94a]. Such non-group CAs are utilized for generating powetful hashing function.

Based on the above charactenzation, CA based applications have been developed in the following directions :

1. CA based one-way hash function : propertics of non-group, non-linear complemented MACAs (Multiple Attractor CA) are utilized in defining a onc-way hash function. To improve the intıuders' complexity, CA based block ciphering functions [Nandi94a] are used as pec-ptocessing steps to the MACA-based hashing modulc. The whole hashing process is operated in a feedback mode for several cycles.
2. CA based data encryption : a block enctyption scheme has been developed based on the ultimate periodicit, properties of group ENCAs. To improve the intruders' complexity, it utilizes a CA-based prumutation scheme [Nandi94b] as a pre-processing step to the ENCA based block cipher. Due to the many-to-many mapping among the plaintext and ciphertext blocks, and due to the exponential or der of key-space size, the scheme is guarded against all possible types of intruders' attacks.
3. CA based password-only authenticated key exchange : using the CA based schemes (for authentication aud data enciyption) developed so far, a new authenticated key exchange scheme based on a small password is developed. Due to the regular, modular and cascadable logic structure of CAs, the scheme has been found to be significaut in comparison to the existing schemes The scheme was examined in light of the various known as well as unknown attacks and it has been found to be guarded and secure.

Besides, we have also cxtended our work in the following diections:
4. Error detection and correction : a new scheme to construct a $t$-EC/d-ED $(t<d)$ and AUED systematic codes with faster and lesses hardware is discussed and established For langer values of $t$, in majority of cases, the proposed codes need Lesser mumber of clack-bits A new class of Single Enor Conection (SEC) / Double Eur Detection (DED) and All Unidinctional Enfor Detection (AUED) codes also have bern developed based on odd-wenght column matior for even-panty check In
case of both the schemes, the ROM based implementation show significant results by roducing the ROM word-length.
5. Study and analysis of hypermedia data models : an analysis of a structured hypermedia application data model, referred as RMDM (Relationship management data model) [Isakw95] is discussed. Some drawbacks of RMDM are detected and subsequently, possible iemedies also have been given, which ultimately extend the picsent RMDM to enable the inodellers to represent any scale of application domains in a conceptual manner. Some implementation results based on the extended RMDM also have been reported.
6. Nèw architecture for image database system : a modular, threc-layeıcd and user-fiiendly architecture for image database proccssing and retrieval, based on content-based and text-based features is pesented. For better understanding of the complex queries, a visual semantic datia model also has been defined. Fut then, for the sake of testing and justification, a prototype implementation of the proposed architecturc also has becu discussed.

The main contributions of the iescarch work can be summerised as follows :

- Charactenization of extended ncighborhood additive CA behaviours (not explored by picvious researchers).
- CA based one-way hash function design.
- Design of C $\Lambda$ based data encryption scheme.
- Design of CA based authenticated key exchange based on a small password.
- Desigu of
- SEC/DED/ $\Lambda$ UED systematic Codes,
$-t-\mathrm{EC} / d-\mathrm{ED} / \Lambda \mathrm{UED}(t<d)$ systematic codes.
- Analysis of RMDM ( a hypermedia data model), detection and reporting of the diawbacks of RMDM, remedies to overcome the datwbacks as well as to extend the RMDM and finally implementation of the extended RMDM.
- Design of a new image database system architecture and to assist in the query solving mechanism, derelopment of a scmantic data model.


### 1.3 Thesis Organization

To fulfill the aforesaid objectives, the research work reported in this thesis has been organized as follows :

- Prior to describing the application of cellular automata for design of onc-way hash function, data encryption and authenticated key exchange schemes, the homogeneous structure of CA and its characterization based on matrix algebraic tool are briefly reviewed in Chapter 2. Some new chatacterization of the ENCA bchaviours using matrix algebra as a tool, has also been reported.
- Based on the propertics of non-group, non-lincar complemented MACAs, a oncway hashing scheme is presented in Chapter 3. Application of such a CA based hash function in Electronic Economy has also been elaborated
- Based on the state transition features of group ENCAs, a block cipher system is presented in Chapter 4. Exploitation of programmable structures of additive group CAs in obtaining better randomness among the plaintext and ciphertcxt blocks, in the proposed cipher system, has also becı reported.
- A now schenic on password-based authenticated key exchange, designed using the CA based schenies discussed so far in the previous chapters(Chapter 3 \& 4) has been presented in Chapter 5. Various applications of such CA based schemes also has becn established.
- Design of two efficient error control coding schemes has been presented in Chapter 6.
- Analysis of hypermedia data model in the context of a rcal-life case has been discussed Chapter 7; some drawbacks ane detected and for remedies, solutions are suggested towards the extension of the data model. For justification of the extensions, implementation results auc included
- New architecture for an image database system and its implementation issucs in the context a real-life case have been reported in Chapter 8
- Finally, Chapter 9 summenised the overall contabutions of the thesis and adentifies future iescarch directions in the relevant fields

CHAPTER 1. INTRODUCTION

## Chapter 2

## Properties of Cellular Automata and its extension

### 2.1 Introduction

In early 50 s, J. von Neumann first introduced Ccllular Automata (as a 'ccllular spacc') to study the complex structures capable of self-reproduction and self-repair [Neuma66]. Following him, several researchers have taken interest in the study of CA for modelling the behaviour of complex systems. Theory of CA reccived a consolidated attention by Burks [Burks70] and considerable simplifications were introduced by Codd, Banks, and Smith [Codd68, Palch97]. CA has been investigated as a class of Mathematical tool in early 75's for modelling a wide variety of biological systems such as self-reproduction, birth, growth, death etc. The development of structures and patterns in the growth of otganisms, as pointed out, in [Steve74], often appear to be governed by vety simple local rules and can be modelled with a CA. Aladyev [Alady76] has surveyed vaious computational and theoretical aspects of CA, particulanly the decidability of reachability problem for configurations. CA has also been used as a tool to study number theory and associated applications [Millc70, $\Lambda$ psim70]

However, it can be observed that in the carly phase of the development, the theory has evolved in a bit unsystematic and fragmented way Several rescatchers' persistent efforts [Yamad71, Amoo 72, Richa72, Harao78, Toffo77, Wills75] icsulted in the con-
solidation of the theoretical framework; they started analyzing CA by means of well tested mathematical tools such as abstract algebra, topology, measure theory, etc. Current intensive interest in this field can be attributed to the significant development of efficient schemes such as those for data encryption, pseodorandom pattern generation, error conrection/detection etc. with the cost effective realization of the CA structure. In this chapter, development of CA and its applications in diverse fields have been briefly revicwed. It also introduces some new characterizations of the Extended Neighbourhood CA and its applications. In the following section, present development of CA based on the Wolfram's extensive investigations has been discussed bricfly.

### 2.2 Present development of CA

Wolframs' investigations [Wolfr83, Wolfr84, Wolfi85a, Wolfr85b] on CA confirmed its usability as a mathematical model for self-organizing statistical systems. Several new charactcistic features of self-organization in uniform 3-neighbourhood (lcft, right and self vide Fagure 2.1) infinite CAs with 2-state per cell, were identified by him based on polynomial algebra.

The stiucture of a CA investigated by Wolfram can be viewed as a discrete lattice of sitcs (cells) where each cell can assume either the value 0 or 1 [Palch97]. At discretc time step (clock cycle), the evolution of a site value depends on some iule (a combinational function), which is a function of the prescut state of ' $k$ ' of its neighbours for a $k$-neighbourhood CA. For a 2 -state 3 -neiglibourhood CA, the evolution of the $\imath^{\text {th }}$ cell can be represented as a function of the prescit states of $(i-1)^{\text {th }},(i)^{\text {th }}$ and $(\imath+1)^{\text {th }}$ cells as • $q_{2}(t+1)=f\left\{q_{\imath-1}(t), q_{2}(t), q_{1+1}(t)\right\}$, where $\int$ represents a combinational function. In effect, each cell as shown in Fugure 2.1, consists of a storage elcment (D flip-flop) and combinational logic implementing the next state function.

In this Cellular Automata, there anc $2^{3}$ distinct neighbouhood configurations and $2^{2^{3}}$ distinct mappings from all these neighbourhood configurations to the next state; each mapping represents a $\mathrm{C} \Lambda$ rule

| Neighbourhood State • | 111 | 110 | 101 | 100 | 011 | 010 | 001 | 000 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Next State: | 0 | 1 | 0 | 1 | 1 | 0 | 1 | 0 | (Rule90) |
| Next State : | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | (Rule150) |




Figure 2.1: A typical CA cell

The top row gives all the 8 possible states of the 3 neighbouring cells at the time instant $t$, while the second and third rows give the conesponding states of the $2^{\text {th }}$ cell at time instant $t+1$ for two consecutive CA rules. A detailed study of the truth tables for these rules can be found in [Palch97]. If in a CA the same rule applies to all of the cells, then the CA is referred to as a uniform CA; otherwise the CA is called hybrid CA. If the rule of a CA cell involves only XOR logic, then it is called a linear rule. Rules involving XNOR logic are referred to as complemented rules. A CA with all the cells having linear rules is called a linear CA, whereas a CA having a combination of XOR or XNOR rules is called an additive CA. The CA with non-lincar rules is called non-linear CA.

A CA is said to be a Periodic Boundary CA (PBCA) if the extreme cells are adjacent to each other (Figure 2.2). A $\mathrm{C} \Lambda$ is said to be aNull Boundary CA (NBCA) if left(right) neighbour of leftmost(rightmost) terminal cell is connected to logic-0 state.

However, the polynomial algebra-based analytical tool has some difficulties in characterizing the hybrid $\mathrm{C} \Lambda$ employing non-unifom rules Also, a detailed polynomial algebraic analysis on non-group CA, had been lacking for long time. To overcome this, a new analytical tool based on matrix algebra [Das90b, Barde90, Das91] has been developed. In the next section, for the sake of completeness, some properties and icsuits of 1-D 3-neighbouhood additive CA based on this matrix algebraic tool have been reported from [Palch97].

Definition 2.1 An $n$-bit complement vector associated with an $n$-coll complemented
 cell to be a complemented one


$$
\begin{gathered}
T=\left[\begin{array}{llll}
0 & 1 & 0 & 1 \\
1 & 1 & 1 & 0 \\
0 & 1 & 0 & 1 \\
1 & 0 & 1 & 1
\end{array}\right] \\
T=\left[\begin{array}{llll}
x & 1 & 0 & 1 \\
1 & 1+x & 1 & 0 \\
0 & 1 & x & 1 \\
1 & 0 & 1 & 1+x
\end{array}\right]
\end{gathered}
$$

Characteristic polynomial $=x^{4}+x^{2}$
Figure 2.2: Four cell periodic boundary CA with iule vector $\langle 90,150,90,150\rangle$

Corresponding to each complemented CA, there exists a non-complemented CA whose state transition behaviour can be utilized as follows to derive the behaviour of the complemented one. For a complemented CA with the complement vector $S_{c}$, the next state $S(t+1)$ of a present state $S(t)$ is represented as

$$
S(t+1)=[T] S(t) \oplus S_{c}
$$

where $[T]$ is the CA matrix of the corresponding non-complemented CA. The state transition diagrams of cellular automata have been characterized using the $[T]$ matrix and its chaacteristic polynomial. Depending on the nature of their state transition behaviour, CA can be broadly classified into two classes - (i) group CA and (ii) nongroup CA. In the state transition diagram of a group CA all states are cyclic; cach state has a unique successor and a unique predecessor state. The state thansition diagram of two group CAs are shown in Figure 2.3 \& 2.4.

For the sake of completeness, some of the basic definitions and fow importanit results related to group and non-group CAs have been reproduced from $[$ Das90b, Prics86, Barde90, Scrra90, Nandi94a] below.

Group CA :A group CA has been identified by the condition that the [T] matrix is nonsingular. In other words, there must exist some positive integer $p$ such that $[T]^{p}=I$ (the edentaty matrix), and $S(t+p)=[T]^{p} S(t)=S(t)$


Figure 2.3: The state transition diagram of a nommaximum length group CA


Figure 2.4: The state transition diagram of a maximum length group CA

Theorem 2.1 A CA is a group $C A$ if and only if the determinant $\operatorname{det}[T]=1$, where $[T]$ is the charactcristic matrix of the $C A$.

Theorem 2.2 A group CA has a cycle of length $p$ or factors of $p$ with a nonzcro starting state if and only if $\operatorname{det}\left[[T]^{p} \oplus[I]\right]=0$.

Theorem 2.3 Let $\bar{T}^{\mathfrak{p}}$ denote application of the complemented rule $\bar{T}$ for $p$ succossive cycles, then

$$
T^{\prime} S(t)=\left[I+T+T^{2}+\cdots+T^{p-1}\right]\left[S_{c}\right]+\left[T^{p}\right][S(t)]
$$

where $T$ is the characteristic matrix of the corresponding non-complemented rule vector and $\left[S_{\mathrm{r}}\right]$ is an $n$-dimensional vector ( $n=$ number of cells) iesponsible for inversion after XORing. $S_{c}$ has '1' entries (i.e. nonzero entries) for CA cell positions wher XNOR. function is cmployed.

Theorem 2.4 The complement of a group $C A$ is also a gıoup $C A$.
Theorem 2.5 CA rules 60, 102 and 204 form groups for all longths(l) with a group
order $O(G)=p=2^{a} ; a=0,1,2, \cdots ; m \geq l>m / 2$.
Group CAs can further be classified into non-maxımum (Fıgure 2.3) and maxımum (Figure 2.4) length CAs. An $n$-cell maximum length $C A$ is characterized by the prosence of a cycle of length $\left(2^{n}-1\right)$ in the corresponding state transition diagram and a primitive characteristic polynomial.

All states of a CA with complemented counter part (with rule 195, 153 and 51) form cycles of equal length and cycle length is $2^{3}$, where $j=1,2,3, \cdots$ and $j \neq 0$ [Nandi94a].

Lemma 2.1: Complemented CA rules 195, 153 and 51 form groups for all lengths with group order $O(G)=m=2^{a} ;(a=1,2,3, \cdots)$.

Theorem 2.6 : If a null boundary uniform or hybrid CA configured with rules 51, 153 and 195 is a group CA, then its state transition diagram consists of cqual cycles of cren length.

The null boundary CA with rule configuration $\langle 153,153,153,153\rangle$ generates cycles as shown in Figure 2.5.



Figure 2.5: The state transition diagram of a nonmaximum length group $\mathrm{C} \Lambda$

In periodic boundary conditions, the only rule available forming equal cycles of even length is rule 51.

Non-Group CA : In a non-group CA (Figure 2.6), all the states are not cyclic, moreover, a state can have 0 or $2^{p}(p \geq 1)$ number of predecessors (Figure 2.7). In the state transition diagram of a CA, a state is said to be reachable if it has one or more predecessors. A state without any predecessor is referred to as a non-reachable statc. Reachable states which form cycles are called cyclic states.

Definition 2.2 A state with a self-loop is referred to as a graveyard state (or attractor). In other words, an attractor is a unit length cyclic statc.

In the state transition graph, level of a state $S_{\imath}$ is defined as the minimum number of time steps required to reach a cyclic state starting fıom $S_{1}$ Level of a cyclic state is counted to be zero. In Frgure 2 7, level of state '15' is 2. 'Thus node 15 can be marked as 2 -level predecessor of the attractor 3 .

Definition 2.3 Depth of a CA can be formally definced as the minimum number of time steps required to reach a cyclic state from a state in the highest level of the state transition diagram of the CA.

Depth of the CA in Figure 2.7 is 3. All the $\imath$-level ( $0 \leq \imath \leq d$ ) predecessors of an attractor form an inverted tree rooted at the attractor, where $d$ is the depth of the tice

Such an inverted tree is simply mentioned as a tree in the rest of the thesis.
Definition 2.4 All the $\imath$-level ( $0 \leq \imath \leq d$ ) predecossors of an attiactor constitute the corresponding attractor basin, where $d$ is the depth of the tree rooted at the attiactor The basin with a state $\alpha$ as attractor is referred to as $\alpha$-basin (Figure 2.7).

If $l$ is the smallest integer for which $T^{d+l}=T^{d}$, for $d>0$, then the CA is a non-group CA with depth $d$ and cycle length factors of $l$.


Figure 26: A 4 cell null boundary CA with rule $\langle 102,60,90,204\rangle$

Example 2.1 The state transition diagıam of a hon-group CA (Fugure 20) having rule vector $\langle 102,60,90,204\rangle$ with periodic houndary is shown in Frgure 2 7. The


Figure 2.7: State transition diagram of non-group CA with rule $<102,60,90,204>$
characteristic matrix $T$, characteristic polynomial $p(x)$, depth, graveyard state (attractor) and attractor basins are illustrated below.
$T=\left[\begin{array}{llll}1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1\end{array}\right] \begin{array}{ll}\text { Characteristic poly. } & : p(x)=\operatorname{det}(T+I x)=x^{3}(x+ \\ \text { Depth } & : 3 \\ \text { Attractors } & : 0 \text { and } 3 \\ 0 \text {-basin } & :\{0,2,4,6,8,10,12,14\} \\ \text { 3-basin } & :\{1,3,5,7,9,11,13,15\}\end{array}$
Some of the results related to non-group CA's, are restated from [Das90b] below without any proof.

Theorem 2.7 If for a largest value $d, x^{d}$ divides the minimal polynomial $f(x)$ of the $T$ matrix of a CA, then the depth of its state transition graph is $d$.

Theorem 2.8 If a state is reachable from $p$ predecessors for a CA, then only $1 / p$ of the total states are reachable.

Theorem 2.9 The number of predccossors of a state in the statc transition graph is $2^{n-r}$, where $r$ is the rank of the $T$ matrix of the $n$ cell CA.

Theorem 2.10 If for a CA of depth $d>0, l$ is the smallest integer for which $T^{d+l}=T^{d}$, thon the CA state transition graph has cycles of lengths which arc factors of $l$.

Theorem 2.11 In an $n$-ccll non-complemented $C A$ with charactoristic matıix $T$, mum-
ber of graveyard states is $2^{n-r}$ whene $r$ is the rank of the $[T+I]$ matrix Any graveyard state can be ıepresented as a linear combination of $n-1$ lineally independent state vectors.

In the next subsection, a special class of non-group CAs, referied to as Multiplc Attiactor CA (MACA), where all the cycles are of unit-length, has been discussed. Some important properties of this class of CAs are also cited. This class of CAs has been used to realize efficient hashing function.

### 2.2.1 Properties of Multiple Attractor CA (MACA)

The state transition diagram of a MACA is shown in Fugure 2.7. It is a non-group $\mathrm{C} \Lambda$ with the following properties:

- each of its reachable states has two predecessors; and
- it has a set of cyclic states, each cycle of unit length;
that is, each cyclic state is a graveyard state (also referred to as an attractor).
The structure of the state transition diagram of a MACA consists of a subset of states leading to an attractor, in an inverted tree-like fashion. That is, if the CA is leaded with any state in the tree, after a few cycles (equal to the depth of the tree) the CA will evolve to the attractor state. Each such set of states along with its attractor is called a basin (Definitıon 2.4). Thus, the complete set of CA states are divided into a number of basins, and each basin is built around a specific attractor. One of the athactors is always 0 -state (all 0 's binary bit) and its corresponding basin is known as the 0 -basin. Any other basin with non zero attractor (say with decimal value 2 ) is referred to as a 2-basin. In Fıgure 2.7, statcs (in decimal notation) 0, 2, 4, 6, 8, 10, 12 and 14 belong to the 0 -basin, while the states in the 3 -basin arc $1,3,5,7,9,11,13,15$. The states are distributed at different levels of a basin. If the CA is loaded with a $j^{\text {th }}$ level $(\jmath>0)$ state on the $i^{\text {th }}$ basin, the CA will evolve to state 2 after $\rho$ number of cycles The $0^{t h}$ Ievel state is the attractor itself with self-loop and so it needs one cycle to reach to itself. 'The icsults'reported below from [Nandi94a, Palch97] characterize some important propertics of MACAs.

Lemma 2.2 The sum of two parent states of any state is the non zero predecessor of the 0 -state.

Theorem 2.12 The sum of two states lying at different levels $p$ and $q(p>q)$ of the $\imath$ basin is a state at level $p$ of the 0 -basin.

Lemma 2.3 There exists a one to one correspondence between the statcs of the 0-basin and $\imath$-basin of a MACA.

Lemma 2.4 In a depth MACA, if the level wise transitions from a non-reachable state to its attractor are known, the states in the 0-basin can be enumerated level-wise.

Lemima 2.5 In a depth $n$ bit MACA, if (i) the level wise transitions of a non-rcachable state to its attractor, and (ii) ( $n-d$ ) lineanly independent attractors anc known, then states belonging to all the basins can be enumerated level-wise.

Lemma 2.6 In a d depth $(d>1) M A C A$, the sum of all states in any basin is zero.

Lemma 2.7 No of attractors in the complemented MACA is same as that in the original linear one.

Lemma 2.8 The complemented CA dẹived from multiple attractor linear CA can not have cycles of length greater than unity.

An important advantage of 3-neighbourhood CA is its programmability features, which have been found to be useful in many applications such as cryptography, pscudorandom pattern generation, test pattern generation etc. One of the major advantages of CA is that it can be programmed with minimum logic structure. The main objective of a Programmable CA (PCA) is to configure the CA with different rules at different instants of time. An application of a variant of such PCA (based on rule 90 \& rule 150) can be found in [Nandi94a]. As from the positional representation of rule 90 and sule 150 , it is evident that they are neighbourhood dependent, differ by only one position, namely viz. on the cell itself. Therefore, by allowing a single control line per cell (Frgure 2.8), one can apply both rule 90 and rule 150 on the same cell at different time steps. Thenely, an $n$ cell $\mathrm{C} \Lambda$ structure can be used for implementing $2^{n} \mathrm{C} \Lambda$ conlignations. Realizing different CA configurations on the same structure cau be achicved by using a control logic to control the appropriate switches; a control program, stoted in a ROM,
can be employed to activate the switches. The $1(0)$ state of the $\imath^{t h}$ bit of a ROM word closes (opens) the switch that controls the $2^{\text {th }}$ cell. Frgune 28 shows a PCA with simple control structure- allowing one control input per cell that configures the CA cell, cither to rule 90 or rule 150 . For example, the control word $<0110>$ for a four coll PCA lcads to the fact that the 1st and 4th cells are configured with rule 90 , while the 2nd and 3rd cells are configured with rule 150 .


Figure 2.8: A 3-cell Programmable CA structure and a PCA cell

Using such a structure for all the cells, all possible additive non-complemented rule combinations can be achieved to realize any hybrid additive CA [Nandi94a]. Such an $n$ cell PCA can implement $2^{3^{n}}$ number of different CA configurations. A 3-neighbourhood PCA cell with provision of both complemented and non-complemented rules is shown in Figure 2.9. This is the structure of the most general PCA cell with 4 control lines per cell.


Figure 2.9: A PCA cell with all possible additive rules

### 2.3 Characterization of Extended Neighbourhood CA (ENCA)

In this section, a general class of CA (based on $n$-neighbourhood interconnections) is investigated. The characterizations of this class of CAs are basically extensions of the group and non-group 3-neighbourhood additive CAs, discussed in the previous sections. If the ENCA is non-singular and with a repeated application of the CA in a finite set of elements, if the entire set of states ultimately converge to a single or multiple cycles, it is referred to as a group ENCA; otherwise, it is called non-group ENCA. Both these categories of ENCAs have some important propertics, which can be successfully utilised in the field of cryptography, pseudo-random pattern generation, hashing etc. In the next section, characterization of these CAs, in general, has been given.

### 2.3.1 General Characterization

Consider any finite set of elements, $V=\left\{\alpha_{0}, \alpha_{1}, \alpha_{2}, \cdots, \alpha_{w}\right\}$ which is closed with resipect to an associated operator $T$ (i.e.an ENCA). In a crude analogy with construction of a 'power' sub-group of a multiplicative group, one can generate a sequence, say, $\alpha_{0}=$ $a_{0}, \alpha_{1}=\alpha_{0}+a_{0}, \alpha_{2}=\alpha_{1}+a_{0}, \cdots, \alpha_{r+1}=\alpha_{r}+a_{0}, \cdots$. Since the set $V$ is finite and as the sequence is gradually built, at some stage, i.e. say, for some $\gamma \leq w$, the ordered subsct $V_{1}:\left\{\alpha_{0}, \alpha_{1}, \cdots, \alpha_{\gamma-1}\right\}$ has all elements distinct but $\alpha_{\gamma}=\alpha_{\gamma-1}+a_{0} \in V_{1}$ and from then onwards, the sequence $\alpha_{0}, \alpha_{1}, \cdots, \alpha_{\gamma-1}, \alpha_{\gamma}$ will start repcating itself, though not necessarily from the beginning; suppose, $\alpha_{\gamma}=\alpha_{a 1+1}$, where $a 1<w$ and hence, the sequence will be $\alpha_{0}, \alpha_{1}, \cdots, \alpha_{a 1}, \alpha_{a 1+1}, \cdots, \alpha_{a 1+p}, \alpha_{a 1+p+1}=\alpha_{a 1}, \cdots$, with an aper zodzczty ' $a 1$ ' and (ultimate) perıodıcıty ' $p$ ', i.e. $a 1+p=w$.

However, if $\gamma<w$, the set $V$ has elements not included in the subset $V_{1}$. Stanting with another element say, $a_{2} \notin V_{1}$, one can build another sequence $\alpha_{21}, \alpha_{22}, \cdots \notin V_{1}$ until one of these elements repeats itself with an ultimate periodicity say, ' $p_{2}$ ' and aperiodicity ' $a_{2}$ ' or, some $\alpha_{\beta} \in V_{1}$, in which case the sequence or stream 'merges' into the calicr stream $V_{1}$. In Figure 2.10, an illustration is given

Thus, in gencral, an ENCA generates trajectories, starting from some element, (one can call these elements as non-reachable or startang states, which have no predecessors


Figure 2.10: Basin structure showing 'aperiodic' behaviour
but, are different starting points and ending in possibly more than one cycles (lengths of cycle may even be one only, i.e. attractor)). In other words, an Extended-Neighbourhood CA (ENCA) partitions the elements of the 'operand set' into patially ordeted sets (POSET), referred as basins, where the structure of each basin is characterized by the type of CA chosen. These basin-structures exhibit some peculiar characteristics which can be of use in many different contexts. Some of the results found from the analysis of the various types of ENCA based basin structures, have been reported next.

Example 2.2 Consider the characteristic matrix

$$
T=\left[\begin{array}{lllll}
1 & 0 & 1 & 1 & 0 \\
0 & 1 & 1 & 0 & 1 \\
1 & 1 & 1 & 0 & 1 \\
0 & 0 & 1 & 1 & 1 \\
1 & 0 & 1 & 0 & 1
\end{array}\right]
$$

It is seen that $T^{3}=I$ (i e. identity matrix) and the characteristic equation is $x^{5}=x^{4}+x^{3}+x^{2}+x+1 ; x^{6}=1$, i.e. $T^{6}=I$; Hence, $T^{2} \cup T^{3} \cup T^{6}=I$, i.e. lengths of cycles either may be 2 or 3 or 6 ; It is verified that $T^{2} \neq I$ but $T^{3}=I$. It follows that there can be cycles of length 3 only. Also, since $T$ is non-singular, cvery state has only one parent (possibly itself). Hence, in the basin structure induced by this CA- there can be either 'attractors' or cycles of length three only; every state is cither its own parent or it is a member of a 3 -cycle. To obtain all the attiactors of $T$, one has only to find the solutions of $(T+I) \Delta=0$, (where $\Delta$ is a boolean variable). The only possible solutions arc $(\Delta 0 \Delta \Delta \Delta)^{\prime}$. Thus, thete anc only 2 attactors, viz 0 itself and 23 The other 30 states in the space are partitioned into $10(=30 \div 3)$ cycles as follows.

$$
\{1,5,14\},\{2,18,7\},\{3,29,9\},\{4,31,27\} \cdots
$$

For illustration, see Figure 2.11.


Figure 2.11: State transition diagram of non-maximum length group ENCA

If the characteristic polynomial of group ENCA is primitive, then it cxhibits properties analogous to the 3-neighbourhood additive, maximum-length CAs [Nandi94a]. Such an ENCA of size $n$ gencrates all the $2^{n-1}$ states in successive cycles, excluding the all-zero state. One such CA with the maximum-length cycle is illustratcd in Example 2:3.

Example 2.3 Consider the characteristic matrix

$$
T=\left[\begin{array}{lllll}
1 & 1 & 0 & 1 & 1 \\
0 & 1 & 1 & 1 & 1 \\
0 & 1 & 0 & 1 & 0 \\
1 & 0 & 0 & 1 & 1 \\
1 & 1 & 0 & 1 & 0
\end{array}\right]
$$

From the matrix $T$, it can be found that it is of non-singular type and the characteristic equation is : $x^{5}+x^{4}+x^{2}+x+1=0$; This has $x=1$, not as a root and it docs not possess any attractor other than 0 . Also, we have $x^{31}=I$. So, this CA gives rise to a fully periodic basin (maximum-length cycle) of all 31 non-zero statc, as shown in Frgure 2.12.


Figure 2.12: State transition diagram of maximun-length group ENCA

### 2.3.2 Properties of Group ENCA

Some of the properties of 3-neighbourhood additive CAs from [Palch97, Nandi94a]) derived with matrix algebraic tool were tried with ENCAs and similar results were obtained. The findings of such investigations are reported next. However, the proofs of lemmas and theorems are not reported here, because they are analogous to those reported in the Section 2.2 of the present chapter.

Theorem 2.13 An ENCA is group $C A$, if and only if the determinant $\operatorname{det} T=1$, wherc $T$ is the characteristic matrix for the CA.

Theorem 2.14 A group ENCA has cycle-lengths of $m$ or factors of $m$ with a non-zero starting state iff $\operatorname{det}\left[T^{m} \oplus I\right]=0$.

Lemma 2.9 If the order ( $O_{P}$ ) of a group ENCA characterized by $T$ is a non-prime number, then the cycle-lengths are equal to its factors only.

Theorem 2.15 If the characteristic polynomial of a group ENCA is primitive it generates a maximum-length cycle.

Non-group ENCAs form a special class of CAs, in which some of the states are not reachable from any state. In contrast to the group ENCA, (i) in the state transition graph of such CA, the reachable states can have multiple predecessors, and (ii) the characteristic matrix is singular in nature. The study of non-group CA behviour has not reccived sufficient attention for long time. Next section presents some of the interesting properties of this class of CAs. In Examples 2.4 B 2.5, an analysis of the basin structure due to a 5 -cell non-group ENCA, has been given. From state transition graph, it can be found that the cyclic states are lying on one or more cycles. Other states form inverted trees rooted at one of the cyclic states. Such inverted trees are reforred here as simply trees. The 'cycles' in the state transition diagram of a non-group ENCA are referred as attractor. Thus an attractor is a cycle of length $l(l \geq 1)$. The tree rooted at a 'cyclic-state' $\alpha$, is denoted as ' $\alpha$-basin'. The depth of such a basin is defined to be the minimum number of 'clock-cycles' [Palch97] required to reach the ncarest cyclic state from any non-reachable state in the state-transition graph.

### 2.3.3 Properties of Non-Group ENCAs

This subsection presents some fundamental results characterizing a special class of nongroup ENCA (analogous with the TPMA 3-neighbourhood CA of [Palch97]). For the sake of clearness about the behaviour of such ENCAs, the following examples have been cited.

Example 2.4 Consider the CA

$$
T=\left[\begin{array}{lllll}
1 & 1 & 0 & 1 & 0 \\
1 & 0 & 1 & 1 & 1 \\
1 & 0 & 1 & 0 & 1 \\
0 & 1 & 1 & 0 & 1 \\
0 & 0 & 1 & 1 & 1
\end{array}\right]
$$

Thus, we have the characteristic equation as : $x^{5}+x^{4}+x^{3}=0$ and here, $x^{6}=x^{3}$. Hence, $T^{6}=T^{3}$. Thus, for any state $S$, one has $T^{6} . S=T^{3} . S$ and any sequence $\left\{S_{n} \mid S_{n}=T . S_{n-1}\right\}$, will have at most only 5 distinct states, the sixth state $S_{6}$ in the sequence being identical with $S_{3}$. The sequence is ultimately periodic with periodicity either 3 or a factor of 3 . Of course, since 3 is prime, the ultimate periodicity is cither 1 or 3 only. Again, since, $x^{5}+x^{4}+x^{3}=0$, the only eigen valuc admissible is $x=0$. Solving the equation $T . S=0$, we have $T[00101]^{t}=T .5=0$ as the only solution, other than 0 , of $T . S=0$. Also, $T . S=b$ has no solution if $b_{1}+b_{2}+b_{4}=1$, i.c. there are $2^{2} \cdot\left(\binom{3}{1}+\binom{3}{3}\right)=16$ states got by choosing components $b_{1}, b_{2}$ and $b_{4}$ such that only one of them or all these are ' 1 ', the elements $b_{3}$ and $b_{4}$ being aubitrarily ' 0 ' or ' 1 ', which can not be reached from any other state. These only can be the non-reachable states of a trajectory. Since, $T .5=0$, we have $T .(S+5)=T . S$, only for all ' $S$ '. Hence, if $S$ has $T . S=b$, then $T .(S+5)=b$ also, i.e. for any state in the trajectory other than a starting state, there will be two parents, which differ by the state 5 . Thus, for instance, since $T .28=1$ we have $T .(28+5=25)=1$ als. .

Also, since all the columns of $T$ have now been used as a parent, with its progeny obtained, one can compute $T^{2}, T^{3}, \cdots$ by simple table look-up. The structure and contents of the table is as shown in Table 2.1. Again, from the characteristic equation i.c. $x^{5}+x^{4}+x^{3}=0$, as it can be observed that $x=1$ is not a root, there is no ' $S$ ' such that $T . S=S$. Also, we have $T^{6}=T^{3}$, thus the periodicity is $(6-3)=3$. So, cycles of length 3 can exist as the terminal points of the trajectorics.

Table 2.1: CA and Its Power Sequences

| Operators | Corresponding Sequences |
| ---: | ---: |
| $T$ | $28,18,15,25,15$ |
| $T^{2}$ | $1,5,11,1,11$ |
| $T^{3}$ | $15,0,4,15,4$ |
| $T^{4}$ | $11,0,15,11,15$ |
| $T^{5}$ | $4,0,11,4,11$ |
| $T^{6}$ | $15,0,4,15,4$ |




Figure 2.13: Basin structure generated by non-group ENCA

Since, each offsprong shall have only two parents, i.e. $T . S=b$, if at all solvable, has only two solutions, and since each element in a cycle necessarily has one parent in the cycle, there should be another parent to it, which is not in the cycle. If the parent is itself not a starting state, it should have exactly two parents, etc. Further, from $T^{3}=(15,0,4,15,4)$, we find, for $\left(T^{3}+I\right)$ that- there are exactly four 'eigen values' of $T^{3}$, including the trivial 0 state. Hence, there is only one cycle of length 3 (for illustration, see Figure 2.13).

Example 2.5 Consider the CA

$$
T=\left[\begin{array}{llllll}
0 & 1 & 1 & 0 & 1 & 0 \\
1 & 0 & 1 & 1 & 0 & 0 \\
1 & 0 & 0 & 1 & 1 & 1 \\
1 & 0 & 1 & 0 & 0 & 1 \\
1 & 1 & 0 & 0 & 1 & 1 \\
1 & 1 & 1 & 1 & 0 & 0
\end{array}\right]
$$

Thus, we have the characteristic equation as : $x^{6}-x^{5}-x^{2}=0$; from this characteristic equation it is obvious that the CA is singular and $x=1$ is not a root.Hence, there is no non-trivial eigen vectors with $x=1$. Also, we have -
$x^{6}=x^{5}+x^{2} ;$
$x^{7}=x^{5}+x^{3}+x^{2} ;$
$x^{8}=x^{5}+x^{4}+x^{3}+x^{2} ;$
$x^{9}=x^{4}+x^{3}+x^{2}$;
$x^{11}=x^{4}+x^{2}$;
$x^{13}=x^{5}+x^{4}+x^{2}$;
$x^{14}=x^{3}+x^{2} ; x^{17}=x^{2} ;$

Since, $x^{17}=x^{2}$, we have, aperioducity $a=2$ and perioducity $p=15$. Hence, one can have cycles only of lengths ( $1 \cup 3 \cup 5 \cup 15$ ). From the derived power sequences, we have : $T^{3}=(14,45,14,22,0,51) ; T^{5}=(51,30,51,35,0,22)$; and $T . S=0$ has only one solution : $S=42$. It provides the only cycle of length 1 . Also, for the starting state, $\beta_{1}+\beta_{4}^{\dot{\prime}}+\beta_{5}=1$. Hence, there are 32 non-reachable states. Thus, in this basin of 64 states, 32 are non-reachable states; since, each offspring has cxactly two parents (one of them possibly, itself) which differ by the value $\mathbf{4 2}$, the 32 starting states can be paired
off with 16 pairs, each pair giving rise to one reachable state. There is a cycle of length 15 and each state on the cycle is having one predecessor in the cycle and hence must have one parent not in the cycle; these have to be from among the 16 offsprings from the starting states. Hence, the 15 elements in the cycle and their non-cycle parents, again 15 in number, and their two parents each of which is a starting state, account for 60 of the states in the space. This leaves a set of 4 valucs: 2 starting states, their one offspring and its offspring which should also be its own parent (viz. the zero state) which constitute a tree like structure. Since 42 is the only non-trivial solutions of $T . S=0$, each offspring has exactly two parents, the state difference between them being 42. Also, since $T^{3}+I$ and $T^{5}+I$ are non-singular (in fact they are permutation matrices), they can not be cycles of length 3 or 5 . Hence, $T^{15}=(8,16,8,6,0,43)$ and $T^{15}+I$ is of rank 2. Hence, there are $2^{4}=16$ stales which are such that $T^{15} . S=S$; this set, of coursc includes the zero state. The other 15 states constitute a cycle, of length 15 .

The followiug lemmas and theorems have been found to be valid for this special class of uon-group ENCAs :

Theorem 2.16 The number of predecessors of a rcachable state and those of the state 0 in a non-group ENCA are equal.

Lemma 2.10 If $d$ is the dimension of the null space of the characteristic matrix of a mon-group ENCA, then the total number of predecessors of the all zero states (i.e. 0 -state) is $2^{d}$.

Lemma 2.11 If a state is reachable from ' $k$ ' predecessors for an ENCA, then only $1 / k$ of the total states are reachable.

Lemma 2.12 If an $n$-cell non-group ENCA with characteristic matrix $T$, the number of attractors is $2^{n-r}$, where ' $r$ ' is the rank of the ( $T \oplus I$ ) matrix.

Lemma 2.13 The numbor of $l$ predecessors $(l>0)$ of any cyclic state is the same as that 0-statc.

Lemma 2.14 The number of states at level ' $l$ ' ( $l>0$ ) of a tree rooted at a cyclic state is the same as the number of states at level ' $l$ ' of the tree rooted at 0 -state.

Lemma 2.15 The 'depth' of a tree rooted at any cyclic state camot be more than that rooted at the 0 -state.

Theorem 2.17 Let 'd' be the largest integer $\geq 0$ such that $x^{d}$ divides $m(x)$ (the minimal polynomial of the ENCA). Thon, each of the cyclic states in the state transition graph is the root of a trice of depth 'd' aud the structure of each tree is isomorphic to that of the tree rooted at the 0-state.

Lemma 2.16 The sum of two parent states of any state is a non-zero predecessor of the 0 -state.

Theorem 2.18 The sum of two states lying at diffcrent levels ' $p$ ' and ' $q$ ' (wherc, $p>q$ ) of the $2^{\text {ch }}$ tree is a state at level ' $p$ ' of the 0 -tree.

Lemma 2.17 For an n-cell d-depth non-group ENCA with characteristic polynomial $x^{d}(x+1)^{n-d}$ and minimal polynomial $x^{d}(x+1)$ -

- the number of attractors is $2^{n-d}$,
- the number of states in each attractor-tree is same and equal to $2^{d}$.

Theorem 2.19 In an $n$-cell d-depth non-group ENCA with $2^{m}$ attractors, there exist m-bit positions at which the attractors give $p$ seudo-exhaustive $2^{n}$ bit-patterns.

### 2.4 Conclusion

The theory of 3-ncighbourhood additive CAs based on matrix algebra has been re- . ported in this chapter. We have further extended characterization of $n$-neighbourhood or extended-ncighbourhood CA i.c. ENCA based on matrix algebraic tools. The various group aud non-group properties of JNCAs have been repoted. In the subsequent chapters (chapters $3,4 \mathcal{O}$ ), applications are developed by utilizing properties of these 3 -ncighbourhood and ENCAs.

## Chapter 3

## One-Way Hash Function Design Using Cellular Automata

### 3.1 Introduction

In the previous chapter, the theory of group and non-group 3-neighbourhood Cellular Automata(CA) has been addressed The regular, modular and cascadable structure of those additive CAs has becu successfully exploited as a tool in several application arcas, such as cryptography, error correction/detection, pseudo-random pattern generation, test pattern generation etc. Application of CA in other areas has also been explosed. One such area is the one-way hash function design.

One-way hash functions play a fundamental role in moden cryptography. For the pupose of authentication of transmission of confidential data in insecure network, oneway hash function has an important rolc. They are used as building blocks in many protocols. Most of the one-way hash functions $H(M)$ s operate on an arbitrary-length message, $M$ and generates a fixed-length information, $h$, known as 'hash value'. Two common propesties in these hash-functions are: finstly, it is irreversible in nature and secondly, it is hatd to find another message $M^{\prime}$, such that $H(M)=H\left(M^{\prime}\right)$. Onc-way hash function hers several applications, such as: public key cryptography, distributed database security, network security etc. It has becn found that most of the onc-way hashing schenes operate with $2 r$-bil input and $r$-bit output, where, the input to the
function is the block of text and the hash of the previous block of text. That is, hash of a block $M_{i}$ is, $h_{i}=\left(M_{i}, h_{i-1}\right)$, where $h_{i-1}$ is the hash of the previous block used on feedback mode. The hash of the last block becomes the hash of the entire message.

In this chapter, a new one-way hashing scheme for message authentication purpose has been designed by utilizing mainly, the features of non-group, non-linear, Multiple Attractor-based 3 -neighbourhood CA. The scheme can be found to be significant in comparison to the other existing schemes [Merk190, Rivst92, NIST93, Schnr96], in view of the following facts:

1: A CA whose rule vector can be modified dynamically is referred to a PCA (Programmable Cellular Automata) (see Chapter 2, Section 2). Such a PCA based hardwired implementation of the hash function provides better flexibility of configuring different CAs from the same structure.

2: Due to the simple, regular, modular and cascadable structure of CA, the implementation of this scheme becomes attractive and it can be operated at higher speed due to the local inter-connection.

3: It provides better security against different types of attacks because, besides using a general one-way hashing strategy analogous to the other existing ones, it also incorporates features of non-group, non-linear CAs.

There are several applications of one-way hash functions, such as distributed database security, network security, public key cryptography, authonticated key exchange etc. With the enormous growth of information technology, another major application of oneway functions is Ecash or Electronic economy. Utilization of the proposed scheme has been shown in the context of such an ecash application. In the next subsection, a brief review of the existing one-way hashing schemes has been reported.

### 3.1.1 Reviewing the existing schemes

A definitive reference for the cryptographic hash function and its detail survey can be found in [Precn94]. Davis and Price [Davis83] also provides a solid treatment of message authentication and data integrity. Simmons independently developed a general theory [Simon92] of unconditionally secure message anthentication schemes and the
subject of authentication codes. Rabin [Rabin78] first suggested employing a one-way hash function in conjunction with a one-time signature scheme and later in a public key signature scheme. Merkle [Merk190] further explored uses of one-way hash functions for authentication, including the idea of tree authentication for both one-time signatures and authontication of public files. The DES-based hash-function of Merkle [Merk190] which employs a compression function $f$ mapping 119-bit imput to 112-bit output in 2 DES operations, allows 7 -bit message blocks to be processed (at the rate of 0.055 ). An optimized version was also introduced, which maps 234 -bits to 128 -bits in 6 DES operations and it processes 106-bit message-blocks (at the rate of 0.276). MD4 and MD5 were designed by Rivest [Schnr96, Menez97]. An Australian extension of MD5, known as HAVAL has also been proposed by Zheng, et al. [Zheng93]. The first published partial attack on MD4 was by den Boer and Bosselaers [Menez97] who demonstrated that collisions could be found when Round 1 (of the three) was omitted from the compression function, and confirmed unpublished work of Merkle showing that collision could be found (for ioput pairs differing in only 3-bits) in under a millisecond on a personal computer, if Round 3 was omitted. Another devastating attack on the full MD4, was due to Vaudenay [Vaude95], which provided only near-collisions, but allowed sets of inputs to be found for which, of the corresponding four 32 -bit words, threc are constants while the remaining word takes on all possible 32-bit values. Later, in 1995, Dobbertin [Dobbr96] brokc MD4 by finding collisions for meaningful messages (in one hour, requiring 20 free bytes at the start of the messages). RIPEMD [Schnr96] was designed in 1992 by den Boer and others. However, carly in 1995, Dobbertin [Menez97] demonstrated that if the first or last (parallel) round of the 3 -round RIPEMD compress function is omitted, collisions can be found in $2^{31}$ compress function computations. This result coupled with concern about inherent limitations of 128-bit hash results motivated RIPEMD-160 by Dobbertin, Bosselaer and Preneel [Dobbr96]. NIST, along with the NSA, designed the Secure Hash Algorithm (SHA) for use with the Digital Signature Standard [NIST93]. SHA produces 160 -bit hash, longer than MD5. The SHA is called secure, because it is designed to be computationally infeasible to recover a message corresponding to a given message digest, or to find two different messages which produce the same digest. Besides. these, several other hash functions have also evolved during the past decade, such as [Dmgrd90, Daernn93a, Daemn93b, Schno91, Schno93]. However, as found in [Schnr96], most of these hashing schemes consume huge time and resource complexitics, as a result of which their hardware implementation has become costly as well as complicated.

In this backeromed, utilizing the regular, morlular, gascadablo and non-linear features
of 3-neighbourhood additive CAs, a novel one-way hashing scheme has been designed. The mathomatical foundation of the proposed scheme is provided by the Lemmas 2.1, 2.2, 2.3, 2.4, $2.5 \mathcal{B} 2.6$ and Theorems 2.1, 2.2, 2.3, $2.4 \mathcal{E} 2.6$ as found in Chapter 2. The next section describes the design of the proposed scheme.

### 3.2. CA based Hashing Scheme : CHA

The proposed hashing scheme is designed based on the properties of 3-neighbourhood additive group and non-group CAs. The scheme operates block-wise and it hashes arbitrary length messages into fixed $r$-bit hash value. Firstly, the input message is broken into $r$-bit chunks, to make exact multiple of $r$-bit blocks, 0 's are padded at the end of the message. Four $r$-bit variables are initialized. Then the main loop of the algorithm begins. The loop continues for as many iterations as there are $r$-bit blocks in the message.

The hashing process is mainly performed in two major phases : in Phase I, for cach original source block, an intermediate cipher-block is built, through a sequence of thrce opcrations; in Phase II, using the intermediate ciphertext-block along with the previous hash value, MACA based hashing is performed and a corresponding hash value is generated. These two steps for each block continue until all the blocks finish. The final hash value becomes the hash of the entire message.

## Phase I : Intermediate Cipher Block Building

For each $r$-bit block of message $b_{2}$, which is further divided into four sub- blocks, each of $r / 4$-bit length - the inner loop begins for four rounds. Each round consists of three operations - bit-wise substitution of $r / 4$-bit sub-block using a BS (Bit Substitution) table of size $r / 4$, XORing with a set of $r$-bit constants ( $\delta_{i}$ 's) (dynamically changed for each message during run-time) and finally enciphering each $r$-bit block using a PCA based Block Cipher. In the following sub-sections, each of these operations are discussed.

## Bit-wise Substitution

In this phase, each of the input $r / 4$-bit sub-blocks is bit-wise substituted according
to a substitution table. Duing substitution, the table is scanned from left to right, top t.o bottom and each bit position in the input sub-block is substituted using the corresponding bit values from the table. An important property which is trivial for this operation is peesented next.

Lemma 3.1 : Let $\alpha_{\imath}$ and $\beta_{\imath}$ be two $r / 4$-bit plaintext messages then, $\operatorname{BS}\left(\alpha_{\imath}\right)=\operatorname{BS}\left(\beta_{\imath}\right)$, only if, $\alpha_{\imath}=\beta_{\imath}$ and wherc BS is the Bit-wise substitution.

An example BS table is shown in Table 3.1 for ( $r / 4=64$ ). According to this table, bit-1 of the input block is permuted to bit-43, bit- 17 is permuted to bit-32. The major advantage of this permutation is that its hardwined implementation is trivial and it imptoves the overall complexity of the proposed scheme. The substituted sub-block is concatenated with the rest of the three sub-blocks, to obtain $\beta^{\prime}$. The next step of operation is initiated with $\beta^{\prime}$ as the input.

Table 3.1: Bit-wise Substitution Table

| 43 | 23 | 55 | 34 | 26 | 18 | 10 | 53 | 60 | 52 | 44 | 36 | 28 | 20 | 12 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 32 | 54 | 46 | 38 | 30 | 22 | 14 | 6 | 64 | 56 | 48 | 40 | 62 | 24 | 16 | 8 |
| 57 | 49 | 41 | 33 | 25 | 17 | 9 | 1 | 59 | 51 | 58 | 35 | 27 | 19 | 11 | 3 |
| 61 | 2 | 45 | 37 | 29 | 21 | 13 | 5 | 63 | 42 | 47 | 39 | 31 | 50 | 15 | 7 |

## XORing With Constants

A set of four $r$-bit constants are chosen for each plaintext message. In this phase, during each round of operation, these four initialized constants are XORed with the block, $\beta^{\prime}$ casc-wise as follows:
switch(round) $\left\{/^{*}\right.$ 'round' is initialized with 1 and incremented with each cycle upto $4^{*}$ /
case 1: $\beta^{\prime \prime}=\beta^{\prime} \oplus \delta_{1}$;
case 2: $\beta^{\prime \prime}=\beta^{\prime} \oplus \delta_{2}$;
casc 3: $\beta^{\prime \prime}=\beta^{\prime} \oplus \delta_{3}$; $\operatorname{casc} 4: \beta^{\prime \prime}=\beta^{\prime} \oplus \delta_{4} ;$ \}

The following important property is trivial from the above XORing operation -
Lemma 3.2 Let $\alpha_{i}{ }^{\prime}$ and $\beta_{i}{ }^{\prime}$ be two $r$-bits plaintext message blocks then, $\alpha_{i}{ }^{\prime} \oplus \delta_{i}=\beta_{i}{ }^{\prime} \oplus \delta_{i}$, only if, $\alpha_{i}{ }^{\prime}=\beta_{i}{ }^{\prime}$, where, $\delta_{i}$ is a distinct $r$-bit constant.

The XORed output i.e. $\beta^{\prime \prime}$ is subjected to the next phase of operation i.e. enciphering using a Block cipher.

## Enciphering Using PCA based Block Cipher

Each intermediate block, $\beta^{\prime \prime}$ ( $r$-bit) is enciphered using one of the enciphering functions, $E$, where, $E \in k_{2}{ }^{8}$, the space of enciphering functions with the exponential order of cardinality, a considerably large number [Palch97]. The enciphered block, $\beta^{\prime \prime \prime}$ is yielded by acting $E$ on $\beta^{\prime \prime}$, i.e. $\beta^{\prime \prime \prime}=E\left(\beta^{\prime \prime}\right)$. The enciphering function consists of $q$ fundamental transformations and each of the transformations is derived from different CA rules. By permutation of $q$ fundamental transformations, a total of ( $q!$ ) enciphering functions can be generated. For example, let $E=a b c d$, with $q=4$, where

$$
a=\pi_{1}{ }^{4}, b=\pi_{2}{ }^{4}, c=\pi_{3}{ }^{4}, d=\pi_{4}{ }^{4} ;
$$

and $\pi_{i}{ }^{8}=I ; i=1,2,3,4$; implying that $a, \dot{b}, c, d$ are involutions and $\pi$ 's are CA representation of various permutations. An important result of this enciphering is reported next.

Lemm'a 3.3 Assume $\alpha_{i}^{\prime \prime}$ and $\beta_{i}^{\prime \prime}$ be two $r$-bit plaintext message blocks, then $E\left(\alpha_{i}{ }^{\prime \prime}\right)=$ $E\left(\beta_{i}{ }^{\prime \prime}\right)$; only if $\alpha_{i}{ }^{\prime \prime}=\beta_{i}{ }^{\prime \prime}$ and $E\left(\alpha_{i}{ }^{\prime \prime}\right)$ represents the enciphering function acted on $\alpha_{i}{ }^{\prime \prime}$ and $\alpha_{i}{ }^{\prime \prime}=\left(B S\left(\alpha_{i}{ }^{\prime}\right)+\delta_{i}\right)$.

The proof of the above lemma can be easily established from the 'non-maximum length' group CA properties found in ' [Nandi94a]. By rotating left the sub-blocks of $\beta^{\prime \prime \prime}$ - above three operations are repeated for four rounds. Finally, the resultant block, $\beta^{\prime \prime \prime}$ is concatenated with the previous hash value, $h_{i-1}(r$-bit) and then iniput to the final phase of hashing.

## Phase II : Hashing Using Complemented MACA

The structure of the MACA (as described in Chapter 2, Section 2) should be selected in such a way that it generates enough number of basins(trees), each rooted on an attractor. From the properties of MACA, it can be found that if the characteristic matrix of
a $k$-cell MACA is $T$, and $\operatorname{rank}\left(T \oplus S_{c}\right)=r$, then the number of attractor states is $2^{k-r}$. Bascd on some propertics observed in complemented MACA (Lemmas 2.78 2.8) the following property of MACA is derived.

Lemma 3.4 In an $k$-cell complemented MACA with $2^{m}$ attractors, there exists m-bit positions at which the attiactors give pseudo-exhaustive $2^{m}$ patterns.

Pıoof: Let $T$ be the characteristic matrix corresponding to an $k$-ccll MACA, $C A_{1}$ with $2^{m}$ altractors. As per lemmas $2.7 \& 2.8$, noted above- the corresponding complemented MACA, $C A_{1}{ }^{\prime}$ derived from $C A_{1}$ has same number of attractors (cycles of length unity). Since, $C A_{1}^{\prime}$ has $2^{\text {nn }}$ attractors, we have

$$
\operatorname{rank}(T \oplus I)=(k-m) ;
$$

whoce, $I$ is the $(k \times k)$ identity matrix. The attractors of $C A_{1}{ }^{\prime}$ will be governed by $m$-dimensional null space of $(T \oplus I)$. Hence, there exists $m$ linearly independent basis vectors, i.e. all possible combination of these basis vectors will be present in the mull space. Hencc, of $C \Lambda_{1}{ }^{\prime},(T \oplus I)$ moduces pscudo-cxhaustive bit patterns at m-bit positions.

In this phase, the proposed scheme uses a $2 r$ bit Complemented MACA which induces $2^{r}$ number of basins, where each of them is rooted at an attractor (characterized by Pseudo-Exhaustive $m$-bit positions). During hashing, each block of intermediate enciphered message concatenated with the previous hash value and is loaded as a seed to the $2 r$-bit non-group complemented MACA and it is allowed to run autonomously for a number of cycles equal to the depth to reach the attractor ( $2 r$-bit). The PscudoExhaustive $r$-bits of the attractor ane then separated out as the present hash valuc, $h_{2}$.

The whole process (phase I and II) repeats for the remaining set of blocks. The final hash value $h_{n}$ is the hash of the entire message.

### 3.2.1 The Algorithm CHA

CHA uses the following variables.

| $n$ | $:$ | total number of $r$-bit message blocks (after padding ); |
| :---: | :---: | :---: |
| $h_{2}$ | $:$ | $i^{\text {th }}$ hash values; |
| $\beta_{2}, \beta_{2}{ }^{\prime}, \beta_{2}{ }^{\prime \prime}, \beta_{2}{ }^{\prime \prime \prime}$ | $:$ | variables to hold intermediate values; |
| $\eta_{1}, \eta_{2}, \eta_{3}, \eta_{4}$ | $:$ | variables to hold the $(r / 4)$ bits sub-blocks; |
| $\delta_{1}, \delta_{2}, \delta_{3}, \delta_{4}$ | $:$ | $r$-bit constants; |
| $M_{2}$ | $:$ | $2 r$-bit message input |
| $\xi_{2}$ | $:$ | $\imath^{\text {th }} 2 r$-bit attractor; |
| $Y_{1}, Y_{2}$ | $:$ | temporary variables to hold $r / 2$-bit blocks; |
| $P C A$ | $:$ | $r$-bit null boundary hybrid CA; |
| $M A C A^{\prime}$ | $:$ | the Complemented $2 r$-Cell MACA; |
| $B S$ | $:$ | Bit-wise Substitution table of size $r / 4$-bit. |

Input: Plaintext message sticam divided into ' $n$ ' blocks (each of $r$-bit);
Output: $r$-bit hash value;
Step 1: Initialise $r$-bit constants: $\delta_{1}, \delta_{2}, \delta_{3} \& \delta_{4}$;
Step 2: $\quad \imath \leftarrow 1 ; h_{\imath-1} \leftarrow 0$;
Step 3: Read $r$-bit block $b_{2}$; decompose it into four sub-blocks $\left(\eta_{1}, \eta_{2}, \eta_{3}, \eta_{4}\right)$ of length ( $r / 4$ ) bits;
Step 4: $\quad j \leftarrow 1$;
Step 5: Rcad right-most sub-block $\eta_{1}$ of $b_{2}$ and substitute it with the corresponding bit-pattern using the BS table; Concatenate the modified sub-block $\eta_{1}{ }^{\prime}$ with the rest other sub-block: ( $\eta_{l}{ }^{\prime} \mathrm{s}$ ) in the same order to obtain the $r$-bit block $\beta_{i}{ }^{\prime}$;
Step 6: Perform XOR operation between the pair $\left(\beta_{\imath}{ }^{\prime}, \delta_{j}\right)$ to obtain $\beta_{\imath}{ }^{\prime \prime}$;
Step 7: Encipher $\beta_{2}{ }^{\prime \prime}$ using a PCA-based block-cipher to obtain block, $\beta_{2}{ }^{\prime \prime \prime}$;
Step 8: Rotate left $\beta_{2}^{\prime \prime \prime}$ by ( $r / 4$ )-bits;
Step 9: $\quad j \leftarrow \jmath+1$; If $j \leq 4$ goto stcp 5;
Step 10: Perfom the following operations to prepare input for the $2 r$-bit $M A C A^{\prime}$ :

$$
\begin{aligned}
& Y_{1} \leftarrow \operatorname{left}(r / 2) \text { bits of } \beta_{2}^{\prime \prime \prime} ; \\
& Y_{2} \leftarrow \operatorname{rgght}(r / 2) \text { bits of } \beta_{\imath}^{\prime \prime \prime} ; \\
& M \leftarrow \operatorname{concat}\left(Y_{1}, h_{\imath-1}, Y_{2}\right) ;
\end{aligned}
$$

Step 11: Load $M A C A^{\prime}$ with $M$ and iun upto the depth level to obtain attractor, $\xi_{i}$;
Step 12: Extract the PE $(r)$-bits from $\xi_{2}$ and store in $h_{t}$;
Step 13: $\quad i \leftarrow \imath+1$; If $\imath \leq n$ then goto step 3 ;
Step 14: Return $h_{n}$ as the final hash value.

The following block diagram (sce Frgure 3.1) shows the datapaths in the CHA algorithon. This diagram is basically repiesenting the hashing process for a single block of message. The controller logic is not shown in the Figure 3.1.


Figure 3.1: Logic diagram of the CHA (for a single block)
For an $r$-bit message, the proposed scheme generates a unique $r$-bit message digest or hash value. This uniqueness can be proved trivially based on the lemmas 3.1, 3.2, 3.3 B 3.4 and hence, the following property can be derived.

Theorem 3.1: For any $r$-bit encrypted message block, conctenated with the previous $r$-bits hash value $h_{\imath-1}$ (i.e.'r' PE-bits), as per Lemmas 3.1, 3.2, $3.3 \& 3.4$, the corresponding $r$-bit signature is unique.

### 3.3 Invulnerability of the proposed scheme

The sccurity of the schemc against the two possible types of attacks is described below :
A. Hash-Value only Attacks : For example, if $r=128$, for a cryptanalyst it is essential to study 16 characters (each character made of 8 bits) frequency distribution tablewhich is of size $\left(2^{8}\right)^{16}=2^{128}$, i.e. an enormous quantity. Hence, the scheme is guarded against cryptanalysts' hash-value only attack.
B. Known 8 Chosen (Message, Hash-Value) Pair Attacks: In the case of known plaintext attack, the intruder is assumed to possess a considerable amount of messages
and corresponding hash values. While in case of chosen plaintext attack, the intruder is able to acquire an arbitrary number of messages and the corresponding hash value pairs $(M, h)$ of his own choice.

In the proposed scheme, as per Lemmas 3.1, 3.2, $3.3 \& 3.4$, it can be found that cach Phase and Step (within a phase) are independent to the others. Hence, the cracking complexity for the whole scheme will be the multiplication of the individual complexities offered by each of them. Next, we compute the complexitics duc to each of these steps, phase-wise :

- for an $r$-bit message, the bit-wise substitution offers complexity of the order of $O(2 r / 4)$;
- for XORing with $r$-bit constants, the complexity will be $O\left(2^{r}\right)$;
- In case of the PCA-based block ciphering, as it is based on the application of Alternating Group, which offers- in general, the complexity of the order of $\left(2^{r}!\right) / 2$. However, the proposed block enciphering operation basically uses a subset of this alternating group (i.e. the affine group). So, the actual complexity will be less than it, i.e. may be of the order of $O\left(2^{r-1}\right.$ ! $)$.

In Phase I, these three operations repeat for four times. Thus, the order of complexity due to first phase will be, approximately:

$$
2^{2} \times\left(2^{r / 4}\right) \times\left(2^{r}\right) \times\left(2^{r-1}!\right) \approx\left(2^{2 r}\right)
$$

Similarly, for the second phase,

- since, the MACA is basically a 3 -neighbourhood additive CA, it uses $(6 r-2)$ variables (i.e. the threc major diagonals of the non-group CA). Thus, there will be basically $2^{6 r-2}$ possible useful matrices among the whole set of $2^{r^{2}}$ matriccs. From experimental study, it has been found that - for $r=16$, and for 10100 random sample matrices of size $(32 \times 32)$, the number of MACAs is 2789 , which is approximately, $(1 / 5)^{t / h}$ of the total sampled matrices taken.Thus, it can be assumed that- the possible number of MACAs can be more than $2^{1 r}$ and hence, it will offer complexity approximately of the order of $\left(2^{1 r}\right)$.
- again, as the chosen MACA is complemented, due to the complement vector of say, size $r$, the complexity for this step will be $O\left(2^{r}\right)$.

So, Phase II will offer complexity of the order of :

$$
\left(2^{1 r}\right) \times\left(2^{r}\right) \approx\left(2^{5 r}\right) ;
$$

Hence, total complexity due to Phase I and Phase II will be, approximately :

$$
\left(2^{5 r}\right) \times\left(2^{2 r}\right) \approx\left(2^{7 r}\right) ;
$$

In the precceding section, the proposed one-way hashing scheme has been established and its security against all the possible attacks has also been reported. To justify the usefulness of the scheme, the next section discusses a potential application of the proposed scheme.

### 3.4 Application of the proposed scheme

In the present day world, one of the major applications of the one-way hashing scheme for message anthentication is clectronic cconomy or censh, where a vaticty of cryptographic techniques are being used to minimise threats to electronic transactions. Ecash is an electronic payment system developed by the Digicash Co. of Amstcrdam [Panur96]. It is currently bcing implemented by the Mark Twain Bank of Missouri in the U.S. In this payment system, to undertake transactions, both buyers and sellers must have deposits in the concerned implementor Bank's World Currency Access accounts. Access accounts are conventional checking accounts insured by an Insurance corporation, without paying interest or having a fixed maturity period.

As per the instruction of the Buyers, the Bank transfers funds from their World Currency Access accounts into their accounts' Ecash. Mint. Funds in the mint are no longer deposits in the Bank, and they are not insured. The mint acts as a personal bulfer account. At any time buyers can order their computers to remotely interface with the mint and withdraw funds from the mint into the hard drives on their personal computer. The format of the funds is digitized- and it is cryptographically secure and unique.

To solve the security problems in Electronic Cash Transfer System, basically, four mechanisms are used, such as privacy, authentication, integrity and scalability. In many cases, it has been observed that- more than one kind of these problerns are mitigated by using a single mechanism [Baldu97]. Privacy includes the desire to keep documents and communication secrets, as well as to hide the very existence of certain kinds of information
and to protect the identities of the parties communicating. Authentication and integrity refer to the need to confirm the identity of user, the authenticity of messages, and the integrity of messages or connections. Scalability mechanisms like distribution centers and digital certificates, are other crucial aspects to the success of electronic commerce systems. For, they help in creating systems that involve millions of users, transactions and documents. Among these various possible threats, authentication problems are serious, and so, special care is essential for designing the authentication scheme particularly from the message authentication point of view.

The most basic form of authentication is validating the identity of system users. One mechanism that oflers substantially better user authentication is a credit-card-sized authentication device- a token or smartcard- that can store a secret key and perform a cryptographic challenge response. To access the system, the user must have the authentication token as well ạs a password. Once the users have been authenticated, the next problem is authenticating the individual messages. An electronic fund transfer system has to know that its instructions come from the expected source and have not been modified by an attacker. The core mechanism for achieving this kind of authentication is called a one-way digest. Cryptographic digests are one-way in the sense that it is easy to compute them, but computationally infeasible to find a message that has a given digest, that is computing the function is easier than computing its inverse. In this regard, the proposed CHA fulfills all these criteria. Tempering of any message will be easily detected with very high confidence in the proposed scheme. Any attacker cannot modify a message without changing the digest. Due to high exponential order of complexity, it is hardly possible for the intruder to compute the message, if the corresponding digest is given. Also, by combining one-way-digests and public-keys, one can achieve better results in authentication and integrity. By using public keys with the one-way digest, a digital signature is created, which is attached to the clectronic messages or other business documonts. The senders can sign a message by computing the digest and then encrypting it with their private keys. The receiver verifies that the message came from the specified receiver by decrypting the digest using the senders' public key and comparing that value with the digest he computed for the message. In Figure 3.2, this process is illustrated. If an intruder modifies the message, the digest will not match. If an at, tacker tries to modify the message and its encrypted digest, that too will fail, bacause the attacker does not know senders' private keys. In the following block dingram (see Figure 3.2), the role of CHA has been shown in the electronic economy.


Figure 3.2: Scnder's signing and receiver's verification process

### 3.5 Conclusions

In this chapter, a new scheme for message authentication purposes has been introduced. The scheme is based upon the propertics of $r$-bit group and $2 r$-bit non-group, non-linear CAs, which have been utilised to generate unique $r$-bit hash valucs. It has been established that a particular class of non-group CA (referred to as MACA) can serve as an cfficient hashing function gencrator. The schemes also utilise Bit-wise permutation as well as PCA based block enciphering mechanisms- which make the schemes more significant from security point of view. The scheme offers an exponential order of cracking complexity and thus, protects it from all possible types of attacks. The complexity of the scheme can be further improved with an increase in block size.Another major advantage of this scheme is the use of simple, regular, modular and cascadable structure of CA as the basic building block that ideally suits for VLSI implementation.

In the next chapter Chapter 4, an application of $n$-neighbourhood CA in the context of an enciphering scheme design has been discussed.

CHAPTER 3. ONE-WAY HASH FUNCTION USING CA

## Chapter 4

## Design of $\mathbb{E N C A}$ based Cipher System

### 4.1 Introduction

In the previous chapter, it has been established that CA can be used as a useful tool for efficient one-way hash function design. This chapter explores the possibility of application of the extended neighbourhood CA (ENCA) in the area of cryptographic system design. Cryptography has become an essential requirement for ensuring communication privacy or concealment of data in a data bank. The process by which an unprotected message, i.c. the plaintext is transformed into ciphertext (or cryptogram) of an unintelligible form is called encryption or encipherment. Encryption may be achicved by constructing two different types of ciphers : stream and block cipher. In a stream cipher, the message is broken into successive bits or characters and then the string of characters is encrypted using a key stream. On the other hand, a block cipher is one in which a message is broken into successive blocks and then encrypted using single or multiple keys. Two most commonly desired characteristics of such cryptosystems are : (3) good measure of strength, and (22) case of implementation. However, a class of block-ciphers arising in computer privacy have been studied in [Denni82, Reupl90, Welsh88, Sebry89, Schnr96, Menez97]; it reveals that most of them have two common drawbacks: use of a large key, or need of a much langer ciphertext than the plaintext [Schmr96]. It also appears that the time and icsouce complexitics of the existing schemes are significantly large, which make the hardware implementation more complicated. This chapter introduces the design of two simple CA-based cipher systems based upon the group propertics of ENCA. The next
subsection presents a brief survey on the existing block ciphering schemes.

### 4.1.1 Reviewing the existing schemes

In the early days, a transposition cipher was used to rearrange characters according to some specified scheme [Melln73]. A simple substitution cipher replaced each character of an ordercd plaintext alphabet [Sinko66]. In those days messages were also encoded in musical symbols [Sam79]. A common method was a simple substitution of individual notes for letters. A homophonic substitution cipher maps each character of the plaintcxt alphabet into a sct of ciphertext elements called homophones. Hammer [Palch97] has shown that it is possible to construct a high order homophonic cipher such that any intercepted ciphertext will decipher into more than one meaningful message under diflerent keys. The development of Poly alphabetic ciphers began with Leon Battista Alberti, the father of western cryptography [Kahn67]. Most polyalphabetic ciphers are periodic substitution ciphers based on a period. A popular form of the periodic substitution cipher based on shifted alphabets is the Vigenere Cipher [Kahn67]. All the preceding substitution ciphers encipher a single letter of plaintext at a time. By enciphering larger blocks of letters, polygram substitution cipher makes cryptanalysis harder by destroying the significance of single-letter frequencies. The Playfair cipher is a diagram substitution cipher named after the English scientist Lyon Playfair; the cipher was actually invented in 1854 by Playfair's friend, Charles Wheatstone, and was used by the British during World War I [Kahn67].

A product cipher is the composition of a set of functions (ciphers), where each function may be a substitution or a transposition. Shannon [Shann49] proposed composing different kinds of functions to create "mixing transformation", which randomly distribute the meaningful messages uniformly over the set of all possible ciphertext messages The LUCIFER cipher, designed at IBM by Feistel [Feist73], uses a transformation that alten nately applies substitutions and transposition. In 1977 the National Burcau of Standards (USA) announced a data encryption standand (DES) to be used in unclassificd US Govt applications [DES67]. The encryption algorithm was developed at IBM and was the outgrowth of LUCIFER [Palch97]

In 1978, Pohling and Hellman [Pohln78] published an encryption.scheme based on computing exponentials over a finte field At about the same time, Rivest, Shamir
and Adleman [Rivst76] published a similar scheme, but with a slight modification that gave the MIT group a method for realizing public-key encryption as put forth by Diffie and Hellman [Diffi76a]. In 1979, Shamir [Shamr79] studied the feasibility of constructing a Knapsack system for both secrecy and authentication. Merkle and Hellman [Merkl79] proposed a scheme whose security depends on the difficulty of solving the 0-1 Knapsack problem. They show how to convert a simple Knapsack into a trapdoor Knapsack that is hard to solve without additional information. Following them, several new enciphering schemes have been proposed in [Denni82, Reupl86, Welsh88, Sebry89, Schnr96, Menez97, Palch97]. The present block cipher systems are also particular cases of these schemes. The proposed schemes can be found to be attractive and significant in view of the following facts:

1: The security of the schemes is mainly based on the CA (i.e. the binary matrices) used. As the CAs are not easily characterizable and as the size of the matrix spaces tremendously increases with the increase in size of the CAs, the measure of strength against intrusion can be found to be at least comparable to, if not better than the existing schemes.

2: Encipherment and decipherment proceed with the similar protocols.
3 : Due to the simplified logic structure, the scheme can be implemented with minimum hardware.

The next Section presents the design of the proposed ENCA based cipher system.

### 4.2 Design of the Cipher System

The proposed enciphering scheme is designed by utilizing the periodicity propertics exhibited by the group ENCAs. The Theorems 2.13, $2.14 \& 2.15$ and Lemma 2.9 basically provide the mathematical foundation of the scheme.

A group ENCA $T$ of size $s$ and a complenent vector $S_{c}$, of same size are selected, which generates say, $p$ number of cycles, i.c. $B_{1}, B_{2}, \cdots, B_{p}$. In the state transition diagram of the cycle-structure, every state with a repeated multiplication of $T$ and exclusive ORing with $S_{c}$, ultimately ends up in one of $p$ different cycles. These cycle-struct.m:
induced by $T$ and $S_{c}$ can be utilized for encryption of any binary file having not more than $p$ distinct $r$-bit blocks. During encryption, for cach distinct $r$-bit block, a unique cycle is identified and is mapped to any element taken at random (with equal chance, for example) from this cycle. The decryption process also uses the same CAs. By a repeated application of $T$ and $S_{c}$ on the ciphertext blocks, one will get the smallest element in the cycle, which is uniquely associated with a plaintext block and hence decrypted.

## Algorithm Encrypt I;

Input to the algorithm is a plaintext message stream $b_{1} b_{2} \cdots b_{n}$, where each $b_{i}$ refers to a $r$-bit block in the plaintext language. Let there be $p$ distinct blocks in the language, where, $p \leq 2^{r}$.

Define an operator matrix $T$ of size $s \times s(s>r)$ and a complement vector $S_{c}$ of size $s$; by a repeated application of the operators (i.e. $T$ and $S_{c}$ ) will generate at least $p$ cycles of equal or various length.

Input: Plaintext message stream $b_{1} b_{2} \cdots b_{n}$, where there are ' $p$ ' distinct possible $b_{i} s$. Outplit: Ciphertext stream $c_{1} c_{2} \cdots c_{n}$, where each $c_{i}$ is an $s$-bit vector.

Step 1: $\quad i=1$;
Step 2: Read $r$-bit message block $b_{i}$;
Select the corresponding cycle uniquely associated with $b_{i}$;
Choose an element ' $m$ ' at' random from the set of elements of the corresponding cycle and substitute $c_{i}$.
$c_{i} \leftarrow m$;
Step 3: $\quad i \leftarrow i+1$;
if $i \leq n$ goto Step 1 ;
Step 4 : Stop execution.

## Algorithm Decrypt I

We will have a table of length ' $p$ ', where entries of the table are the least elcment $(x)$ of cycle and the corresponding $b_{i}$.

Input: The ciphertext $c_{1} c_{2} \cdots c_{n}$.

Output: The deciphered text $a_{1} a_{2} \cdots a_{n}$
Step 1: $\quad \imath=1$;
Apply $T$ and $S_{c}$ on $c_{\imath}$ repeatedly until it will form a loop;
Sclect the least element $x$ among those generated by the above process.
Step 2: Assign the corresponding entry from the table to $a_{2}$;
Step 3 :' $\quad \imath \leftarrow i+1$;
if $\imath \leq n$ goto Step 1 ;
Step 4: Stop execution.
The Encrypt I and Decrypt I procedures are illustrated in the Example 4.1. b
Example 4.1 Consider the CA $T$ and the Complement Vector $S_{c}$ as below

$$
T=\left[\begin{array}{lllllll}
0 & 1 & 1 & 1 & 0 & 1 & 1 \\
0 & 0 & 0 & 1 & 1 & 1 & 0 \\
1 & 0 & 0 & 0 & 1 & 1 & 1 \\
0 & 1 & 0 & 0 & 1 & 1 & 0 \\
0 & 0 & 0 & 1 & 1 & 0 & 1 \\
1 & 1 & 0 & 0 & 1 & 0 & 1 \\
1 & 0 & 1 & 1 & 1 & 0 & 0
\end{array}\right], \quad S_{c}=\left[\begin{array}{c}
0 \\
1 \\
1 \\
1 \\
1 \\
0 \\
0
\end{array}\right]
$$

The CA and the complement vector are of size $s=7$ and has 15 cycles as listed below: Since $T$ is non-singular, it will generate fully periodic cycle structure, where cycles are represented by the numbers $1,2,3,6,8,9, \cdots$ ctc. which are the smallest in the corresponding cycles.

$$
\begin{aligned}
& B_{1}=\{1,106,120,65,121,23,108,63,67,1, \ldots\} \\
& B_{2}=\{2,68,16,125,40,19,83,64,47,2, \ldots\} ; \\
& B_{3}=\{3,18,5,85,7,45,122,57,4,3, \ldots\} ; \\
& B_{4}=\{6,123,111,17,43,61,59,124,126,6, \ldots\} ; \\
& B_{5}=\{8,89,93,98,29,113,114,92,52,8, \ldots\} ; \\
& B_{6}=\{9,15,72,74,50,79,91,37,31,9, \ldots\} ; \\
& B_{7}=\{10,33,32,118,99,75,100,90,115,10, \ldots\} ; \\
& B_{8}=\{11,119,53,94,76,117,77,35,88,11, \ldots\} ; \\
& B_{9}=\{12,102,34,14,30,95,26,96,101,12, \ldots\} \\
& B_{10}=\{13,48,55,38,49,97,51,25,78,13, \ldots\}
\end{aligned}
$$

$B_{11}=\{20,66,87,127,80,110,71,62,21,20, \ldots\} ;$
$B_{12}=\{22,58,42,107,46,84,81,56,82,22, \ldots\} ;$
$B_{13}=\{27,54,112,36,73,28,39,103,116,27, \ldots\} ;$
$B_{14}=\{24\} ; B_{15}=\{0\} ;$
The cycle $B_{1}$, for instance stands for the cycle $1 \rightarrow 106 \rightarrow .120 \rightarrow \cdots$ i.e. $T \cdot 1 \oplus S_{c}=106, T \cdot 106 \oplus S_{c}=120, \cdots$ where $1,106,120,65, \cdots$ are integers representing the valucs $(000001),(1101010) \cdots$ etc. Let us consider that the plaintext language consists of 12 unique $r$-bit blocks (e.g. $\delta_{1}, \delta_{2}, \cdots \delta_{12}$ ). Now, as the cycles from $B_{14}$ onwards have only cycles of length 1 and as according to the proposed scherne, this plaintext will require only 12 cycles, so, $B_{13}, B_{14}$ and $B_{15}$ are not used here. The mapping of the blocks to their corresponding cycles is as given in the Table 4.1. Let an example

Table 4.1: Mapping $r$-bit block to corresponding cycle

| Block | Basin | Representative | Petiod |
| :---: | :---: | :---: | :---: |
| $\delta_{1}$ | $B_{8}$ | 11 | 9 |
| $\delta_{2}$ | $B_{4}$ | 6 | 9 |
| $\delta_{3}$ | $B_{2}$ | 2 | 9 |
| $\delta_{1}$ | $B_{9}$ | 12 | 9 |
| $\delta_{5}$ | $B_{1}$ | 1 | 9 |
| $\delta_{6}$ | $B_{11}$ | 20 | 9 |
| $\delta_{7}$ | $B_{12}$ | 22 | 9 |
| $\delta_{8}$ | $B_{7}$ | 10 | 9 |
| $\delta_{9}$ | $B_{10}$ | 13 | 9 |
| $\delta_{10}$ | $B_{3}$ | 3 | 9 |
| $\delta_{11}$ | $B_{5}$ | 8 | 9 |
| $\delta_{12}$ | $B_{6}$ | 9 | 9 |

sequence of plaintext blocks be : $\delta_{3} \delta_{4} \delta_{4} \delta_{2} \delta_{5} \cdots$.
The cycle ieprescntatives are: $B_{2}(2) B_{9}(12) \mathcal{B}_{9}(12) B_{4}(6) B_{1}(1) \cdots$.
For instance, $\delta_{3}$ is associated with cycle $B_{2}$ which is iepiesented by the 6 -bit pattern for the number 2 , Hence, encryption for $\delta_{3}$ is $T^{q}$. (2) $\oplus S_{c}$, where $q$ is random over $0 \cdots 8$. Thus, if $q=4, \delta_{3} \rightarrow 40$. Similarly, for the second and thind characters, $\delta_{4} \rightarrow T^{q 1}$.(12) $\oplus S_{c}$ and $\delta_{4} \rightarrow T^{q^{2}}(12) \oplus S_{c}$ iespectively; if $q 1=4$ and $q 2=2$, the same plaintext block $\delta_{4}$ will be mapped to 30 and 34 respectively. Thus, the encrypted message may be $40,30,34,111,23, \cdots$ ctc.

For decryption, one starts with 40, which is not a representative i.e. smallest in any cycle as seen from Table 41 . Hence, it is repeatedly multiplied by $T$ and exclusiveORed with $S_{c}$ giving the scquence $-40,19,83,64,47,2,68,16,125$ and back to 40 , the smallest element being 2 , which is the representative of cycle $B_{2}$ and hence, for message block $\delta_{3}$ of plaintext The next encrypted block value is 30 which is again not in the list of representatives and hence, is also operated repeatedly by $T$ and $S_{c}$ giving the sequence $30,95,26,96,101,12,102,34,14$ and back to 30 . The smallest number in this sequence being 12 , (representing $B_{9}$ ) it stands for $\delta_{4}$ of the plaintext. The third cucrypted block is leading to the cycle $34,14,30, \cdots, 12,102$ and back to 34 and hence leading to again plaintext block $\delta_{4}$ and so on. Thus, for instance, the same plaintext block $\delta_{4}$ is mapped sometimes to 30 and sometimes to 34 , but is still recoverable as cycle $B_{9}$, and hence, block $\delta_{4}$, by using the same keys i.e. $T$ and $S_{c}$.

With this scheme, one disadvantage is that- presently, the sets of cycle elements are totally disjoint or mutually exclusive and as a result, among the plaintext and the ciphertext blocks - only a one-to-many mapping becomes possible. But, to achieve poifect security in a cryptosystem, a necessary condition is that there must exist many-to-many relationships among the plaintext and ciphertext messages [Shann49]. In two ways, this limitation could be overcome:

- by use of a binary matrix transformation and
- by use of a bit-permutation table.

In the next, both these mechanisms have been described as additional processing steps to the aforesaid scheme, which lead to two different block enciphering schemes. Due to these additional steps, in each of the schemes, the cycle elcments are overlapped in a random manner, and as a result, it becomes possible for the same block to map into the different blocks at the same time and hence, the same input block can map to different cycles also.

## [A] Binary Matrix Transformation Scheme :

A permutation $\pi$ of a finite set $V$ can be defined to be an injection, $\pi: V \rightarrow V$, where, $V=\left\{u_{1}, u_{2}, \cdots, u_{d}\right\}$. The set of all possible permutations on $V$ basically form a non-commutative group $G_{d}$ of order ( $d^{\prime}$ ) under the operation of permutation multiplica-
tion. One distinct feature of permutation is its cyclic structure, i.e. for any permutation $\pi$ in $V$, one can have $\pi\left(z_{j}\right)=z_{j+1}$, where, $j=1,2, \cdots(l-1)$ for a cycle $\left(z_{1}, z_{2}, \cdots z_{l}\right)$ of length $l$. It has been established that every permutation can be uniquely expressed as a product of disjoint cycles. By a transposition, it is meant a cycle of length two. An even permutation is one that is expressible as a product of an even number of transpositions; otherwise a permutation is called an odd permutation. It is a well known result that all even permutation on $V$ form a normal subgroup $G_{d}$, which is the alternating group, say $A_{d}$ of degree $d$ and order $(d!) / 2$.

Now, considering a CA, say $T_{1}$, which through a repeated application upon the elements of a finite set, say, $F$ over GF(2), ultimately ends in one of ' $p$ ' different cycles. Now, every permutation can be uniquely expressed as a product of these ' $p$ ' disjoint cycles. Let us now consider an ' $r$ '-dimensional vector space $V_{r}$, which consists of all the message blocks, each of ' $r$ '-bits long. According to this modified scheme (which operates in two steps), each ' $r$ '-bits message block ' $b_{i}$ ' is subjected to a permutation operation in the finst step, to gencrate the intermediate block ' $\bar{b}_{2}$ ', which is finally substituted using the ENCA based block cipher (i.e. Encrypt I) to ultimately generate the final cipher-block $c_{i}$. Now, let $\Upsilon$ be an enciphering function and $b_{i} \in V_{r}$ be a $r$-bit message block to be encrypted. Here, $\Upsilon \in V_{2^{r}}$, the space of enciphering function with cardinality $\left(2^{r}!\right)$. Thus, according to this scheme, the encrypted message block will be : $\bar{b}_{i} \leftarrow \Upsilon\left(b_{i}\right)$. Basically, each of these functions i.e. $\Upsilon$ consists of ' $g$ ' fundamental transformations [Naudi94a] and by using permutation among ' $g$ ' transformations, one can have ( $g$ !) permutation fuuctions. For the sake of clarity, let us take an example, say $\Upsilon=k_{1} k_{2} k_{3} k_{4}$, where -

$$
k_{1}=\pi_{1}^{y} ; k_{2}=\pi_{2}^{y} ; k_{3}=\pi_{3}^{y} ; k_{4}=\pi_{4}^{y}
$$

here, $\pi_{1} ; \pi_{2}, \pi_{3}$ and $\pi_{1}$ are permutation representation of four disjoint cycles of say, length $l$, induced by a group ENCA and ' $y$ ' represents the 'cycle-length'. Now, according to the scheme, the intermediate cipher-block is obtained by applying $\Upsilon$ on each of the plaintext blocks, i.c.

$$
\overline{b_{2}}=\Upsilon\left(b_{r}\right)=\left(k_{1} k_{2} k_{3} k_{4}\right)\left(b_{2}\right)
$$

Similarly, during deciphering, the inverse permutation will be applied :

$$
b_{i}=\Upsilon^{-1}\left(\overline{b_{i}}\right)=\left(k_{1} k_{2} k_{3} k_{4}\right)^{-1}\left(\bar{b}_{i}\right)=k_{k_{4}}^{-1} k_{3}^{-1} k_{2}^{-1} k_{1}^{-1}\left(\bar{b}_{i}\right)=\left(k_{4} k_{3} k_{2} k_{1}\right)\left(\bar{b}_{i}\right)
$$

Thus, in the deciphering process, the fundamental transformations are applied just in the 'reverse order on the intermediate block ${ }^{\prime} \overline{b_{i}}$ '. Here, $y<r$ and $\pi^{r}{ }_{i}=I, i=1,2,3,4$ and $k_{i}$ are involutions. The above logic is illustrated in Example 4.2:

Example 4.2 For clear understanding of the permutation operation, consider the following two permutation functions, $\pi_{1}$ and $\pi_{2}$ representing two disjoint cyclic structures, gencrated by a CA, say $T$ of size '4':

$$
\pi_{1}:\left[\begin{array}{cccccccc}
0 & 5 & 6 & 7 & 8 & 13 & 14 & 15 \\
15 & 0 & 5 & 6 & 7 & 8 & 13 & 14
\end{array}\right], \quad \pi_{2}:\left[\begin{array}{cccccccc}
1 & 2 & 3 & 4 & 9 & 11 & 12 & 10 \\
12 & 9 & 10 & 3 & 4 & 2 & 11 & 1
\end{array}\right]
$$

Now, $\pi_{1}{ }^{3}(0)=15 ; \pi_{1}{ }^{6}(14)=0 ;$ Similarly, $\pi_{2}{ }^{4}(3)=11 ; \pi_{2}{ }^{5}(9)=12$;
Now, consider that an example sequence of plaintext blocks be : $\delta_{9} \delta_{6} \delta_{2} \delta_{12} \delta_{9} \cdots$.
During enciphering, for instance, $\delta_{9}$ is associated with table $P_{1}$ (here, each table $P_{j}$ corresponds to a permutation, say $\pi_{3}$ in implementation) and after bit-substitution it becomes $P_{1}\left(\delta_{9}\right) \rightarrow \delta_{3}$. Similarly, for the second and the third blocks i.e. $\delta_{6}$ and $\delta_{2}$, let it be $P_{2}\left(\delta_{6}\right) \rightarrow \delta_{4}$ and $P_{3}\left(\delta_{2}\right) \rightarrow \delta_{4}$ respectively. Again, for the fifth block i.e. $\delta_{9}$, let the corresponding table be $P_{j}$, where $j=0 \cdots q$. After substitution, let it becomes $P_{j}\left(\delta_{9}\right) \rightarrow \delta_{5}$. Thus, the substituted sequence of blocks will be : $\delta_{3} \delta_{4} \delta_{4} \delta_{2} \delta_{5} \cdots$.

Similarly, for the inverse substitution, each substituted block is picked up and subjected for inverse substitution. For instance, $\delta_{3}$ is taken and substituted with table $\overline{P_{1}}$, which will result $-\overline{P_{1}}\left(\delta_{3}\right) \rightarrow \delta_{9}$. Similarly, for the second and the third blocks i.e. $\delta_{4}$ and $\delta_{4}$, it will be $\overline{P_{2}}\left(\delta_{4}\right) \rightarrow \delta_{6}$ and $\overline{P_{3}}\left(\delta_{4}\right) \rightarrow \delta_{2}$ respectively. Similarly, for the remaining other blocks also, the corresponding inverse tables will be applied and finally, one can casily obtain the original plaintext block sequences.

## [B] Bit-Permutation Scheme :

This scheme uses a set of bit-wise permutation tables: $P_{1}, P_{2}, \cdots P_{q}$, (analogous to that found in DES [DES67], where ' $q$ ' is the cardinality of the set. During encryption, each ' $r$ '-bit plaintext block $b_{i}$ is associated with a Permutation table say, $P_{j}$ and operated by it to obtain the substituted $r$-bit block $\overline{b_{i}}$, which is finally used as an input to the previous encryption algorithm i.e. Encrypt I). Similarly, for deciphering also, it uses a sct of corresponding Inverse Permutation tables: $\overline{P_{1}}, \overline{P_{2}}, \cdots \overline{P_{q}}$. The first step in the deciphering is analogous to the previous decryption algorithm (i.e. Decrypt I); it identifies the smallest element in the cycle associated with the ciphertext block $c_{2}$ and then through a simple table lookup, identifies the corresponding intermediate cipher-block,
i.e. $\overline{b_{i}}$. In the second step, the corresponding inverse permutation table is applied on $\overline{b_{1}}$ to obtain the original plaintext block $b_{i}$.

To illustrate the above procedure, the Example 4.3 is cited.
Example 4.3 Let us take some simple Brt-Permutation and its corresponding Inverse permutaition tables, such as:
$P_{1}=\left[\begin{array}{lll}3 & 241\end{array}\right] ; \overline{P_{1}}=[4213] ;$
$P_{2}=\left[\begin{array}{llll}4 & 2 & 1 & 3\end{array}\right] ; \overline{P_{2}}=\left[\begin{array}{llll}3 & 2 & 3 & 1\end{array}\right] ;$
$P_{3}=\left[\begin{array}{lll}2 & 1 & 4\end{array}\right] ; \overline{P_{3}}=\left[\begin{array}{ll}2 & 1\end{array}\right.$ 3 $]$;

Now, consider that an example sequence of plaintext blocks be : $\delta_{9} \delta_{6} \delta_{2} \delta_{12} \delta_{9} \cdots$. During enciphering, for instance, $\delta_{9}$ is associated with table $P_{1}$ and let after bitsubstitution it becomes $P_{1}\left(\delta_{9}\right) \rightarrow \delta_{3}$. Similarly, for the second and the third blocks i.e. $\delta_{6}$ and $\delta_{2}$, let it be $P_{2}\left(\delta_{6}\right) \rightarrow \delta_{4}$ and $P_{3}\left(\delta_{2}\right) \rightarrow \delta_{4}$ respectively. Again, for the fifth block i.e. $\delta_{9}$, let the corresponding table be $P_{j}$, where $j=0 \cdots \kappa$. After substitution, let it becomes $P_{3}\left(\delta_{9}\right) \rightarrow \delta_{5}$. Thus, the intermediate sequence of input blocks may be : $\delta_{3} \delta_{4} \delta_{4} \delta_{2} \delta_{5} \cdots$.

Similarly, for the reverse permutation, each permuted block is picked up and subjected for inverse permutation. For instance, $\delta_{3}$ is taken and substituted with table $\overline{P_{1}}$, which will result $-\overline{P_{1}}\left(\delta_{3}\right) \rightarrow \delta_{9}$. Similarly, for the second and the third blocks i.e. two consecutive $\delta_{4} \mathrm{~s}$, it will be $\overline{P_{2}}\left(\delta_{4}\right) \rightarrow \delta_{6}$ and $\overline{P_{3}}\left(\delta_{4}\right) \rightarrow \delta_{2}$ respectively. Similarly, for the remaining other blocks also, the corresponding inverse tables will be applied and finally, one can casily obtain the original plaintext block sequences.

From such bit-substitution, one can easily observe that the different blocks are sometimes mapped into the same block and also the same block is mapped into different blocks. So, basically it establishes a many-to-many mapping. By increasing the size of the permutation table, one can have more varieties in mapping among the blocks.

The algorithms Encrypt II and Decrypt II presented below are cnhanced versions of the previous algorithıns i.e. Encrypt I and Decrypt $I$. For encryption, Encrypt II uses a set of permutation tables: $P_{1}, P_{2}, \cdots P_{\kappa}$, (' $\kappa$ ' is the cardinality of the set) induced by any of the scheme reported so far (i.e. either binary-matrix transformation or, bit-
permutation), where each table is uniquely associated with any of the distinct ' $r$ '-bit plaintext block $b_{i}$. Similarly, Decrypt $I I$ also uses a set of corresponding inverse tables, i.e. $\overline{P_{1}}, \overline{P_{2}}, \cdots \overline{P_{\kappa}}$ (due to the corresponding scheme), where each of them is uniquely associated with any of the intermediate cipher-block. Encrypt $I I$ operates on each of the plaintext block $b_{i}$ and substitutes it with the permutation table, say $P_{j}$ (where $j=1,2, \cdots \kappa$ ) to obtain intermediate cipher-block, $\overline{b_{i}}$. The next step of encryption is analogous to Encrypt $I$. Similarly, the first step of Decrypt $I I$ is analogous to the previous decryption algorithm (i.e. Decrypt I); it identifies the smallest element in the cycle associated with the ciphertext block $c_{i}$ and then through a simple table lookup, it identifies the corresponding $\overline{b_{i}}$. In the second step, the corresponding inverse permutation table is applied on $\overline{b_{2}}$ to obtain the original plaintext block $b_{i}$.

## Algorithm Encrypt II ;

Input to the algorithm is a stream of plaintext message blocks $b_{1} b_{2} \cdots b_{n}$, where, each $b_{i}$ consists of ' $r$ '-bits. Let there are be ' $p$ ' distinct blocks in the language, where $p \leq 2^{r}$.

Define a set of Permutation tables of cardinality $\kappa$ : $P_{1}, P_{2}, \cdots P_{\kappa}$, induced by either bit-permutation or matrix transformation scheme, where each table is of size $r$-bits. During enciphering, each $b_{i}$ will be associated with a $P_{j}$ (where, $j \leq \kappa$ ) and substituted as $r$-bit $\overline{b_{i}}$.

Define a matrix Tof Size $s \times s$ and a complement vector $S_{c}$ of same size which will generate at least $p$ number of cycles, each of which will correspond to $p$ distinct $r$-bit intermediate cipher-block $\overline{b_{i}}$ 's.
input: Plaintext message blocks $b_{1} b_{2} \cdots b_{n}$, where cach $b_{i}$ is of $r$-bits.
Ontput: $\mathrm{Ci}_{\mathrm{p}}$ hertext strean $c_{1} c_{2} \cdots c_{n}$, where cach $c_{i}$ consists of $s$-bits.
Step 1: $\quad i=1$;
Step 2: $\quad j=1$;
Step 3 : Read a $r$-bit block, $b_{i}$;
Substitute $b_{i}$ using the corresponding $P_{j}$ to obtain $\overline{b_{i}}$, i.e. $\overline{b_{i}} \leftarrow P_{j}\left(b_{i}\right) ;$
Step 4: Call Encrypt $I$ with $\overline{b_{i}}$ as input;
sclect an element ' $m$ ' randomly from the corresponding cycle of $\overline{b_{\imath}}$ and substitute it, i.c. $c_{2} \leftarrow m$;
Step 5: $\quad \jmath \leftarrow \jmath+1 ; \imath \leftarrow \imath+1$;
if $i \leq n$ and $j \leq \kappa$ then goto step 3 ;
if $i \leq n$ and $j>\kappa$ then goto step 2 ;
Step 6 : Stop execution.

## Algorithm Decrypt II

We will have a table of length $p$, where entrics of the table are the least element ( $x$ ) of cycles and corresponding $\bar{b}_{2}$.

Dcfine a set of corresponding Inverse Permutation tables : $\overline{P_{1}}, \overline{P_{2}} \ldots \overline{P_{\kappa}}$;

Input: The ciphertext $c_{1} c_{2} \cdots c_{n}$, where each $c_{1}$ is of $s$-bits.
Output: The deciphered text $b_{1} b_{2} \cdots b_{n}$, where each $b_{1}$ is of $r$-bits.
Step 1: $\quad \imath=1$;
Step 2: $\quad \jmath=1$;
Step 3: Call Decrypt I with $c_{\imath}$ as the input;
find the least element ' $x$ ' of the corresponding cycle associated with $c_{2}$ and assign to $\overline{b_{i}}$;
Step 4: $\Lambda$ pply the corresponding Inverse table $\overline{P_{j}}$ on $\overline{b_{2}}$ -
$b_{2} \leftarrow \overline{P_{j}}\left(\overline{b_{2}}\right) ;$
Step $5: \quad \imath \leftarrow \imath+1 ; \jmath \leftarrow \jmath+1$; if $\imath \leq n$ and $\jmath \leq \kappa$ goto Step 3 ;
if $\imath \leq n$ and $\jmath>\kappa$ goto step 2 ;
Step 8 : Stop execution.
For better understanding of the enhanced version of the proposed scheme, Example 4.4 is cited.

Example 4.4 Let the number of distinct plaintext blocks ' $p$ ' be 12 and the blocks be - $\delta_{1}, \delta_{2}, \cdots \delta_{12}$; and let each block consist of 4 bits. Now, let us define a set of bitpermutation tables $P_{1}, P_{2}, \cdots P_{\kappa}$ induced by cither the benary-matrix transformation or the but-permutation scheme, where, the cardinality of the sct, $\kappa \leq p$ and each $P_{3}$ is of size 4. During enciphering, each block of message (say $\delta_{2}$ ) is subjected to a permutation
table $P_{3}$ (chosen according to a sequence maintained) and the corresponding $\bar{\delta}_{1}$ is generated. The next step of cucryption with $\overline{\delta_{2}}$ is similar with that found in Example 4.1. As found in the previous example, select two key operators i.e. say $T_{1}$ and $S_{c 1}$ such that it generates at least $p=12$ cycles. Each of the $12 \bar{\delta}_{1}$ s is associated with any of the 12 cycles as shown in Table 41.

Now, consider that an example sequence of plaintext blocks be : $\delta_{9} \delta_{6} \delta_{2} \delta_{12} \delta_{9} \ldots$. Duing enciphoring, for instance, $\delta_{9}$ is associated with table $P_{1}$ and suppose after bitsubstitution it becomes $P_{1}\left(\delta_{9}\right) \rightarrow \delta_{3}$. Similarly, for the second and the third blocks i e. $\delta_{6}$ and $\delta_{2}$, let it be $P_{2}\left(\delta_{6}\right) \rightarrow \delta_{4}$ and $P_{3}\left(\delta_{2}\right) \rightarrow \delta_{4}$ repectively. Again, for the fifth block i.e. $\delta_{9}$, let the corresponding table be $P_{\jmath}$, where $\jmath=0 \cdots \kappa$. After substitution, let it becomes $P_{\jmath}\left(\delta_{9}\right) \rightarrow \delta_{5}$. Thus, the intermediate sequence of input blocks become : $\delta_{3} \delta_{4} \delta_{4} \delta_{2} \delta_{5} \cdots$.

With this sequence of input blocks, the next phase of enciphering will be similar as found in Example 41.

During decryption, the first step is similar with the deciphering operation that found in Example 4.1. It unambiguously identifies the cycle $B_{2}$ for each cipher-block and hence also the corresponding $\delta_{\imath}$ through a simple table look-up. Thus, through certain repetition one can lecover the entire sequence of the intermediate blocks i.e.

$$
\delta_{3} \delta_{4} \delta_{4} \delta_{2} \delta_{5} \cdots
$$

Nextly, one starts with the second step of decryption. Each intermediate block is picked up and subjected to inverse substitution. For instance, $\delta_{3}$ is taken and substituted with table $\overline{P_{1}}$, which will result $-\overline{P_{1}}\left(\delta_{3}\right) \rightarrow \delta_{9}$. Similarly, for the second and the third blocks i.e. $\delta_{1}$ and again $\delta_{1}$, it will be $\overline{P_{2}}\left(\delta_{4}\right) \rightarrow \delta_{6}$ and $\overline{P_{3}}\left(\delta_{4}\right) \rightarrow \delta_{2}$ respectively. Similarly, for the remaining other blocks also, the corresponding inverse tables will be applied and finally, one can casily obtain the original plaintext block sequences, i.c. $\delta_{9} \delta_{6} \delta_{2} \delta_{12} \delta_{9} \ldots$

Implementation of the proposed scheme : From the hardware implementation point of view, it can be found that as the sets are finite only and of only moderate size, one need not have a table stored in memory for the table look-up referred above. Only the matrix $T$ of order $s \times s$ and the complement vector $S_{c}$ of size $s$, which are the keys, are to be stored in memory, each row of the matrix itself being stored as a binary number. For instance, the mataix $T$ used in the illustrative example can
be stored as the sequence of six numbers $\{59,14,71,38,13,101,92\}$ written in binary foum. In fact, relevant matrix multiplication can obviously be carried out as suitably formulated operations on individual bits, a possible advantage in respect of hardware implementations. Software can be so constructed that when the task of encryption or decryption is at hand, oue is only to feed the key numbers viz. the matrix rows as 'numbers' and the software constructs the tables for mapping as well as cycle identifiers along with their cycle lengths.

From the software amplementation point of view, it has been found that- it is not necessary to use explicitly the CA multiplication and exclusive ORing- carried out on cach ciphertext block. At the start of encryption or decryption, one can generate the table or inverse table for mapping encrypted blocks to plaintext as a single subscript array and carry out decryption by table lookup.

### 4.3 Invulnerability of the Schemes

Security of the proposed schemes against possible attacks are discussed below :
(a) Ciphertext only attack: According to the schemes, as among the plaintext and ciphertext blocks, a many-to-many mapping exists, the schemes may be considered to be guarded against clypt-analyst's ciphertext only attack.
(b) Known and Chosen Plaintext attack: In case of known plaintext attack, the intruder is assumed to possess a considerable length of plaintext and the corresponding ciphertext. While in case of chosen plaintext attack, the intruder is able to acquire an arbitrary pairs of message and corresponding ciphertexts i.c. $(M, C)$ of his own choosing.

In case of both the schemes, the encryption is basically performed in two major steps and each step is independent of the other. So, the intruders' complexity will be the product of the individual complexities offered by each step. One can compute the cracking complexit, in the following manner:

- in step I, for an $r$-bit message block, due to the permutation operation, the possible order of complexity is: $O\left(2^{\prime}\right.$ !);
- in step II, the complexity offered is due to the key-space generated by the CA used;
if the size of the CA is ' $s$ ', in general, the size of the key-space is $O\left(2^{s^{2}}\right)$. However, the scheme uscs only those $\mathrm{C} \Lambda$ s which exhibit uitrnate perzodicıty propertics and generate ccrtain minimum number of cycles. Thus, the actual size of the keyspace should be less than the aforesaid size. From our exhaustive experimentation, based on sample data generated by random sampling it has been observed that for ( $s=6$ ), the proportion of matrices with at least 8 cycles is around $20 \%$ and for $(s=8)$ the proportion appears to be 21 percent; similarly, for $(s=7),(s=9)$ and ( $s=10$ ), it is reported in Table 4.2. Thus the complexity may be higher than $O\left(2^{s^{2} / 2}\right)$; Lastly, due to the complement operation using the complement vector $S_{c}$, of size ' $s$ ', the possible complexity is of order $O\left(2^{s}\right)$;

Hence, the total approximated complexity due to step I \& step II may be of the order of:

$$
O\left(2^{r}!\right) \times O\left(2^{s^{2} / 2}\right) \times O\left(2^{s}\right)
$$

- an extremely laıge numbeı!

Table 4.2: Finding ' $m$ ' for different CAs of size ' $s$ '

| No. of | Size of the Operator |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: |
| Sample Matrices | $T$ |  |  |  |  |
| $M$ | $s=6$ | $s=7$ | $s=8$ | $s=9$ | $s=10$ |
| 10 | 2 | 2 | 2 | 3 | 2 |
| 100 | 20 | 27 | 21 | 31 | 25 |
| 1000 | 197 | 214 | 219 | 259 | 267 |
| 10000 | 2108 | 2179 | 2203 | 2574 | 2682 |

### 4.4 Conclusion

Two simple, but invulnerable block ciphering schemes have been presented in this chapter. The schemes are based on the periodicity propertics of a finite set of elements ovel the field of GF(2). The encipherment and decipherment procedures of the schemes follow the similar protocols. Due to the non-linear operations and many-to-many mapping, the measure of strength of the proposed schemes against intrusion can be found to be comparable, if not better, than the existing schemes. There are further scopes to
improve the complexity by increasing the size of the message block as well as the CAs. The simplified logic structure makes the schemes more efficient from the implementation point of view.

In the modern cryptography, authenticated key exchange scheme has an important role in providing security over an insecure channel. In such scheme, one-way hash functions and cipher systems are used as the basic building blocks for authentication as well as data encryption purposes. A new password-only authenticated key-exchange scheme, has been developed based on the schemes designed and presented so far (i.e. in Chapter 3 and in the present), which will be discussed in the next Chapter.

## Chapter 5

## CA based Password Authenticated Key Exchange

### 5.1 Introduction

The theory of C.A and its applications in the area of data security and message authentication have been discussed in detail in the previous chapters (namely, Chapters 2, 3 6 4). It has been observed that it is possible to apply C.As and the CA based schemes reported so far, in the area of authenticated key exchange applications. In this chapter, an attempt has been made to explore such possibilities in password-only authenticated key exchange systems. Password authenticated key exchange schemes (PAKE) are very important for strong authentication over an insecure channel. Designing an efficient password scheme over an insecure network has been a challenging problem, particularly in the light of dictionary attack. There is an increasing volume of work focussed on the password problem in the last few years and several novel solutions have been produced [Schnr96, Menez97, Jabin96, Belvn92, Diff92]: From crypt-analysis point of view, large passwords are always preferable, whereas for ordinary people, it is difficult to remember them. So, construction of a strong remote user authentication scheme using only a small password is always encouraging. For user authentication purpose, though smart-cards are more convenient, there is always added advantages with a password-only authentication scheme, because firstly, it is less expensive and secondly, it is more resistant to theft. This chapter presents a new password-only authenticated key exchange scheme, designed by utilizing the features of group and non-group Cellular Automata (CA) [Palch97]. It uses the results reported in the earlier chapters (namely Chapters 2, 384 4). Due to
the simple logic structure and the high order of intruders' complexity, the proposed CA -based scheme could be found to be a potential alternative to the existing one. The scheme is shown to be guarded from various previously-known and new attacks.

Such authenticated key exchange schemes can have several applications, which may be broadly classified into two: user-to-host and user-to-user authentications. This chapter highlights some of the potential applications of the proposed CA based scheme. Next section discusses some of the existing related works and some general classifications derived from the literature survey.

### 5.2 Existing Related Works

The landmark 1976 paper of Whitefield Diffie and Martin Hellman [Diffi76b] is the pioneer work for both the seminal idea of public key cryptography and the fundamental technique of exponential key agreement. An early work of Diffie and Hellman [Diffi76a] presented the concept of public key agreement and the use of public-key techniques for identification and digital signature. In the fall of 1974, Merkle independently conceived a particular method for key agreement [Menez97], known as 'Merkle's puzzle system', which may be presented as follows. Alice constructs ' $m$ ' puzzles. each of which is a cryptogram and which Bob can solve in ' $n$ ' steps (exhaustively trying ' $n$ ' keys until a recognizable plaintext is found). Alice sends all ' $m$ ' puzzles to Bob over an insecure channel. Bob picks one of these, solves it (cost : ' $n$ ' steps) and treats the plaintext therein as the agreed key, which he then uses to encrypt and send to Alice a known message. The encrypted message, now a puzzle which Alice must solve, takes ' $n$ ' steps (by exhaustively trying ' $n$ ' keys). For $m \approx n$, both Alice and Bob require $O(n)$ steps for key agreement while an opponent require $O\left(n^{2}\right)$ steps to deduce the ker: Reuppel [Reupl90] explores the use of function composition to generalise Diffie-Hellman key agreement. Shmuely [Menez97] and McCurley [Mcrly88] considered composite Diffie-Hellman, i.e. Diffie-Hellman key agreement with a composite modulus. McCurley presents a variation thereof, with an RSA like modulus ' $m$ ' of specific form and particular base ' $r$ ' of high order in $Z_{m}^{*}$, which is probably as secure (under passive attack) as the more difficult of factoring ' $m$ ' and solving the discrete logarithm problem with modulo the factors of ' $m$ '. Regarding Diffie-Hellman key agreement, Van Oorschot and Wiener [Oorsc91c] note that the use of "short" private exponents in conjunction with a random prime modulo
' $p$ ' (e.g. 256-bit exponent with 1024 -bit ' $p$ ') makes computation of discrete logarithm easy. They also document the attacks, which is related to issues explored by Sımmon [Simon95] concerning a party's ability to control the resulting Diffie-Hellman key, and more general issues of unfairness in protocols. Waldvogel and Massey [Wldvg93] carefully examine the probability distribution and entropy of Diffie-Hellman keys under various assumptions. When private exponents are chosen independently and uniformly at random from $\{0,1 \cdots p-2\}$ (as is customary in practice); in the best case (when $p$ is a safe prime, $p=2 q+1$, where $q$ is prime) the most probable Diffie-Hellman key is only six-times more likely than the least probable, and the key entropy is less than 2-bits. While in the worst case governed by a particular factorization pattern of $p-1$ the distribution is still sufficiently good to preclude significant cryptanalytic advantage, for ' $p$ ' of industrial size or larger. The One-pass ElGamal key agreement protocol [Menez97] a variant of Diffie-Hellman, provides a one-pass protocol with unilateral key authentication, provided the public key of the recipient is known to the originator a priori. The MTI/AO protocol (as found in [Menez97]) is closely related to a scheme later presented by Goss. Matsumoto et al. equate the computational complexity of Passive attacks (excluding the known key attack) on selected key agreement protocols to that of one or two Diffie-Hellman problems. Active attacks (source substitution) on MTI/AO are considered by Diffie, van Oorschot and Wiener [Diffi92] and Menezes, Qu and Vanstone [Menez97]. Yacobi and Shmuely [Yacob90] note two time-variant versions of Diffie-Hellman key agreement which are insecure against known-key attacks. A similar protocol which falls prey to known-key attack was discussed by Yacobi [Yacob91], subsequently rediscovered by Alexandris et al. [Alexn93] and re-examined by Nyberg and Rueppel [Nybrg93]. Yacobi [Yacob91] proves that the MTI/AO protocol with composite modulo is probably secure under known-key attacks by a passive adversary; Desmedt and Burnmester [Desmd93], however, note the security is only heuristic under known-key attack by an active adversary. A formal logic security comparıson of the protocols of Goss, Gunther, and STS is given by van Oorschot [Oorsc92]. Burnmester [Burms94] identifies known-key triangular attacks, which may be mounted on the former two and related protocols, which provide only implicit key authentication (including MTI protocol). Variations of STS and an informal model for authentication and authenticated key establishment are discussed by Diffie, Oorschot and Wiener [Diffi92]. Bellovin and Merrit [Belvn92, Belvn93] propose another hybrid protocol (Encrypted Key Exchange - EKE) involving exponential key agreement with authentication based on a small shared password, designed specifically to protect against password-
guessing attacks by precluding easy verification of guessed passwords; Steiner, Tsudik and Waidner [Stein95] provide further analysis and extensions. A hybrid protocol with similar goals is given by Gong et al. [Gong93], including discussion of its relationships to EKE and expanding the earlier work of Lomas et al. [Lomas89]. Recently, Jablon [Jabln96] also proposed a simplified password exponential key exchange method, which is basically a variant of DH-EKE [Belvn92]. From the survey, it reveals that a strong authenticated key exchange scheme using only a small password, is always desirable for any insecure network. For the sake of understanding, the following subsections provide general classifications and some basic concepts, relevant to the proposed scheme, from [Menez97].

### 5.2.1 General Classifications

Key establishment is a process or protocol whereby a shared secret becomes available to two or more parties, for subsequent cryptographic use. Basically, one can have two broad subclasses of key establishments, such as: key transport and key agreement as defined below.

Definition 5.1 A key transport protocol or mechanism is a key establishment technique where one party creates or otherwise obtains a secret ralue, and securely transfers it to the other(s).

Definition 5.2 A key agreement protocol or mechanism is a key-establishment technique in which shared secret is derived by two (or more) parties as a function of information contributed by or associated with, each of these, (ideally) such that no party can pre-determine the resulting value.

Key establishment protocols involving authentication typically require a setup phase whereby authentic and possibly secret initial keying material is distributed. Most protocols have as an objective the creation of distinct keys on each protocol execution. In some cases the initial keying material predefines a fixed key which will result every time the protocol is executed by a given pair or group of users. Usually systems involving such static keys are insecure under known key attacks.

Definition 5.3 'Key pre-distribution' schemes are key establishment protocols whereby the resulting established keys are completely determined a priori by initial keying mate-
rial. In contrast, dynamic key establishment schemes are those whereby the key established by a fixed pair of users varies on subsequent executions.

Dynamic key establishment is also referred to as session key establishment. In this case, session keys are dynamic, and it is usually intended that the protocols are immune to known key attacks.

### 5.2.2 Basic Concepts

It is a desired property in a key establishment protocol that each participating party be able to determine the true identity of the other(s) which could possibly gain access to the resulting key, implying preclusion of any unauthorized additional parties from deducing the same key. In this case the technique is said to (informally) provide secure key establishment. This requires both secrecy of the key and identification of those parties with access to it. Furthermore, the identification requirement differs subtly, but in a very important manner, from that of entity authentication- here the requirement is knowledge of the identity of parties which may gain access to the key, rather than corroboration that actual communication has been established with such parties. In the following, various such related concepts are highlighted by the definitions. Entity authentication is defined as the process whereby one party is assured of the identity of a second party involved in a protocol, that the second has actually participated (i.e. active at, or immediately prior to, the time the evidence is acquired). Entity authentication presents protocols providing entity authentication alone.

Definition 5.4 Key authentication is the property whereby one party is assured that no other party aside from a specifically identified second party may gain access to a particular secret key.

Key authentication is independent of the actual possession of such key by the second party, it need not involve any action whatsoever by the second party. For this reason, it is sometimes, also referred to as (implicit) key authentication.

Definition 5.5 Key confirmation is the property whereby one party is assured that a second (possibly unidentified) party actually has possession of a particular secret key.

Definition 5.6. Explicit key authentication is the property obtained when both (implicit) key authentication and key confirmation hold.

In the case of explicit key authentication, an identified party is known to actually possess a specified key, a conclusion which can not otherwise be drawn. Encryption applications utilizing key establishment protocols which offer only implicit key authentication often begin encryption with an initial known data unit serving as an integrity check-word, thus moving the burden of key confirmation from the establishment mechanism to the application.

The focus in key authentication is the identity of the second party rather than the value of the key, whereas in key confirmation, the opposite is true. Key confirmation typically involves one party receiving a message from a second containing evidence demonstrating the possession of the key by the latter. In practice, possession of a key may be demonstrated by various means, including producing a one-way-hash encryption of a known quantity using the key.

Entity authentication is not a requirement in all protocols. Some key establishment protocols (such as unauthenticated Diffie-Hellman key agreement) provide none of entity authentication, key authentication and key confirmation. Unilateral key confirmation may always be added e.g. by including a one-way-hash of the derived key in a final message.

Definition 5.7 An authentic-key establishment protocol is a process or protocol whereby a shared secret becomes available to two or more parties and which provides assurance to the communicating parties that no other parties (except them) may gain access to a particular secret key.

The security of a protocol is examined based on the assumption that the underlying cryptographic mechanisms used, such as encryption algorithm and digital signature schemes are secure. A passive attack involves an adversary who attempts to defeat a cryptographic technique by simply recording data and thereafter by analyzing (e.g. in key establishment, to determine the session key). An active attack involves an adversary who modifies or injects messages.

It is simply assumed that protocol messages are transmitted over unprotected network, modeled by an adversary able to completely control the data therein, with the
ability to record, alter, delete, insert, redirect, reorder and reuse past or current messages, and inject new messages. An adversary in key establishment protocol may pursue many strategies, including attempting to :

- deduce session key using information gained by eavesdropping,
- participate covertly in a protocol initiated by one party with another, and influence it, e.g. by altering messages so as to be able to deduce the key;
- initiate one or more protocol executions (possibly simultaneously), and combine (interleave) messages from one with another, so as to masquerade as some party or carry out one of the above attacks.
- Without being able to deduce the session key itself, deceive a legitimate party regarding the identity of the party with which it shares a key.

In analyzing key establishment protocols, the potential impact of compromise of various types of keying material should be considered, even if such compromise is not normally expected. In particular, the effect of the following is often considered :

1. Compromise of long term secret (symmetric and asymmetric) keys, if any, and
2. Compromise of past session key.

A protocol said to have perfect forward secrecy if compromise of long term keys does not compromise past session key. The idea of perfect forward secrecy (sometimes called break forward protection) is that previous traffic is locked securely in the past. A protocol is said to be vulnerable to a known key attack, if compromise of past session keys allows either a passive adversary to compromise future session keys, or impersonation by an active adversary in the future.

Next section presents a CA based authenticated key exchange scheme, which fulfills the requirements, as determined in the previous discussion. The scheme is designed based on the properties of group \& non-group CAs as discussed in Chapter 2 as well as the schemes developed and reported so far, in the Chapter 3 \& 4.

### 5.3 CA based Password-only Authenticated Key Exchange : CPAKE

The objective is to design an authenticated key exchange scheme based on some small shared password, which not to be vulnerable to dictionary attack. The scheme should bridge the growing gap between the smallest safe key and the size of the largest easily remembered password.

The proposed CPAKE scheme operates in two major phases; the first phase, establishes the secret session key $K$, through exchange of intermediary computed values $Q$; and in the second phase, both confirm each other's knowledge of the key i.e. $K$ before proceeding to use it as a session key. Each of these phases operates in a sequence of stages. Key establishment phase is operated in two major stages and each stage follows multiple steps of processing. In the first stage, both $A$ and $B$ uses a small ( $r$-bits) shared password $Y_{p}$ as input to a function $f_{e}\left(Y_{p}\right)$, which expands it into an $2 r$-bits $Y_{p}^{\prime}$. Next $Y_{p}^{\prime}$, is further operated with a Pseudo-random sequence-based permutation scheme $\pi$ to generate $Y_{p}^{\prime \prime}$. A strong one-way hashing scheme $H_{1}$ is applied on $Y_{p}^{\prime \prime}$ to finally generate a $2 r$-bits digest $Q_{A}$, which is communicated to $B$. At the other end also, $B$ will follow the similar protocol to generate $Q_{B}$ and will be communicated to $A$. The second stage then computes the secret session key based on the values of $Q_{A}$ and $Q_{B}$ and a small ( $r$-bits), shared, secret key $m$. It performs in two steps : in the first step, both $A$ and $B$ uses $m$ with each of the $Q_{A}$ and $Q_{B}$ and after mixing up the bit-patterns using the function ((after necessary padding of 0 's), they are subjected to the hash function $H_{1}$ to obtain the corresponding digests $Q_{A}{ }^{\prime}$ and $Q_{B}{ }^{\prime}$ ( $2 r$-bits each) respectively. These bitpatterns (i.e. $Q_{A}{ }^{\prime}$ and $Q_{B}{ }^{\prime}$ ) are then again operated with $\eta$ and the output is hashed using another strong one-way function $H_{11}$ to generate finally the $2 r$-bits shared session key $K$.

It is presumed that John and Diana (i.e. $A$ and $B$ ) are two well-behaved legitimate parties. In user-to-host situation, John is the user. The various notations along with their meanings, used in this scheme are described in Figure 5.1. The logic for the Phase-I operations to establish the session key is presented in Figure 5.2. In the second phase, both $A$ and $B$ confirms each other's knowledge of $K$ before proceeding to use it as a session key. For confirmation purpose, either one can use the traditional keyconfirmation method, as found in [Jabln96], or, any of the CA based encryption schemes
found in [Schnr96, Palch97, Menez97] or, the ENCA based cipher system reported in the previous chapter (i.e. Chapter 4 of the present thesis). To use the scheme proposed in Chapter 4, the user will select an operator $T$, based on the value of $K$. Here, $T$ can be either Group or a non-group CA. For confirmation, each communicates to the other a randomly chosen number say $c_{A}$ or $c_{B}$, which will be used as a basin element by both the end and by using $T$ repeatedly, either the attractor (in case of non-group CA) or the least element in the corresponding cycle (in case of group CA) i.e. say, $\gamma$ will be computed. Next, each of them will verify $\gamma_{A}$ or $\gamma_{B}$ with respect to $T$. The steps of processing for each phase are noted below :

| $Y_{p}$ | $:$ a small ( $r$-bits) shared password for John and Diana. |
| :--- | :--- |
| $f_{e}\left(Y_{p}\right)$ | $:$ a function to expand $Y_{p}$ into a $2 r$-bits $Y_{p}^{\prime}$. |
| $R$ | $:$ a maximal-length Group CA-based Pseudo-random Sequence Generator. |
| $\pi_{v}^{y}$ | $:$ a permutation scheme $\pi$ based on non-maximal-length group CA where |
|  | $: v^{\prime}$ represents the particular CA and ' $y$ ' represents the cycle-length. |
| $H_{1}, H_{11}$ | $:$ two group and non-group CA based strong One-Way hash functions. |
| $m$ | $:$ a small (r-bits) shared secret for John and Diana. |
| $A \rightarrow B: \gamma_{A}$ | $:$ John sends the value ' $\gamma_{A}$ ' to Diana. |
| $\eta(w, z)$ | $:$ a function to mix $2 r$-bits patterns $w$ and $z$ to generate a $2 r$-bits patterns. |
| $K$ | $:$ a $2 r$-bits session key. |

Figure 5.1: Various Notations used and their meanings

## Phase I : Computation of the Secret Session Key

S1. John computes: $\quad Q_{A^{-}} \leftarrow H_{1}\left(\pi\left(f_{e}\left(Y_{p}\right)\right)\right) \quad A \rightarrow B: Q_{A}$
S2. Diana computes: $\quad Q_{B} \leftarrow H_{1}\left(\pi\left(f_{e}\left(Y_{p}\right)\right)\right) \quad B \rightarrow A: Q_{B}$
S3. John Computes: $K \leftarrow H_{11}\left(\eta\left(H_{1}\left(m, Q_{A}\right), H_{1}\left(m, Q_{B}\right)\right)\right)$
S4. Diana Computes: $K \leftarrow H_{11}\left(\eta\left(H_{1}\left(m, Q_{A}\right), H_{1}\left(m, Q_{B}\right)\right)\right)$

Phase II : Confirming the knowledge of the Key by each other

S5. John chooses random $c_{A}$ and computes: $\gamma_{A} \leftarrow T^{r 1} \cdot\left(c_{A}\right) \quad A \rightarrow B: \gamma_{A}$
S6. Diana chooses random $c_{B}$ and computes: $\dot{\gamma_{B}} \leftarrow T^{r 2} .\left(c_{B}\right) \quad B \rightarrow A: \gamma_{B}$
S7. John verifies that $\gamma_{B}$ is attractor or least-element corresponding to $T$
S8. Diana verifies that $\gamma_{A}$ is attractor or least-element corresponding to $T$


Figure 5.2: Block diagram of Session Key management

For more concrete confirmation, one can use additionally a secret-key symmetric enciphering scheme on $\gamma_{A}$ or $\gamma_{B}$ before communication. In the following sub-section, the various modules and functions used, are described in brief :

Expanding Function : $f_{e}\left(Y_{p}\right)^{-}$
This operation is similar with the E-Box operation as found in [DES67]. The $r$-bits $Y_{p}$ is expanded to $2 r$-bits $Y_{p}^{\prime}$ by an expansion permutation. This operation has mainly two purposes: it makes the result the same size (i.e. $2 r$ ) for the next step of operation, and it provides a longer result that can be compressed during hashing operation. Because of this expansion, the dependency of the output bits on the input bits spreads faster.

## CA Based Permutation Module : $\pi$

Several permutation schemes can be found in [Schnr96, Menez97]. A CA based potential alternative to the existing permutation schemes can be found in [Palch97]. The major advantages of the CA based permutation schemes are : (a) they are easily imple-
mentable and (b) there are scopes to improve the intruders' complexity to a great extent by - (i) configuring the rule-vectors dynamically (to have combinations of multiple CAs, i.e. $\pi_{1}, \pi_{2}, \pi_{3} \cdots$ ), and (ii) using a sequence of cycle-lengths (i.e. $y$ 's) for the permutations, which are pseudo-random in nature. The cycle-length sequences are obtained from a CA based pseudo-random sequence generator, $R$.

The maximum-length group CAs can be used as an efficient pseudo-random sequence generators [Barde90, Nandi94a]. It is well known fact that fixed-key pseudo-random sequence generator is vulnerable to the intruders' correlation attack. Thus, it is desirable to have a running key generator consists of several pseudo-random sequence generator with a non-linear combining functions. The scheme proposed in the present chapter [Nandi94a], or a variant of it, based on Programmable CA (as found in Section 2 from Chapter 2) can be used here.

## CA Based One-Way Hashing Function : $H$

The proposed CPAKE uses a CA based hashing scheme, designed based upon the properties of group, non-group and non-linear CAs, with a similar concept as discussed and reported in Chapter 3. The scheme hashes $2 r$-bits $Y_{p}^{\prime \prime}$ into a fixed-length $r$-bits hash value in feedback mode. Hashing is performed mainly in two steps : in the first step, $r$-bits block is taken, divided into ' $k$ ' sub-blocks; these sub-blocks are then subjected to three operations: Bit-wise substitution, XORing with Constants and Enciphering using a PCA based Block Cipher (a variant of which is reported in Chapter 4). With a shift-rotate operation among these sub-blocks, the above these operations are repeated for ' $k$ ' cycles. The final $r$-bits (concatenated) output is then concatenated with the previous $r$-bits hash value (in case of the first block, it will be zeros) and then input to a $2 r$-bit non-group multiple attractor CA (MACA). CA runs for few cycles to reach the attractor [Palch97]. The Pseudo-Exhaustive $r$-bits of the attractor are then separated out as the present hash value, $h_{2}$. Similar process will repeat for the second block also. Thus, after repeating the processes for several cycles, the final hash value of the $2 r$-bits input block, i.e. $Y_{p}^{\prime}$ is generated. In the following section, an analysis of the scheme in light of the various known and unknown intruders' attacks is presented.

### 5.4 Invulnerability of CPAKE

The proposed scheme is designed with an integrated key exchange supported by mutual authentication provision. It sufficiently proves to each of the two parties that the other knows the password. The scheme aims to generate a session key for securing a subsequent authenticated session between the parties, which does not leave any separation information regarding its individual steps. The scheme also does not generate any persistent data, which have to be distributed and securely stored. It shares only a small password $Y_{p}$ and a small key $m$ (i.e. for $r=64$, a total of 128 -bits, reasonably small in size for a secret key). Thus, the scheme is advantageous in this context. Security of the scheme against the various possible attacks are now discussed :

## Dictionary Attack

All passwords are vulnerable to dictionary attack - if any opportunity is given. So, the primary job of the designer is to remove the opportunities. Dictionary attacks can be online as well as offine. In case of the proposed scheme, the online dictionary attack can be easily detected by counting the access failures and thus thwarted. However, offline dictionary attacks are of complex type and it needs to be handled with care. One can make this attack by posing as a legitimate party to gather information, or by one who monitors the messages between two parties during a legitimate valid exchange. A very little information 'leakage' during an exchange can be exploited. If the expansion, permutation or hashing functions are not carefully built, the exchanged messages $Q_{A}$ or $Q_{B}$ may reveal discernible structure, and can "leak" information about $Y_{p}$. In the following - it has been attempted to establish the efficiency of each function or module of the CPAKE, in this regards.

- In case of the expansion permutation $f_{e}$, by allowing each bit of the secret password i.e. $Y_{p}$ to undergo this expansion permutation, the avalanche effect can be increased, because- dependency of the output bits on the input bits increased substantially.
- For the $C A$-based randomizer $R$, it has been established in [Nandi94a] that- the sequence generated by $R$ fulfills all the Knuth's criteria and hence ensures the desired immunity against the conventional correlation attack. The huge exponential
order of intruders' complexity to crack-key stream also guards the scheme from known plaintext attack.
- In case of the permutation scheme $\pi$, as the same ciphertext may be generated from different plaintext, as well as any ciphertext may give rise to different plaintext under different CA rule configurations, the scheme is guarded from caphertext only attack. The exponential order of intruders' complexity guards the scheme from other known as well as chosen plaintext attacks.
- Due to the non-group, non-linear features of complemented MACA in the one-way hashing scheme $H$, as well as the due to the PCA-based block ciphering strategy used for intermediate substitution, the scheme has been found to be immune from hash-value only attack. In case of the known as well as chosen (message, hash-value) attack, as the scheme offers an exponential order of complexity, approximately of the order of $O\left(2^{8 \times r}\right)$ (as reported in Chapter 3), the scheme is guarded from other possible attacks.


## Stolen Session Key Attack

In this type of attack, a stolen session key $K$ is used to mount a dictionary attack on the password $Y_{p}$ [Jabln96, Stein95]. CPAFE appears to be guarded in this attack, because with only $K$, probably it will not be easy to compute $Y_{p}$ - it requires the appropriate assessment of $R, \pi, f_{e}$ and also the hash functions $H_{1}$ and $H_{11}$ to find $Y_{p}$, whereas each of them already has been established to be immune from ciphertext only attack.

## Verification Stage Attack

The verification stage of CPAKE is where both parties prove to each other- knowledge of the shared key $K$. As $K$ is cryptographically large, the second stage is presumed to be immune to brute-force attack.

### 5.5 Applications of CPAKE

Password-only schemes are broadly useful for any applications where the prolonged key storage is risky or impractical, and where the communication channel may be insecure.

Some of its common applications are : user-to-user applications, diskless workstations, bootstrapping new system installation, cellular phones or other key-pad systems, multifactor password + key systems etc. From the economic point of view as well as to encounter the stolen key problems, these authentication schemes are always preferable than the smart-cards. Applications of password-only methods basically can be classified into two : user-to-host authentication and user-to-user authentication; some of the potential applications of the proposed CPAKE are described here.

### 5.5.1 User-to-Host Authentication

In case of the systems, where only a numeric key-pad is available, e.g. cellular telephone authentication, such a CA based password-only scheme is especially convenient, as it is based on a small numeric password. TV remote-controlled set-top boxes might be another area of new applications for the proposed scheme. It is advantageous in terms of these applications, because- it avoids the necessity for long-term storage of persistent keys for such environments.

Diskless workstations are another class of device where it is inconvenient to have locally stored keys. The proposed password-only method can be ideal for establishing an initial connection to a trusted host, and to obtain the user's safely stored credentials. The concept of bootstrapping a new secure system is broad, and is best illustrated with a common case. Unless some additional site-specific keys are manually installed on the system, a strong password-only method is needed to allow the new station to make a secure channel to the rest of the network. Once an authenticated channel is established, the station can automatically obtain any further credentials or keys. Similar bootstrapping situation arise in almost all secure systems.

### 5.5.2 User-to-User Authentication

So far, it has been established the usage of CPAKE on user-to-host authentication; this method is equally useful in direct user-to-user authentication also. [Ellis96] describes the use of an interactive questionnaire session to authenticate the identity of a user across a network. The main idea behind this authentication is that they are sharing some common facts, which has to be proved to each other, without revealing those facts.

Such general authentication paradox can easily be solved by the proposed CA based authentication method. For example, in a bank application, the banker may want to know that his client knows his secret social security number, and at the same time, the client may also like to know that the bank knows his secret account number, but neither wants to reveal the information directly to the other. In solving such a problem, a CA based password-only method can be successfully applied.

### 5.6 Conclusion

A new password-only authentication protocol based upon the properties of group and non-group CAs is introduced in this chapter, which appears to be at least as strong as the existing SPEKE [Jabln96] and DH-EKE [Diffi92] methods. Using particularly a small password, the proposed method provides authentication over an insecure channel, and are immune to offline dictionary attack. Due to its exponential order of intruders' complexity, the scheme is guarded against the other possible types of attacks. The proposed scheme utilizes non-group CA (MACA) as an efficient hashing function generator and the PCA based block ciphering mechanism, in generating the intermediate values. The major advantage of the scheme is the use of simple, regular, modular and cascadable structure of CA as the basic building block that is ideally suitable for VLSI implementation. The possible usage of the proposed scheme has been justified in many application domains, such as: user-to-host authentication, user-to-user authentication etc. In all such applications, one of the major requirements is the receiving of error-free information by both the participating parties. As such, it is essential that the errors if any, caused during transmission of information be detected and (if possible) corrected at the receiving end. The next chapter presents two schemes which take into account such communication errors.

## Chapter 6

## Theory and Design of Unidirectional Error Correcting Codes

### 6.1 Introduction

In the earlier chapters theory and applications of binary matrices for designing authorization and data security schemes have been addressed. With the advancement in the convergence of computer and communication technologies, there has been an increasing demand for efficient and reliable digital data transmission and storage systems. This demand has been accelerated by the emergence of large-scale, high-speed data networks for exchange, processing and storage of digital information in the military, governmental and private spheres. In this background, a major concern of a researcher is to control the errors so that reliable reproduction of data can be obtained.

It is observed that many faults in VLSI memories, PLA, shift registers are due to three classes of errors : (a) Symmetric, where both $1 \rightarrow 0$ and $0 \rightarrow 1$ errors are equally likely in a codeword, (b) Asymmetric, where only one of the errors, $1 \rightarrow 0$ or $0 \rightarrow 1$, can occur in a codeword, and (c) Unidirectional, where both $1 \rightarrow 0$ and $0 \rightarrow 1$ errors can occur but not in the same codeword. The various possible causes of such errors are : transient, intermittent and permanent, among which the transient errors are responsible for mostly limited number of symmetric or multiple unidirectional errors. The intermittent faults cause a limited number of errors and, but the permanent faults may cause both symmetric as well as the unidirectional errors. Among these errors, many faults in VLSI circuits cause mostly unidirectional errors [Ra089]. The number
of symmetric errors is usually limited while the number of unidirectional errors can be very large. Thus, construction of an efficient class of symmetric error(s) correcting codes which can also simultaneously detect all unidirectional errors, is essential. In the next subsection, the background of such error correcting codes with review of some of the existing related works have been discussed.

### 6.1.1 A Review of Error Correcting Codes

In a generalized error correcting code, the source encoder transforms the information sequence $I_{s}$ into another sequence $C$, called the codeword. In most instances $C$ is a binary sequence. After transfer through the coding channel, let the codeword be transformed from $C$ to $C^{\prime}$ due to some error. The decoder receives the codeword $C^{\prime}$ that is the same as $C$ in error free condition. Using some error correction logic, the errors, if there are any, are detected or corrected by the decoder on processing the codeword $C^{\prime}$. The correct information sequence $I_{s}$ can thus be forwarded to the destination. There are two different types of codes in common use : (a) Block Codes and (b) Convolutronal Codes. This chapter is restricted to the linear block codes only. The basic principles of linear block codes are briefly given as follows. A detailed discussion on block codes and convolution codes may be found in [Rao89].

Linear Block Codes : A block code of length $n$ and $2^{k}$ codewords is called a linear ( $n, k$ ) code if and only if its $2^{k}$ codewords form a $k$-dimensional subspace of the rector space of all the $n$-tuples over the field GF(2). A binary block code is linear iff the module-2 sum of two codewords is also a codeword; that is, if $u$ and $v$ are two codewords than $u+v$ is also a codeword, where + refers to bit-wise module-2 sum. Let, the vector space $V_{n}$ of all $n$-tuples over $G F(q)$ be

$$
\mathrm{V}_{\mathrm{n}}=\left(a_{0}, a_{1}, a_{2}, \cdots, a_{n-1}\right) \mid a_{\imath} \in G F(q) ;
$$

A subset $W$ of $V_{n}$ is a linear code, if and only if it is a subspace. Since $W$ is a subspace, all the codewords of $W$ can be conveniently represented as the row space of a ( $k \times n$ ) matrix $G$, called the generator matrix, which is given by,

$$
G=\left[\begin{array}{cccc}
g_{00} & g_{01} & \cdots & g_{0, n-1} \\
g_{10} & g_{11} & \cdots & g_{1, n-1} \\
\cdots & \cdots & \cdots & \cdots \\
g_{k-1.0} & g_{k-1,1} & \cdots & g_{k-1, n-1}
\end{array}\right]=\left[\begin{array}{c}
g_{0} \\
g_{1} \\
\cdots \\
g_{k-1}
\end{array}\right]
$$

If the row vectors of $G$ are linearly independent, then $W$ has dimension $k$ and has exactly $q^{k}$ codewords in it. Such a code $W$ is called an ( $n, k$ ) code. Alternatively, $W$ can be defined as the 'null space' of the parity matrix $H$, which may be written as,

$$
H=\left[\begin{array}{c}
h_{0} \\
h_{1} \\
\cdots \\
h_{r-1}
\end{array}\right]=\left[\begin{array}{cccc}
h_{00} & h_{01} & \cdots & h_{0, n-1} \\
h_{10} & h_{11} & \cdots & h_{1, n-1} \\
\cdots & \cdots & \cdots & \cdots \\
h_{r-1,0} & h_{r-1,1} & \cdots & h_{r-1, n-1}
\end{array}\right]
$$

Again the $r$ vectors of $H$ are linearly independent, and thus $H$ has rank $r$ and its null space has dimension $(n-r)$. Therefore, the $H$ matrix of an $(n, k)$ code satisfies the relation $r=n=k$. The $G$ matrix can be represented in its systematic form [Rao89] as $G=\left[I_{k}, P\right]$, where, $I_{k}$ is a $k \times k$ identity matrix, and $P$ is the 'parity generator matrix', which operates on the information block to generate the check-bits. The $H$ matrix is represented as $H=\left[-P^{T} I_{n-k}\right]$, so that $g_{2} h_{j}=0$, for all $\imath, \jmath$; that is, $G$ is orthogonal to $H . P^{T}$ refers to the transpose of $P$ and the "-" sign implies negation of $P^{T}$; i.e. an element $p_{\imath \jmath}$ of $P$ becomes $-p_{\imath \jmath}$ in $-P$, where $-p_{\imath \jmath}$ is the additive inverse of $p_{\imath \jmath}$ (in mod- 2 operation, $-p_{t \jmath}=p_{2 \jmath}$ ).

Let us now consider a data (information) sequence $I_{s}$ of $k$ symbols ( $\imath_{0}, \imath_{1}, \cdots \imath_{k-1}$ ). If $W$ is an $(n, k)$ linear code over $\operatorname{GF}(q)$, the codeword will be an $n$-tuple $C=$ ( $c_{0}, c_{1}, \cdots, c_{n-1}$ ). If the symbols ( $2_{0}, \imath_{1}, \cdots, \imath_{k-1}$ ) of information $I_{s}$ appear in its codeword $C$ unchanged, then the code is said to be a Systematzc Code [Lin83]. So, if the parity matrix $H$ is of systematic form $H=\left[P^{T} I_{n-k}\right]$, then the codeword $C=\left[H . I_{s}\right]$ generates a systematic code. It is often very important in computer systems that the codewords are in systematic form for speed, cost, and convenience in decoding and processing.

The decoding of linear codes is usually done in parallel, based on the $H$ matrix of the code. For a received word $C^{\prime}=\left(c_{0}{ }^{\prime}, c_{1}{ }^{\prime}, \cdots, c_{n-1}{ }^{\prime}\right)$, its syndrome $s\left(C^{\prime}\right)=\left(s_{0}, s_{1}, \cdots, s_{n-k-1}\right)$ is defined as $s\left(C^{\prime}\right)=C^{\prime} \cdot H^{T}$. If $s=0$, then there are no errors in the received codeword; whereas for $s \neq 0$, some errors are detected. Based on the properties of the code, the detection and correction steps are implemented in the decoder. Let us assume that the correct codeword transmitted is $C=\left(c_{0}, c_{1}, \cdots, c_{n-1}\right)$, and the corresponding received word is $C^{\prime}=\left(c_{0}^{\prime}, c_{1}{ }^{\prime}, \cdots, c_{n-1}{ }^{\prime}\right)$. Then the error word is $E=\left(e_{0}, e_{1}, \cdots, e_{n-1}\right)$ such that -

$$
\begin{aligned}
C^{\prime}= & C+E \text { and, } E=C^{\prime}-C=\left(e_{0}, e_{1}, \cdots, e_{n-1}\right) ; \\
& \text { i.e., } e_{\imath}=c_{\imath}^{\prime}-c_{\imath} \text { for } \imath=0,1, \cdots n-1 . ;
\end{aligned}
$$

Then, $s\left(C^{\prime}\right)=C^{\prime} \cdot H^{T}=C \cdot H^{T}+E \cdot H^{T}=0+E \cdot H^{T}=E \cdot H^{T}=s(E)$. A few encoding/decoding schemes of linear block codes are reviewed next.

Hamming Codes :Hamming codes are the first major class of linear block codes designed for error correcting purpose [Rao89]. For a Hamming code of length ( $2^{m}-1$ ) (where $m$ is a single integer)- one has to construct a matrix where columns consist of all non-zero binary $m$-tuples. For example, a ( $n, k$ ) Hamming code is defined by the parity-check-matrix $H$, where the ordering of the columns is arbitrary and the matrix is designed specially to describe a systematic code. In the corresponding generator matrix $G$, the $k$-information bits always occupy the last $k$ co-ordinates of each codeword. In general, the minimum distance of ( $n, k$ ) Hamming code, i.e. the smallest number of distinct non-zero binary $m$-tuples that can sum to zero is three, and it can be used either as : (i) Single Error Correcting (SEC), or (ii) Double Error detecting (DED) code.

However, one can modify a ( $n, k$ ) Hamming code by adding one parity bit ( $n+1, k$ ) SEC-DED code, where the syndrome-bit is the XOR sum of all $(n+1)$ inputs; which results in higher hardware cost and circuit delay. To circumvent this problem, the Hamming SEC-DED code has been modified and optimized. The resulting code is called modified Hamming SEC-DED code or Hszao Code [Palch97], which is described next.

Hsiao Code : Here, the minimum distance of a SEC-DED code is at least 4. Since, an $n$-tuple of weight 3 or less is not a codeword, any set of 3 columns of the $H$ matrix should be linearly independent. The sum of two odd-weight $r$-tuples is an even-weight $r$-tuple (i.e. odd + odd $=$ even; even + odd $=$ odd; even + even $=$ even). Based on this property, a SEC-DED code with $r$ check-bits can be constructed by performing some row operations on Hamming SEC-DED $H$ matrix. The modified $H$ matrix consists of distinct non-zero $r$-tuples of column vectors having odd-weight. This modified Hamming code is called odd-wezght-column SEC-DED code or Hsaao code because every $H$ matrix column vector is odd-weight.
$t$-Error Correcting Codes : Let $C_{1}$ and $C_{2}$ be two codewords in $C$, such that the minimum distance $D$ (say) between them can be defined as : $d\left(C_{1}, C_{2}\right)=D$. Let $E_{1}$ and $E_{2}$ be two error patterns that satisfy the conditions: (a) $E_{1}+E_{2}=C_{1}+C_{2}$; and (b) $E_{1}$ and $E_{2}$ do not have non-zero components in common place. Thus we have :

$$
\begin{equation*}
W\left(E_{1}\right)+W\left(E_{2}\right)=W\left(C_{1}+C_{2}\right)=d\left(C_{1}, C_{2}\right)=D \tag{6.1}
\end{equation*}
$$

Now, suppose that $C_{1}$ is transmitted and is corrupted by the error pattern $E_{1}$. Then, the received codeword is : $R=C_{1}+E_{1}$; The Hamming distance between $C_{1}$ and $R$ is thus,

$$
\begin{equation*}
d\left(C_{1}, R\right)=W\left(C_{1}+R\right)=W\left(E_{1}\right) \tag{6.2}
\end{equation*}
$$

Similarly, the Hamming distance between $C_{1}$ and $R$ will be:

$$
\begin{equation*}
d\left(C_{2}, R\right)=W\left(C_{2}+R\right)=W\left(C_{2}+C_{1}+R\right)=W\left(E_{1}\right) \tag{6.3}
\end{equation*}
$$

Now, suppose that the error patterns $E_{1}$ contains more than $t$-errors (i.e. $W\left(E_{1}\right)>t$ ). Since, $2(t-+1) \leq-D \leq(2 t+2)$, based on equation 6.1, we have : $W\left(E_{2}\right) \leq(t+1)$.
Combining equations $6.2 \S 6.3$ and using the fact that $W\left(E_{1}\right)>t$ and $W\left(E_{2}\right) \leq(t+1)$, we obtain the following inequality :

$$
\begin{equation*}
d\left(C_{1}, R\right) \geq d\left(C_{2}, R\right) \tag{6.4}
\end{equation*}
$$

This inequality says that there exists an error pattern of $l(l>t)$ errors which results in a received codeword that is closer to an incorrect codeword than to the transmitted codeword. Summarizing the above results, a block code with minimum distance $D$ guarantees correcting all the error patterns of $t=\lfloor(D-1) / 2\rfloor$ or fewer errors, where $\lfloor(D-1) / 2\rfloor$ denotes the largest integer no greater than $(D-1) / 2$. The parameter $t=\lfloor(D-1) / 2\rfloor$ is called the 'random error correcting capability' of the code. The code is referred to as a $t$-error correcting code.

Fujiwara [Fujiw78] proposed a generalized odd-weight-column code, where the $H$ matrix of the subspace $W$ over $\operatorname{GF}\left(2^{q}\right)$ satisfies the following condition for every column in the $H$ matrix : $\sum_{\imath=0}{ }^{r-1}=I_{q}$, for columns, $\jmath=0,1, \cdots, n-1$; where, $h_{2, j}$ is the $\imath^{\text {th }}$ element in the $\jmath^{\text {th }}$ column vector $\in \mathrm{GF}\left(2^{q}\right) ; I_{q}$ is the identity element of $\mathrm{GF}\left(2^{q}\right)$, and $\sum$ denotes summation in $\mathrm{GF}\left(2^{q}\right)$. The major advantage of this code is that it has a minimum equal-weight code, which makes the hardware implementation of the encoding/decoding circuit optimal.

However, the current survey reveals that the failures in the cells of semiconductor based large scale integrated (LSI) non-volatile memories are most likely caused by leakage of the charge, since a charge cannot be created except by a rewrite process. These memory cells are apt to exhibit unidirectional errors. Although the rest of the memory system
the address decoding, the cell selection, the gating logic and so on is subject to symmetric failures, for the overall memory system, the probability of unidirectional errors is significantly large. Some of the theoretical basics of unidirectional errors are described next.

Unidirectional Error Codes : Let, $N(X, Y)$ represents the number of $1 \rightarrow 0$ crossovers from $X$ to $Y$. That is, $N(X, Y)$ is the number of positions $i$ for which $x_{1}=1$ and $y_{2}=0$. For example, when $X=(10101)$ and $Y=(10010), N(X, Y)=2$ and $N(Y, X)=1$. The asymmetric distance is,

$$
d_{a}(Y, X)=\max [N(X, Y), N(Y, X)]=2
$$

Definition 6.1 For vectors $X=\left(x 1, x 2, \cdots x_{n}\right)$ and $Y=\left(y 1, y 2, \cdots y_{n}\right), X$ is said to cover $Y$ if for all $i, y_{2}=1$ implies $x_{2}=1$.

We can write this as $Y \leq X$. If $X \leq Y$ and $Y \leq X$, then $X$ and $Y$ are said to be unordered. If $X \leq Y$ or $Y \leq X$, then they are ordered pair. For $X_{1}=$ (1011) and $Y_{1}=(1001)$, then $Y_{1} \leq X_{1}$. Also $X_{2}=(1010)$ and $Y_{2}=(0110)$ are unordered. Also, if $X$ and $Y$ are an ordered pair, then their $d_{a}(X, Y)<d(X, Y)$. The unidirectional errors in a code are detected based on the following theorem.

Theorem 6.1 A code $C$ is capable of detecting all unidirectional errors (i.er it is a $A U E D$ code) if and only if every pair $X, Y \in C$ are unordered.

Two important classes of AUED codes are known as constant-weight codes and Berger codes. The constant-weight or m-out-of-n codes are of non-systematic as well as nonlinear type. But, for any given $n$, the number of codewords (of weight $m$ ) is given by $\binom{n}{m}=n!/((n-m)!m!)$. For the code $m=\lfloor n / 2\rfloor$ or $[n / 2\rceil$ this number is maximized. This class of constant-weight code has the higher possible information rate, because of which- it is referred to as optimal class of AUED codes [Ra089]. However, the Berger codes are systematic type; for the codeword $\left[a_{0}, a_{1}, \cdots a_{k-1}, a_{k}, \cdots, a_{n-1}\right.$, the information part is : $\left(a_{0}, a_{1}, \cdots, a_{k-1}=I_{s}\right.$ and $\left(a_{k}, \cdots, a_{n-1}\right)=\beta\left(I_{s}\right)$ is the Berger check bits. The Berger check $\beta\left(I_{s}\right)$, is the binary number representing the number of 0 's in $I_{s}$. The number of check-bits $r$ required is given by $r=n-k=\left[\log _{2} k+1\right]$, e.g., for a 6 -bit $(k=6)$ information, $r=\left[\log _{2} 6+1\right]=3$. Berger check(s) are important and form the basis for the construction of systematic classes of $t-E C / A U E D$ codes, which is described next.
$t$-EC/AUED Codes : This class of codes have several applications such as semiconductor memories, PLA, shift registers etc [Pradh80]. Bose and Rao [Bose82] had shown that a code is a $t$-EC/AUED code if and only if, for all distinct $X, Y \in C$, $N(X, Y) \geq t+1$ and $N(Y, X) \geq t+1$, where $N(X, Y)$ is the number of $1 \rightarrow 0$ crossovers from $X$ to $Y$. In practice, however the codes are desired to be systematic. Most of the designers construct it by adding a tail to $t$ - EC code such that the resulting code becomes $t$-EC/AUED code. In [Blaum89], Blaum and van Tilborg proposed their $t$-EC/AUED code by constructing ( $\left.n^{\prime}, k, 2 t+1\right) t$-EC codes and appending a tail of length $r$ such that the code can satisfy the conditions for $t$-EC/AUED code, where $k$ is the number of information bits. The overall code length of $t$-EC/AUED codes in [Bläum89] is $n=n^{\prime}+r$, and the number of redundant bits is $n-k$. Generally, the tail is a function of the number of weight of the codewords in $t$ - EC code. Thus, by reducing the number of weight of the codewords, one can get better $t$-EC/AUED codes due to the small length $r$. Construction of [Bruck92] can be viewed as a modification of the construction in [Blaum89]. Several other significant systematic $t$-EC/AUED codes and more general $t$-EC/d-ED/AUED codes have been reported in [Bose85, Lin88, Nikol86, Ra089, Boinc90, Kundu90, Katti96a, Katti96b, Yang98]. In the following, the necessary and sufficient conditions for a code to be $t$-EC/d-ED/AUED are stated :

Theorem 6.2 [Rao89] A code $C^{*}$ can correct $t$ or fewer unidirectional errors, if and only if for all $X^{*}, Y^{*} \in C^{*}$

$$
\begin{aligned}
& \Delta\left(X^{*}, Y^{*}\right) \geq 2 t+1 \text { for } X^{*}, Y^{*} \text { an ordered pair } \\
& \Delta\left(X^{*}, Y^{*}\right) \geq t+1 \text { for } X^{*}, Y^{*} \text { unordered }
\end{aligned}
$$

Theorem 6.3 [Rao89] A code $C^{*}$ is $t$-EC-AUED if and only if

$$
N\left(X^{*}, Y^{*}\right) \geq t+1 \text { for all } X^{*}, Y^{*} \in C^{*} .
$$

Theorem 6.4 [Nikol91] A code $C^{*}$ is $t-E C-d-E D-A U E D$ if and only if for all distinct $X^{*}, Y^{*} \in C^{*}{ }^{\prime}$

$$
\begin{aligned}
& D\left(X^{*}, Y^{*}\right) \geq t+d+1 \\
& N\left(X^{*}, Y^{*}\right) \geq t+1
\end{aligned}
$$

$$
N\left(Y^{*}, X^{*}\right) \geq t+1
$$

The next section presents a simple method to construct a class of $t$-EC/d-ED/AUED codes, which employs simpler and faster encoding/decoding algorithm with lesser complexity.

The notations used in the subsequent Sections of this chapter and their meanings are given below :
$\mathrm{D}(\mathrm{C})$ : Minimum distance of the code $C$.
$N(X, Y):$ Number of $1 \rightarrow 0$ crossovers from $X$ to $Y$.
$\mathrm{D}(\mathrm{X}, \mathrm{Y})$ : Hamming distance between X and Y .
$W(X)$ : Weight or number of 1 's in $X$.
$\Delta(X, Y)=\max \{N(X, Y), N(Y, X)\}:$ asymmetric distance between $X$ and $Y$.
$\lfloor Z\rfloor$ : The largest integer less than or equal to $Z$.
$\lceil\mathrm{Z}\rceil$ : The smallest integer greater than or equal to Z .
$k$ : number of information bits.
$n: k$ number of information bits and parity check bits for $t$-EC/d-ED $(t<d)$ Code.
$n^{*}: n$ bit $t$-EC code and additional check bits for $t$-EC/d-ED/AUED code.

In the next sections of this chapter, the theory and design of both the schemes have been described.

### 6.2 Theory of $t$-EC/d-ED \& $t$-EC/d-ED/AUED Codes

Let C denote a binary linear systematic $t$ - error correcting $(n, k)$ code with $\mathrm{D}(\mathrm{C})$ $\geq t+d+1$ and $C^{*}$ be a systematic $\left(n^{*}, k\right) t$-EC/d-ED/AUED code. For a codeword $X \in C$, the codeword in the proposed $t$-EC/d-ED/AUED systematic code $C^{*}$ have the following form -

$$
\mathrm{X} X_{1} \lambda_{2} \lambda_{3} \cdots \lambda_{r} .
$$

In other words, each codeword of $C^{*}$ is formed by concatenating a codeword X of C with
$X_{1}, X_{2}, X_{3}, \cdots X_{r^{*}}$, where $X_{2}$ 's are check bits derived by using Berger's technique. The appended check bits are used to increase the crossover between two codewords. Some of the properties of $t$-EC/d-ED code have been established, which would provide the foundation for the proposed code.

Let $C_{2}$ be the set of all codewords of $C$ with exactly $\imath$ number of 1 's. It should be noted that some of the sets $C_{2}$ (e.g., $C_{1}, C_{2}, \cdots C_{t+d}$ ) are empty because they can not satisfy the minimum distance constraint. Example 6.1 noted below illustrates the sets $C_{2}$ for $(16,3) 2$-EC/5-ED code.

Example 6.1 Consider the $(16,3) 2-E C / 5-E D$ code $^{1}$ with $D(C)=8$. It will be partitioned into subsets $C_{0}, C_{8}, C_{10}$ and $C_{14}$ as shown in Table 6.1.

Table 6.1: (16,3) 2-EC/5-ED CODE

| infor. <br> bits | check <br> bits | in <br> $C_{2}$ |
| :---: | :---: | :---: |
| 000 | 0000000000000 | $C_{0}$ |
| 001 | 1111110000001 | $C_{8}$ |
| 010 | 0001111110001 | $C_{8}$ |
| 011 | 1110001110000 | $C_{8}$ |
| 100 | 0000001111111 | $C_{8}$ |
| 101 | 1111111111110 | $C_{14}$ |
| 110 | 0001110001110 | $C_{8}$ |
| 111 | 1110000001111 | $C_{10}$ |

Lemma 6.1 [Nikol91] Let $C$ be a parity check code with minimum Hamming distance $D(C)=t+d+1$, where $d \geq t$. If $X, Y \in C, X \neq \mathrm{Y}$ and $W(X)-W(Y)=q \geq 0$ then $N(X, Y) \geq$ $t+1$ and $N(Y, X) \geq \max \{0, t+1-\lceil(q-(d-t)) / 2\rceil\}$.

Theorem $6.5 \forall Y \in C_{\imath}$ and $X \in C_{2+q}$, the folloming equality holds:

$$
N(X, Y)-N(1 ; X)=q
$$

Proof: There are at least $q$ bits where $X$ has a 1 but $Y^{\prime}$ has 0 . Let $Y^{\prime}$ and $X^{\prime}$ be the bit

[^0]strings obtained by removing those particular $q$ bits from the respective strings. Hence, $W\left(X^{\prime}\right)$ and $W\left(Y^{\prime}\right)$ have the same value. So change in bit positions of $X^{\prime \prime}$ and $Y^{\prime}$ occur pairwise, i.e.
$$
N\left(X^{\prime}, Y^{\prime}\right)=N\left(Y^{\prime}, X^{\prime}\right)
$$

Hence, $N(X, Y)=N\left(X^{\prime}, Y^{\prime}\right)+q$ and $N(Y, X)=N\left(Y^{\prime}, X^{\prime}\right)$
$\Longrightarrow N(X, Y)-N(Y, X)=q$
Corollary 6.1 $D(X, Y)+q$ is always even.
Proof :

$$
\begin{aligned}
D(X, Y)+q & =N(X, Y)+N(Y, X)+q \\
& =N\left(X^{\prime}, Y^{\prime}\right)+N\left(Y^{\prime}, X^{\prime}\right)+q+q \\
& =2 N\left(X^{\prime}, Y^{\prime}\right)+2 q \\
& =2\left(\left(N\left(X^{\prime}, Y^{\prime}\right)+q\right)\right.
\end{aligned}
$$

From the theorem 6.586 .1 , the following fundamental relations for $t$ - $\mathrm{EC} / \mathrm{d}$-ED code are obtained :
a) For $q=0$
$\mathrm{D}(\mathrm{X}, \mathrm{Y}) \geq t+d+1$ and $d>t$
Hence from theorem 6.5, we get

$$
\begin{equation*}
N(\mathrm{X}, \mathrm{Y})=\mathrm{N}(\mathrm{Y}, \mathrm{X}) \geq t+1 \tag{6.5}
\end{equation*}
$$

b) For $1 \leq q \leq t+d+1$,

1) if $t+d$ is even
I) if $q$ is odd then as per corollary 6.1
$\mathrm{D}(\mathrm{X}, \mathrm{Y})$ is also odd i.e. $\mathrm{D}(\mathrm{X}, \mathrm{Y}) \geq t+d+1$.
Hence from theorem 6.5, we get

$$
\mathrm{N}(\mathrm{X}, \mathrm{Y}) \geq t+1+(q-1+d-t) / 2 \& \mathrm{~N}(\mathrm{Y} . \mathrm{X}) \geq t+1-(q+1-(d-t)) / 2
$$

II) if $q$ is even then as per corollary 6.1
$\mathrm{D}(\mathrm{X}, \mathrm{Y})$ is even i.e. $\mathrm{D}(\mathrm{X}, \mathrm{Y}) \geq t+d+2$
Hence from theorem 6.5, we get

$$
\mathrm{N}(\mathrm{X}, \mathrm{Y}) \geq t+1+(q+(d-t)) / 2 \& \mathrm{~N}(\mathrm{Y}, \mathrm{X}) \geq t+1-(q-(d-t)) / 2
$$

2) if $t+d$ is odd
I) if $q$ is odd then as per corollary 6.1
$\mathrm{D}(\mathrm{X}, \mathrm{Y})$ is also odd i.e. $\mathrm{D}(\mathrm{X}, \mathrm{Y}) \geq t+d+2$.
Hence from theorem 6.5, we get

$$
\mathrm{N}(\mathrm{X}, \mathrm{Y}) \geq t+1+(q+(d-t)) / 2 \& \mathrm{~N}(\mathrm{Y}, \mathrm{X}) \geq t+1-(q-(d-t)) / 2
$$

II) if $q$ is even then as per corollary 6.1
$\mathrm{D}(\mathrm{X}, \mathrm{Y})$ is even i.e. $\mathrm{D}(\mathrm{X}, \mathrm{Y}) \geq t+d+1$
Hence from theorem 6.5, we get

$$
\mathrm{N}(\mathrm{X}, \mathrm{Y}) \geq t+1+(q-1+d-t) / 2 \& \mathrm{~N}(\mathrm{Y}, \mathrm{X}) \geq t+1-(q+1-(d-t)) / 2
$$

Hence,

$$
\begin{equation*}
\mathrm{N}(\mathrm{X}, \mathrm{Y}) \geq t+1+\lfloor(q+(d-t)) / 2\rfloor \& \mathrm{~N}(\mathrm{Y}, \mathrm{X}) \geq t+1-\lceil(q-(d-t)) / 2\rceil \tag{6.6}
\end{equation*}
$$

c) For $q \geq t+d+1$
$\mathrm{D}(\mathrm{X}, \mathrm{Y}) \geq q$.
Hence from theorem 6.5, we get

$$
\begin{equation*}
\mathrm{N}(\mathrm{X}, \mathrm{Y}) \geq t+d+1 \quad \text { and } \quad \mathrm{N}(\mathrm{Y}, \mathrm{X}) \geq 0 \tag{6.7}
\end{equation*}
$$

In the above discussions, some of the fundamental properties of $t$-EC/d-ED codes have been derived, which will be utilized in the next section to construct our $t$-EC/dED/AUED code.

### 6.3 Design of Systematic $t$-EC/d-ED/AUED Codes

Our objective is to construct a $t$-EC/d-ED/AUED code (i.e. $C^{*}$ ) from a given $t$-EC/dED code(i.e. C) by appending $r^{*}$ number of extra check bits. These $r^{*}$ check bits (i.e. $X_{1} X_{2} X_{3} \cdots X_{r}$.) can be divided into three subsets. First subset covers the last bit, second subset is the group of $p$-bits (where $t \leq p \leq 2 t$ ) referred to as 'last group' and third one is the subset consisting of groups each with $(t+1)$-bits ( $F \imath g$ 6.1). The 'last group' with $p$ bits can have values $\{11 \cdots 111,11 \cdots 110,11 \cdots 100, \cdots, 10 \cdots 000,00 \cdots 000\}$. The 'last group' of check bits can be derived by using a simple combinational logic circuit. The bit patterns in each of the remaining groups have only two values either
$11 \cdots 111$ or $00 \cdots 000$ - that is either all I's or all 0 's.


Figure 6.1: Circuit block diagram for mapping function

The Function 'map' noted below maps weight of a codeword, W(X) in $t$-EC/d-ED to $W^{\prime}(X)$, called effective weight which is equal to the weight of a codeword in $t$-EC. This is a many-to-one mapping function. We design this function by utilizing the results of the equation (65), (66) and (67). The table noted below specifies the value of $N(Y, X)$ for different ranges of $q$ both for $t$-EC and $t$-EC/d-ED codes.

Table 6.2: Values of $N(Y, X)$ for Different $q s$

| $t$-EC | $t$-EC/d-ED | $\mathrm{N}(\mathrm{Y}, \mathrm{X})$ |
| :---: | :---: | :---: |
| $q=0$ | $q=0$ | $\mathrm{~N}(\mathrm{Y}, \mathrm{X}) \geq t+1$ |
| $1 \leq q \leq 2 t$ | $1 \leq q \leq t+d$ | $t+1 \geq N(Y, X) \geq 1$ |
| $q \geq 2 t+1$ | $q \geq t+d+1$ | $N(Y, X) \geq 0$ |

Keeping the above discussions in view we formulate mapping function as noted below.

## Function $\operatorname{map}(\mathbf{u})$

$/^{*}$ It takes input $u$, weight of a codeword C in $t$-EC/d-Ed, $t$ (the number of errors to be corrected) and $d$ (the number of errors to be detected) */.
$/^{*}$ It returns effective weight, $u^{t}$ which corresponds to the weight of a codeword in $t$-EC. */ begin
$\mathrm{D} \leftarrow t+d+1 ;$ /* Hamming distance for $t$-EC/d-ED codes. */ $^{*}$
dist $\leftarrow 2 t+1 ; /^{*}$ Hamming distance for $t$-EC codes. */
$F_{\mathrm{d}} \leftarrow \mathrm{D} \bmod$ dist;
$I_{d} \leftarrow\lfloor\mathrm{D} /$ dist $\rfloor$;
$F_{t} \leftarrow\left(I_{d}+1\right) \times F_{d}-1 ;$
$I_{w} \leftarrow\lfloor\mathrm{u} / \mathrm{D}\rfloor ;$
$F_{w} \leftarrow u \bmod \mathrm{D} ;$
if ( $F_{w} \geq F_{t}$ ) then
$F \leftarrow\left\lfloor\left(F_{w}-F_{d}\right) / I_{d}\right\rfloor ;$
else $F \leftarrow\left\lfloor F_{w} /\left(I_{d}+1\right)\right\rfloor$;
$u^{\prime} \leftarrow I_{w} \times$ dist $+F ; /^{*}$ It is effective weight. */
return $\left(u^{\prime}\right)$;
end;
Table 6.2 illustrates the Function 'map' for $t=2$. For example, in case of $W(X)=11$, 12 and 13 (sixth row of Table 6.2 with $t=2$ and $d=8$ ) we get $W^{\prime}(X) s=5$.

Next, the algorithm find_no_of_bits will be discussed, which will operate on number of information and parity check bits (1.e.n). First it maps $n$ to its effective value by Function 'map' and gives number of appending bits (i.e. $r^{*}$ ). It also generates information regarding the number of groups and the number of bits in the last group, that is the value of $p$.

The Algorithm find_no_of_bits : This algorithm accepts ' $n$ ' (no. of bits in a Codeword $C$ ) as inputs and generates no_of_bits (appendable to the codeword $C$ to form $C^{*}$ ), 'last' (no. of bits in the last group) and 'max'(no. of groups in the third subset) as the outputs.

Step 1: Compute maximum number of different values that 'last-group' can have :
$t e m p_{-} t \leftarrow(2 t+1)$
Step 2: Find effective value of ' $n$ '
$n \leftarrow \operatorname{map}(n)$
Step 3: Compute ( $n+1 / 2$ ) and store its ceiling value in 'temp'
Step 4: Initialize $\max$ to 0
Step 5: Repeat while (temp >dzst)
Step 5.1 increment 'max'
Step 5.2 assign ceiling value of (temp/2) to temp
Step 6: Decrement 'temp' by 1 and store in 'last'
Step 7: Compute the number of bits to be appended -

$$
\text { no_of_bits } \leftarrow \max *(t+1)+\text { last }+1
$$

## Step 8: Return

The 'find_code' algorithm generates the extra check bits i.e. $X_{1} X_{2} \cdots X_{r}$. It accepts the number of 1 's of a codeword in $C$ as input and other information like 'last' and 'max' from the previous algorithm.

The 'find_code' Algorithm : This algorithm takes input 'no_of_one' (i.e. the number of 1's, $W(X)$ in the codeword $X \in C$ ), 'last' and 'max' as input from the previous algorithm. It uses an array 'group' to store the value of the appended $r$ *. The steps are

Step 1: Compute effective number of 1 's by using function 'map' and store in 'nó_of_one:

Step 2: For $\mathrm{i}=0$ to $\max +1$ initialize 'int' array with 0 . The 'int' array is used to store intermediate values of group of bits.

Step 3: Store- 'modulo-2' output of 'no_of _one' to int $[0]$ and floor-value of (no_of_one)/2 to 'no_of_one'

Step 4: Assign 'count' to 1
Step 5: Compute -
shift_val $\leftarrow$ no_of_one $\bmod ($ last +1$)$
no_of_one $\leftarrow\lfloor$ no_of_one/(last +1 ) $\rfloor$
Step 6: Repeat while no_of _one $>0$
Step 6.1: increment 'count' by 1
Step 6.2: compute int[count] $\leftarrow$ no_of _one $\bmod 2$
no_of_one $\leftarrow\lfloor$ no_of_one /2 $\rfloor$
Step 7: Increment max by 1 and store in 'count'
Step 8: Repeat while (count >1)
Step 8.1: if int[count] $=1$ assign ' $00 \ldots 000$ ' to 'group[count]' else assign '11...111' to 'group[count]'

Step 8.2: Decrement 'count' by 1
Step 9: Perform switch(shift_val) -
case shrft_val $=0: \operatorname{group}[1] \leftarrow{ }^{\prime} 111 \ldots 11$ '
case shrft_val $=1: \operatorname{group}[1] \leftarrow ' 111 \ldots 10^{\prime}$
case shift_val $=2:$ group $[1] \leftarrow ' 111 \ldots 00^{\prime}$
case shrft_val $=$ last-1 : group $[1] \leftarrow{ }^{\prime} 100 \ldots 00^{\prime}$
case shrft_val $=$ last $:$ group $[1] \leftarrow{ }^{\prime} 000 \ldots 00^{\prime}$
end_of_switch
Step 10: if $(\operatorname{int}[0]=1)$
group $[0] \leftarrow 0$;
else
group $[0] \leftarrow 1$;

Table 6.2 illustrates the Procedure 'find_code' for $r^{*}=6$ and $t=2$. For example, in case of $W(X)=11,12$ and 13 (sixth row of Table 6.2 with $d=8$ ) we get 111000 as the value of check bits. Table 6.3 shows $(22,3) 2-E C / 5-E D / A U E D$ codes generated by the proposed

Table 6.3: Output of the Function 'map' and Procedure 'find_code' for $r^{*}=6$ and $t=2$

| $X_{1} X_{2} \cdots X_{r}$. | $W^{\prime}(X)$ | W ( X ) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $d=4$ | $d=5$ | $d=6$ | $d=7$ | $d=8$ |
| 111111 | 0 | 0,1 | 0,1 | 0,1 | 0,1 | 0,1,2 |
| 111110 | 1 | 2,3 | 2,3 | 2.3 | 2,3 | 3,4 |
| 111101 | 2 | 4 | 4,5 | 4,5 | 4,5 | 5,6 |
| 111100 | 3 | 5 | 6 | 6.7 | 6,7 | 7.8 |
| 111001 | 4 | 6 | 7 | 8 | 8,9 | 9,10 |
| 111000 | 5 | 7,8 | 8,9 | 9,10 | 10,11 | 11,12,13 |
| 000111 | 6 | 9,10 | 10,11 | 11,12 | 12,13 | 14,15 |
| 000110 | 7 | 11 | 12,13 | 13.14 | 14,15 | 16,17 |
| 000101 | 8 | 12 | 14 | 15.16 | 16,17 | 18,19 |
| 000100 | 9 | 13 | 15 | 17 | 18,19 | 20,21 |
| 000001 | 10 | 14,15 | 16,17 | 18.19 | 20,21 | 22,23,24 |
| 000000 | 11 | 16,17 | 18,19 | 20.21 | 22.23 | 25,26 |

Table 6.4: 2-EC/5-ED/AUED codes

|  | $X$ | $X_{1-1} I_{2} \cdots X_{r}$ |
| :---: | :---: | :---: |
| 000 | 0000000000000 | 111111 |
| 001 | 1111110000001 | 111000 |
| 010 | 0001111110001 | 111000 |
| 011 | 1110001110000 | 111000 |
| 100 | 000000111111 | 111000 |
| 101 | 1111111111110 | 000101 |
| 110 | 0001110001110 | 111000 |
| 111 | 1110000001111 | 000111 |

scheme. We now prove that the above algorithm results in a $t$-EC/d-ED/AUED codes $C^{*}$. Let ( $\mathrm{X}, X_{1}, X_{2}, \cdots X_{r^{*}}$ ) and ( $\mathrm{Y}, Y_{1}, Y_{2}, \cdots Y_{r^{*}}$ ) be two codewords in $C^{*}$ constructed using the above procedure. The $r^{*}$ check bits, as discussed earlier, are divided into thre' subsets. Let for a codeword $X^{*}$ in $C^{*}$ the subsets be denoted as $S_{1 x}, S_{2 x}$ and $S_{3 x}$. Tiu, subsets $S_{1 y}, S_{2 y}$ and $S_{3 y}$ are defined similarly for codeword $Y^{*} \in C^{*}$. Crossover between these three subsets of $Y^{*}$ with that of $X^{*}$ are denoted as:
$n_{1}=\mathrm{N}\left(S_{1 y}, S_{1 x}\right)=$ change in last bit from 1 to 0 , that is $n_{1}$ may have value 0 or 1 .

$$
n_{2}=\mathrm{N}\left(S_{2 y}, S_{2 x}\right)=m, \quad \text { Where } m= \begin{cases}W\left(S_{2 y}\right)-W\left(S_{2 x}\right), & \text { if } W\left(S_{2 y}\right)>W\left(S_{2 x}\right) \\ 0, & \text { otherwise }\end{cases}
$$

that is $n_{2}$ may have value $0,1,2, \cdots, p$. Let the number of groups in the third subset is $l$ (say). Then, $n_{3}=\mathrm{N}\left(S_{3 y}, S_{3 x}\right)=$ change in zero or more groups in the third subset from ( $t+1$ ) 1's to $(t+1) 0$ 's ; that is, $n_{3}$ may have value $0,(t+1), 2(t+1), \cdots, l(t+1)$.

Lemma 6.2 If $X \in C_{\imath+q}$ and $Y \in C_{\imath}$, then

Case (a) If $q=0$ then

$$
\begin{equation*}
N\left[\left(Y_{1}, Y_{2}, \cdots Y_{r^{*}}\right),\left(X_{1}, X_{2}, \cdots X_{r^{*}}\right)\right]=0 \tag{6.8}
\end{equation*}
$$

Case (b) If $1 \leq q \leq t+d$ then

$$
\begin{align*}
& q^{\prime}=\text { effective value.of } q= \begin{cases}\left\lfloor\left(q-F_{d}\right) / I_{d}\right\rfloor, & \text { if } q \geq F_{t} \\
\left\lfloor q /\left(I_{d}+1\right)\right\rfloor, & \text { otherwise }\end{cases} \\
& N\left[\left(Y_{1}, Y_{2}, \cdots Y_{r^{*}}\right),\left(X_{1}, X_{2}, \cdots X_{r^{*}}\right)\right\rfloor \geq\left\lceil q^{\prime} / 2\right\rceil \tag{6.9}
\end{align*}
$$

Case (c) If $q \geq t+d+1$ then

$$
\begin{equation*}
N\left[\left(Y_{1}, Y_{2}, \cdots Y_{r} \cdot\right),\left(X_{1}, X_{2}, \cdots X_{r} \cdot\right)\right] \geq t+1 \tag{6.10}
\end{equation*}
$$

Proof: Let $N_{y x}=N\left[\left(Y_{1}, Y_{2}, \cdots Y_{r}\right),\left(X_{1}, X_{2}, \cdots X_{r} \cdot\right)\right]$. Here $W(X)=i+q$ and $W\left(Y^{\prime}\right)=i$, $\imath^{\prime}$ is effective value of $i$.

Case (a) If $q=0$ then $X$ and $Y$ are in the same set which gives $n_{1}=n_{2}=n_{3}=0$.
So $N_{y x}=n_{1}+n_{2}+n_{3}=0$.
Case (b) If $1 \leq q \leq t+d$ then $X$ and $Y$ are in different sets. So as per the Function 'map':

$$
q^{\prime}=\text { effective value of } q= \begin{cases}\left\lfloor\left(q-F_{d}\right) / I_{d}\right\rfloor, & \text { if } q \geq F_{t} \\ \left\lfloor q /\left(I_{d}+1\right)\right\rfloor, & \text { otherwise }\end{cases}
$$

Now according to the algorithm 'find_code':

1) for $q^{\prime}$ odd,

$$
n_{2} \geq \begin{cases}\left(q^{\prime}+1\right) / 2, & \text { where } n_{1}=n_{3}=0 \text { and } i^{\prime} \text { is odd } \\ \left(q^{\prime}-1\right) / 2, & \text { where } n_{1}=1, n_{3}=0 \text { and } \imath^{\prime} \text { is even }\end{cases}
$$

and $n_{3} \geq(t \div 1)$,
where $n_{2}=0, i^{\prime}$ is odd or even and $n_{1}= \begin{cases}0, & \text { for } q^{\prime}=1 \\ 0 \text { or } 1, & \text { for } q^{\prime}>1\end{cases}$

$$
\text { So } \dot{N}_{y x}=n_{1}+n_{2}+n_{3} \geq\left(q^{\prime}+1\right) / 2
$$

2) for $q^{\prime}$ even.
$n_{2} \geq q^{\prime} / 2$, where $n_{3}=0, n_{1}$ is 0 or 1 and $\imath^{\prime}$ is odd or even
$n_{3} \geq(t+1)$, where $n_{2}=0, n_{1}$ is 0 or 1 and $\imath^{\prime}$ is odd or even
So, $N_{y z}=n_{1}+n_{2}+n_{3} \geq \boldsymbol{q}^{\prime} / 2$
Hence, $N_{y x}=n_{1}+n_{2}+n_{3} \geq\left\{q^{\prime} / 2\right\rceil$.
Case (c) If $q \geq t+d+1$ then $X$ and $Y$ are also in different set So according to Function 'map':

$$
q^{\prime} \geq 2 t+1
$$

Then as per the algorithm 'find_code':

$$
n_{2} \geq \begin{cases}t+1, & \text { where } n_{1}=n_{3}=0, q^{\prime} \text { is odd and } \imath^{\prime} \text { is odd } \\ t, & \text { where } n_{1}=1, n_{3}=0, q^{\prime} \text { is odd and } \imath^{\prime} \text { is even } \\ t+1, & \text { where } n_{2}=0, n_{1} \text { is } 0 \text { or } 1, q^{\prime} \text { is even and } \imath^{\prime} \text { is odd or cven }\end{cases}
$$

and
$n_{3} \geq(t+1)$, where $n_{2}=0, n_{1}$ is 0 or $1, t^{\prime}$ is odd or even and $q^{\prime}$ is odd or even So $N_{y x}=n_{1}+n_{2}+n_{3} \geq t+1$.

Theorem 6.6 : The code $C^{*}$ constructed using the procedure find_code is a $t$ - $E C / d$ ED/AUED code.
Proof: As per the theorem 6.4, we only need to show that
$\forall X^{*}, Y^{*} \in C^{*} \mid X^{*} \neq Y^{*}$,

$$
N\left(X^{*}, Y^{*}\right) \geq t+1
$$

Consider $X \in C_{\imath+q}$ and $Y \in C_{\imath}$. Three different cases need to be considered

> Case a) $q=0$
> from (1) and (4), we obtain
> $N\left(X^{*}, Y^{*}\right) \geq N(X, Y) \geq t+1$
> and $N^{*}\left(Y^{*}, X^{*}\right) \geq N(Y, X) \geq t+1$

Case b) $1 \leq q \leq t+d$
As per Function 'map' $0 \leq q$ ' $\leq 2 t$
from (2) and (5), we get
$N\left(X^{*}, Y^{*}\right) \geq N(X, Y) \geq t+1$ and
$N\left(Y^{*}, X^{*}\right)=N(Y, X)+N\left[\left(Y_{1}, Y_{2}, \cdots Y_{r}\right),\left(X_{1}, X_{2}, \cdots X_{r^{*}}\right)\right]$
$\geq t+1-\lceil(q-(d-t)) / 2\rceil+\left\lceil q^{\prime} / 2\right\rceil$
2.e., $N\left(Y^{*}, X^{*}\right) \geq t+1$.

Case c) $q \geq t+d+1$
from (3) and (6) we get
$N\left(X^{*}, Y^{*}\right) \geq t+1$
and $N\left(Y^{*}, X^{*}\right)=N(Y, X)+N\left[\left(Y_{1}, Y_{2}, \cdots Y_{r}\right),\left(X_{1}, X_{2}, \cdots X_{r}\right)\right] \geq 0+t+1$
ı.e., $N\left(Y^{*}, X^{*}\right) \geq t+1$.

Hardware implementation :
The algorithm 'find_code' ensures that encoding of information bits in one of the $t$ -EC/d-ED/AUED codes is straight forward and simple. The circuit consists of a $t$-error correcting/d-error detecting parity check code encoder and another circuit for calculating
the values of $X_{1} X_{2} \cdots X_{\tau^{*}}$. The values of $r^{*}$-bits depend only. on the number of 1's in X , $W(X)$. Berger code generator can be used to compute $W(X)$. The circuit for generation of $r^{*}$ check bits accepts $\mathrm{W}(\mathrm{X})$ as the input. It can be implemented in two ways.
I) Using combinational circuit : The algorithm 'find_code' calls Function 'map'. So, we divide our encoding scheme into two parts. First part, Function 'map' takes $W(X)$ as input and produces $W^{\prime}(X)$, the effective value of $W(X)$ as output. Second part, the'find_code' algorithm generates $r^{*}$ check bits with $W^{\prime}(X)$ as input.
(a) Part 1: Here we have designed the Function 'map'. In this logic $F_{t}, F_{d}$ and $I_{d}$ are fixed for a given value of $t$ and $d$. So this circuit consists of one adder, one subtracter, one mod- $(t+d+1)$ counter, one $(2 t+1)$ multipher, one comparator, one mod- $I_{d}$ divider, one mod- $\left(I_{d}+1\right)$ divider and one 2:1 MUX. The complete circuit is shown in Fig 6.1. The size of these components and delay of the circuit depend on the values of $t, d$ and $k$.
(b) Part 2: This part realizes the algorithm 'find_code'. It generates $r^{*}$ check bits, which are partitioned into three subsets. A faster implementation circuit using a high speed array divider circuit is shown in 6.2. The LSB of $W^{\prime}\left(X^{\prime}\right)$ is inverted to generate last group of single bit, i.e. $S_{1 x}$. The remanning bits $W^{\prime}(X)$ are fed into a high speed $\bmod (p+1)$ divider circuit as dividend, D (The $p$ is nothing but last mentioned in the function) The 'remainder' output of the divider, i.e. R is fed into a Combinational Logic Circuit to derive the second subset, $S_{2 x}$, i.e. the 'last group'. Every bit of the divider output 'quotient', Q is inverted to generate the bits of each group (i.e. all 0 's or all 1's) of third subset, $S_{3 x}$. The size and delay of the circuit mainly depends on the size of the divider dictated by the value of $t$ and $k$.
II) Using ROM : Computation of the check bits of $X_{1} X_{2} \cdots X_{r}$. can also be implemented using a ROM (or a RAM) which accepts the value of $W(X)$ as address and the contents of this address are the values of $r^{*}$-bits. $\mathrm{W}(\mathrm{X}) \leq n$, thus a ROM of $n+1$ words, is sufficient. For example, for a parity check code C with $n=127$, a ROM of 128 words is enough. From Table 6.7 we can find that the number of extra check bits necessary for $d=8$ is 21 . Thus, we need a $128 \times 21$ bit ROM. Now according to our code construction method, except the last group and last bit all other groups has a property that in each group all bits have same value i.e. 0 or 1. Therefore, instead of storing $(t+1)$ bits, we can store 1 bit for each of these


Figure 6.2: Faster Circuit Block Diagram for generation of $\mathrm{X}_{1} \mathrm{~s}$
groups in ROM. Hence, word length of the ROM gets reduced significantly. Thus, instead of $128 \times 21$ bit ROM, we need a $128 \times 9$ bit ROM. Further reduction can be obtained if we substitute the ROM with a PLA in order to take into account the fact that many different ROM locations contain identical words. Hence, the hardware implementation of the proposed scheme is significantly lesser than other codes proposed in literature. Table 6.9 shows the reduction achieved for ROM word size.

### 6.3.1 Error Detection/Correction Algorithm for the $t$-EC/dED/AUED Codes

Let $Q=X X_{1} X_{2} X_{3} \cdots X_{r}$. be an error free codeword in the proposed $t$-EC/ $d$-ED/AUED code;
$Q^{\prime}=X^{\prime} X_{1}^{\prime} X_{2}^{\prime} X_{3}^{\prime} \cdots X_{\tau^{*}}^{\prime}$ be the received word with some errors in Q ;
$Q^{\prime \prime}=X^{\prime \prime} X_{1}^{\prime \prime} X_{2}^{\prime \prime} \cdots X_{r^{\prime}}^{\prime \prime}$ be the derived codeword from $Q^{\prime}$.

## Error Detection/Correction Algorithm :

Step 1 : Compute the syndrome $S$ of $X^{\prime}$ in the parity check code. Let $S$ corresponds to $g$ multiplicity error. If $g>t$ then the error is only detectable and stop. While for $g \leq t$, correct $X^{\prime}$ using the correction procedure in the parity check code obtaining $X^{\prime \prime}$ as the resulting word.

Step 2 : Compute the values of $r^{*}$-bits which correspond to $X^{\prime \prime}$. So, $Q^{\prime \prime}=$ $X^{\prime \prime} X_{1}^{\prime \prime} X_{2}^{\prime \prime} \cdots X_{r}^{\prime \prime}$. If $\mathrm{D}\left(Q^{\prime}, Q^{\prime \prime}\right) \leq t$, then the word $Q^{\prime \prime}$ is the correct codeword in $C^{*}$ and stop, else detectable error (i.e. unidirectional) with multiplicity greater then $t$ has occurred.

The decoding algorithm of the $t$-EC/d-ED/AUED code has same order of complexity as that of the $t$-EC/d-ED $(n, k)$ code C. Example 6.2 illustrates the error detection and correction steps.

Example 6.2 We consider the 2-EC/5-ED/AUED code for the (16,3) 2-EC/5-ED code of Example 6.1. The parity check matrix $H$ corresponding to the generator matrix $G$
is given by,

$$
H=\left[\begin{array}{llllllllllllllll}
0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 1 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\
1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\
1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\
1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\
1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\
1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\
1 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1
\end{array}\right]
$$

Consider the following codeword belonging to the above mentioned $2-\mathrm{EC} / 5-\mathrm{ED} / \mathrm{AUED}$ code

$$
Q=\underbrace{1000000001111111}_{X} \underbrace{111000}_{X_{i}}
$$

a) Suppose that one symmetric error has occurred in the above codeword in position marked with ^, as shown below.

$$
Q^{\prime}=\underbrace{1 \hat{1} 0000000111111}_{X^{\prime}} \underbrace{1100}_{X_{i}^{\prime}} 000
$$

The working of the error correction/detection algorithm is presented below -
By step 1: We compute the syndrome $S$ of $X^{\prime}$ in the parity check code

$$
S=H \cdot X^{T T}=\left[\begin{array}{llllllllllll}
0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0
\end{array}\right]
$$

The syndrome $S$ is equal to the second column of the parity check matrix $H$. We conclude that a single error has occurred in the second position of $X^{\prime}$. The error is corrected and resulting word is $X^{\prime \prime}=1000000001111111$
By step 2 : We consider the value of $X_{2}^{\prime \prime}$ which corresponds to $X^{\prime \prime}$. Since $W\left(X^{\prime \prime}\right)=8$, as per the algorithm find_code, $X_{2}^{\prime \prime}=111000$

Then,

$$
Q^{\prime \prime}=\underbrace{1000000001111111}_{X^{\prime \prime}} \underbrace{111000}_{X_{2}^{\prime \prime}}
$$

Since $\mathrm{D}\left(Q^{\prime}, Q^{\prime \prime}\right)=2 \leq t=2$, the word $Q^{\prime \prime}$ is the correct word $Q$.
b) Next, we consider the occurrence of a symmetric error with multiplicity greater than one in the same word Q . Let the received word be

$$
Q^{\prime}=\underbrace{\hat{0} 0 \hat{1} 00 \hat{1} 0001 \hat{0} 11111}_{X^{\prime}} \underbrace{1110 \hat{1} 0}_{X_{1}^{\prime}}
$$

By step 1: We compute the syndrome $S$ of $X^{\prime}$ in the parity check code

$$
\left.S=H \cdot X^{T}=\left[\begin{array}{llllllllllll}
1 & 1 & 0 & 1 & 1 & 1 & 1 & 0 & 1 & 1 & 1 & 1
\end{array}\right]\right]^{T}
$$

Since the syndrome is not equal to a column of $H$ or to the sum of two columns of $H$, more than two errors have occurred in $X^{\prime}$ and hence in $Q^{\prime}$.
Therefore, the error is detected in the received codeword.
c) Finally, we consider the occurrence of an unidirectional error with multiplicity greater than one in the same word $Q$. Let the received word be

$$
Q^{\prime}=\underbrace{10000000 \hat{0} \hat{0} \hat{0} \hat{0} \hat{0} \hat{0} \hat{0}}_{X^{\prime}} \underbrace{\hat{0} \hat{0} 1000}_{X_{i}^{\prime}}
$$

By step 1: We compute the syndrome $S$ of $X^{\prime}$ in the parity check code

$$
S=H \cdot X^{r T}=\left[\begin{array}{llllllllllll}
0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1
\end{array}\right]
$$

The syndrome $S$ is equal to the first column of the parity check matrix $H$. We conclude that a single error has occurred in first position (i.e. MSB) of $X^{\prime}$. The error is corrected and the resulting word is $X^{\prime \prime}=0000000000000000$
By step 2: We compute the value of $X_{2}^{\prime \prime}$ which corresponds to $X^{\prime \prime}$. Since $\mathrm{W}(\mathrm{X})=0$, as per the algorithm find_code, $X_{2}^{\prime \prime}=111111$
Then,

$$
Q^{\prime \prime}=\underbrace{000000000000000}_{X^{\prime \prime}} \underbrace{111111}_{X_{i}^{\prime \prime}}
$$

Since $\mathrm{D}\left(Q^{\prime}, Q^{\prime \prime}\right)=6>t=2$ we conclude that only detectable error has occurred.

Table 6.5: Proposed 1-EC/d-ED/AUED Codes

|  | $n$ range |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: |
|  | $d=2$ | $d=3$ | $d=4$ | $d=5$ | $d=6$ |
| 2 | $1-5$ | $1-6$ | $1-7$ | $1-9$ | $1-10$ |
| 3 | $6-7$ | $7-9$ | $8-11$ | $10-13$ | $11-15$ |
| 4 | $8-10$ | $10-13$ | $12-15$ | $14-18$ | $16-21$ |
| 5 | $11-15$ | $14-19$ | $16-23$ | $19-27$ | $22-31$ |
| 6 | $16-21$ | $20-26$ | $24-31$ | $28-37$ | $32-42$ |
| 7 | $22-31$ | $27-39$ | $32-47$ | $38-55$ | $43-63$ |
| 8 | $32-42$ | $40-53$ | $48-63$ | $56-74$ | $64-85$ |
| 9 | $43-63$ | $54-79$ | $64-95$ | $75-111$ | $86-127$ |
| 10 | $64-85$ | $80-106$ | $96-127$ | $112-149$ | $128-170$ |
| 11 | $86-127$ | $107-159$ | $128-191$ | $150-223$ | $171-255$ |
| 12 | $128-170$ | $160-213$ | $192-255$ | $224-298$ | $256-341$ |

### 6.3.2 Experimental Results \& Comparison with Existing Codes

Number of extra check bits necessary for $t=1,2,3,4$ with different values of $d$ and difierent ranges of $n$ are shown in Table 6.4 to 6.7. Results show that information rate $\left(k / n^{*}\right)$ of the proposed code varies with $t$, the number of errors it can correct. From exhaustive simulation study we have observed that for a few cases the scheme noted in [Nikol91] needs lesser number of check bits. However, for higher values of $t(\geq 3)$. the proposed code has information rate higher than that of [Nikol91]. In case of ROM implementation, word length of ROM for this scheme is much less and reduction in word length varies with $k$ and $t$ as shown in Table 6.8. This table represents effective $t$-EC for a $t$-EC/d-ED code. The major contribution of the proposed scheme is that our encoding/decoding algorithms can be implemented with a simple and faster circuit structure

In the preceding sections (i.e. in Section 6.2 E 6.3), a new, generalised class of $t$ -EC/d-ED/AUED codes have been reported. The superiority of the codes is established by comparing it - with some similar type of popular codes. The various properties exhibited by the aforesaid class of codes, have been utilized to make the codes efficient and comparable to the existing codes. However, one important property i.e. every code is of even-weight, could not be utilized fully during construction of the codes. Next

Table 6.6: Proposed 2-EC/d-ED/AUED Codes

|  | $n$ range |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | :---: |
|  | $d=3$ | $d=4$ | $d=5$ | $d=6$ |  |
| 3 | $1-7$ | $1-8$ | $1-9$ | $1-10$ |  |
| 4 | $8-9$ | $9-11$ | $10-13$ | $11-14$ |  |
| 5 | $10-11$ | $12-13$ | $14-15$ | $15-17$ |  |
| 6 | $12-14$ | $14-17$ | $16-19$ | $18-21$ |  |
| 7 | $15-19$ | $18-22$ | $20-25$ | $22-28$ |  |
| 8 | $20-23$ | $23-27$ | $26-31$ | $29-36$ |  |
| 9 | $24-28$ | $28-34$ | $32-38$ | $37-43$ |  |
| 10 | $29-38$ | $35-45$ | $39-51$ | $44-57$ |  |
| 11 | $39-47$ | $46-55$ | $52-63$ | $58-71$ |  |
| 12 | $48-57$ | $56-67$ | $64-77$ | $72-86$ |  |
| 13 | $58-76$ | $68-89$ | $78-102$ | $87-115$ |  |
| 14 | $77-95$ | $90-111$ | $103-127$ | $116-143$ |  |
| 15 | $96-115$ | $112-134$ | $128-153$ | $144-172$ |  |

Table 6.7: Proposed 3-EC/d-ED/AUED Codes

|  | $n$ range |  |  |  |
| ---: | ---: | ---: | ---: | ---: |
|  | $d=4$ | $d=5$ | $d=6$ | $d=7$ |
| 4 | $1-9$ | $1-10$ | $1-11$ | $1-12$ |
| 5 | $10-11$ | $11-13$ | $12-15$ | $13-16$ |
| 6 | $12-13$ | $14-15$ | $16-17$ | $17-19$ |
| 7 | $14-15$ | $16-17$ | $18-19$ | $20-21$ |
| 8 | $16-18$ | $18-21$ | $20-23$ | $22-25$ |
| 9 | $19-22$ | $22-25$ | $24-28$ | $26-31$ |
| 10 | $23-27$ | $26-31$ | $29-35$ | $32-38$ |
| 11 | $28-31$ | $32-35$ | $36-39$ | $39-43$ |
| 12 | $32-36$ | $36-41$ | $40-46$ | $44-51$ |
| 13 | $37-45$ | $42-51$ | $47-57$ | $52-63$ |
| 14 | $46-54$ | $52-61$ | $58-68$ | $64-75$ |
| 15 | $55-63$ | $62-71$ | $69-79$ | $76-87$ |
| 16 | $64-73$ | $72-82$ | $80-91$ | $88-100$ |
| 17 | $74-91$ | $83-103$ | $92-115$ | $101-126$ |
| 18 | $92-109$ | $104-123$ | $116-137$ | $127-151$ |
| 19 | $110-127$ | $124-143$ | $138-159$ | $152-175$ |

Table 6.8: Proposed 4-EC/d-ED/AUED Codes

|  | $n$ range |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: |
| $r^{*}$ | $d=4$ | $d=5$ | $d=6$ | $d=7$ | $d=8$ |
| 5 | $1-11$ | $1-12$ | $1-13$ | $1-14$ | $1-15$ |
| 6 | $12-13$ | $13-15$ | $14-17$ | $15-18$ | $16-19$ |
| 7 | $14-15$ | $16-17$ | $18-19$ | $19-21$ | $20-23$ |
| 8 | $16-17$ | $18-19$ | $20-21$ | $22-23$ | $24-25$ |
| 9 | $18-19$ | $20-21$ | $22-23$ | $24-25$ | $26-27$ |
| 10 | $20-22$ | $22-25$ | $24-27$ | $26-29$ | $28-31$ |
| 11 | $23-26$ | $26-29$ | $28-32$ | $30-35$ | $32-38$ |
| 12 | $27-31$ | $30-34$ | $33-37$ | $36-40$ | $39-43$ |
| 13 | $32-35$ | $35-39$ | $38-43$ | $41-47$ | $44-51$ |
| 14 | $36-39$ | $40-43$ | $44-47$ | $48-51$ | $52-55$ |
| 15 | $40-44$ | $44-49$ | $48-54$ | $52-59$ | $56-63$ |
| 16 | $45-53$ | $50-59$ | $55-65$ | $60-70$ | $64-75$ |
| 17 | $54-62$ | $60-69$ | $66-75$ | $71-81$ | $76-87$ |
| 18 | $63-71$ | $70-78$ | $76-85$ | $82-92$ | $88-99$ |
| 19 | $72-79$ | $79-87$ | $85-95$ | $93-103$ | $100-111$ |
| 20 | $80-88$ | $88-97$ | $96-106$ | $104-115$ | $112-124$ |
| 21 | $89-106$ | $98-117$ | $107-128$ | $116-139$ | $125-150$ |

Table 6.9: ROM Word-length of the Proposed Code with Effective $t$-EC Code

|  | Word length of ROM (in bits) our proposed scheme |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $t=1$ |  | $t=2$ |  | $t=3$ |  | $t=4$ |  | $t=5$ |  |
|  | reqd. | gain | reqd. | gain | reqd. | gain | reqd. | gain | reqd. | gain |
| 2 | 2 | 0 | - | - | - | - | - | - | - | - |
| 3 | 3 | 0 | 3 | 0 | - | - | - | - | - | - |
| 4 | 3 | 1 | 4 | 0 | - | - | - | - | - | - |
| 5 | 4 | 1 | 5 | 0 | 5 | 0 | 5 | 0 | - | - |
| 6 | 4 | 2 | 4 | 2 | 6 | 0 | 6 | 0 | 6 | 0 |
| 7 | 5 | 2 | 5 | 2 | 7 | 0 | 7 | 0 | 7 | 0 |
| 8 | 5 | 3 | 6 | 2 | 5 | 3 | 8 | 0 | 8 | 0 |
| 9 | 6 | 3 | 5 | 4 | 6 | 3 | 9 | 0 | 9 | 0 |
| 10 | 6 | 4 | 6 | 4 | 7 | 3 | 6 | 4 | 10 | 0 |
| 11 | 7. | 4 | 7 | 4 | 8 | 3 | 7 | 4 | 11 | 0 |
| 12 | 7 | 5 | 6 | 6 | 6 | 6 | 8 | 4 | 7 | 5 |
| 13 | 8 | 5 | 7 | 6 | 7 | 6 | 9 | 4 | 8 | 5 |
| 14 | 8 | 6 | 8 | 6 | 8 | 6 | 10 | 4 | 9 | 5 |
| 15 | 9 | 6 | 7 | 8. | 9 | 6 | 7 | 8 | 10 | 5 |
| 16 | 9 | 7 | 8 | 8 | 7 | 9 | 8 | 8 | 11 | 5 |
| 17 | 10 | 7 | 9 | 8 | 8 | 9 | 9 | 8 | 12 | 5 |
| 18 | 10 | 8 | 8 | 10 | 9 | 9 | 10 | 8 | 8 | 10 |
| 19 | 11 | 8 | 9 | 10 | 10 | 9 | 11 | 8 | 9 | 10 |
| 20 | 11 | 9 | 10 | 10 | 8 | 12 | 8 | 12 | 10 | 10 |
| 21 | 12 | 9 | 9 | 12 | 9 | 12 | 9 | 12 | 11 | 10 |

section presents a new, specific class of codes, which is designed by full exploitation of such even-weight properties (i.e. by using odd-weight-column matrix for the evenparity check) for the SEC (Single Error Correction) / DED (Double Error Detection) and AUED (All Unidirectional Error Detection) purposes. Such codes are very popular in commercial applications, (as stated in Section 6.1).

### 6.4 Construction of Systematic SEC-DED-AUED Codes

Let $C$ denote a binary linear systematic ( $n, k$ ) code with $\mathrm{D}(\mathrm{C}) \geq 4$ having parity-checkmatrix $H$ of odd weight column and $C^{*}$ be a systematic ( $n^{*}, k$ ) SEC-DED-AUED code. For a codeword $X \in C$, the codeword in the proposed SEC-DED-AUED systematic code $C^{*}$ have the following form

$$
X X_{1} X_{2} X_{3} \cdots X_{r}
$$

In other words, each codeword of $C^{*}$ is formed by concatenating a codeword X of C with $X_{1}, X_{2}, X_{3}, \cdots X_{r^{*}}$, where $X_{i}$ 's are check bits derived by using Berger's technique. The appended check bits are used to increase the crossover between two codeword. The proposed SEC-DED-AUED code (i.e. $C^{*}$ ) is constructed from the SEC-DED code(i.e. C) by appending $r^{*}$ number of extra check bits. These $r^{*}$ check bits (i.e. $X_{1} X_{2} X_{3} \cdots X_{r}$.) are divided into groups of 2 bits. Only the last group (i.e. $l_{g}$ ) is one or two bits in width depending on $r^{*}$ odd or even. Each other -bit group has only two values either 11 or 00 while ' $l_{g}^{\prime}$ ' can have values $\{1,0\}$ or $\{11,10,00\}$ depending on $r^{*}$ odd or even. The last group can be generated by using a combinational logic circuit. The procedure compute_code_size noted below operates on number of information and parity check bits (i.e.n) and gives number of appending bits (i.e. $r^{*}$ ). It also computes size information regarding the number of groups and the number of bits in $l_{g}\left(1 \leq l_{g} \leq 2\right)$.

## Procedure compute_code_size( $\mathrm{n}, l_{g}, n_{g}$, no_of_bits )

$/^{*}$ It takes input n , the number of bits in a codeword in C. ${ }^{*} /$
/* It gives output 'code_size' that are appended to the codeword in C to form $\mathrm{C}^{*} .^{*} /$
/* output ' $l_{g}$ ' gives number of bits in the last group. */
/* output ' $n_{g}$ ' gives the number of groups excepting the last one. */
begin

```
    temp_t \(\leftarrow 3 ; \quad / *\) maximum number of different values that last group of bits can have. */
    temp \(\leftarrow\lceil(\mathrm{n}+1) / 2\rceil\);
    \(n_{g} \leftarrow 0 ;\)
    while ( temp > temp_t)
        begin
            \(n_{g} \leftarrow n_{g}+1 ;\)
            temp \(\leftarrow\lceil\) temp/2].;
        end ;
    \(l_{g} \leftarrow\) temp \(-1 ;\)
    code_size \(\leftarrow n_{g} * 2+l_{g}\);
end;
```

The procedure noted below generates the extra check bits i.e. $X_{1} X_{2} \cdots X_{r}$. It accepts the number of 1 's of a codeword in C and other information like 'last' and ' max ' from the previous procedure as the input.

## Procedure compute_code( no_of_one, $l_{g}, n_{g}$ )

$/$ * It takes input no_ofone, the number of I's $\mathrm{W}(\mathrm{X})$ in the codeword $X \in C .{ }^{*} /$ $/^{*}$ Inputs ' $l_{g}$ ' and ' $n_{g}$ ' are outputs of the Procedure compute_code_size. */
$/^{*}$ Array 'gvalue' gives output of the procedure, i.e. value of the appended $r^{*}$ bits. */ begin
for $\mathrm{i}=0$ to $n_{g}-1$
$\operatorname{int}[\mathrm{i}] \leftarrow 0 ;$
/* The 'int' array is used to store intermediate values of group of bits. */
no_of_one $\leftarrow\lfloor$ ไno_of_one/2〕;
count $\leftarrow 0$;
shiftleft $\leftarrow$ no_of_one mod $\left(l_{g}+1\right)$;
$/^{*}$ input to circuit for generation of $l_{g} .{ }^{*} /$
no_of_one $\leftarrow\left\lfloor\right.$ no_of_one $\left./\left(l_{g}+1\right)\right\rfloor$;
Convert_bin ( no_of_one, max, int);
/* Convert 'no_of_one' to binary of 'max' bits and store in 'int' array. */
count $\leftarrow$ max-1;
while ( count $>=0$ )
begin
if $($ int $[$ count $]=1)$

Table 6.10: Output of the procedure compute_code for $r^{*}=4 \& 5$

| $r^{*}=4$ |  | $r^{*}=5$ |  |  |
| :---: | :---: | :---: | :---: | :---: |
| number of <br> 1's in C | $X_{1} X_{2} \cdots X_{r^{*}}$ | number of <br> 1's in C | $X_{1} X_{2} \cdots X_{r^{*}}$ |  |
| 0 | 1111 | 0 | 11111 |  |
| 2 | 1110 | 2 | 11110 |  |
| 4 | 1100 | 4 | 11001 |  |
| 6 | 0011 | 6 | 11000 |  |
| 8 | 0010 | 8 | 00111 |  |
| 10 | 0000 | 10 | 00110 |  |
|  |  | 12 | 00001 |  |
|  |  | 14 | 00000 |  |

```
            gvalue[count++]}\leftarrow00
        else
            gvalue[count++]}\leftarrow11
        count }\leftarrow\mathrm{ count - 1;
        end ;
if ( lg}=1) the
    if ( shiftleft = 1) then
        group[0] = 0;
    else
        group[0] = 1;
else
            begin
            case shiftleft = 0: group[0] = 11;
            case shiftleft = 1: group [0] = 10;
            case shiftleft = 2: group[0] = 00;
            endcase
        endif
```

end;

Table 6.9 illustrates output of the Procedure compute_code for $r^{*}=4$ and 5. Table 6.10 shows $(12,4)$ SEC-DED-AUED codes generated by the proposed scheme.

Table 6.11: (12,4)SEC-DED-AUED codes

| $X$ |  |
| :---: | :---: |
| 0000 | 0000 |
| 0001 | 1110 |
| 0010 | 0111 |
| 0011 | 1001 |
| 0100 | 1011 |
| 0101 | 0101 |
| 0110 | 1100 |
| 0111 | 1100 |
| 1000 | 1100 |
| 1100 | 1100 |
| 1001 | 0011 |
| 1010 | 1010 |
| 1011 | 0100 |
| 1100 | 0110 |
| 1101 | 1000 |
| 1110 | 0001 |
| 1111 | 1111 |$)$

We now show that the above procedure results in a SEC-DED-AUED $\operatorname{codes} C^{*}$. Let ( $\mathrm{X}, X_{1}, X_{2}, \cdots X_{r^{*}}$ ) and ( $\mathrm{Y}, Y_{1}, Y_{2}, \cdots Y_{r^{*}}$ ) be two codewords in $C^{*}$ constructed using the above procedure.

Lemma 6.3: If $X \in C_{\imath+k}$ and $Y \in C_{\imath}$,
case (a) if $k=0$ then

$$
\begin{equation*}
N\left[\left(Y_{1}, Y_{2}, \cdots Y_{r^{*}}\right),\left(X_{1}, X_{2}, \cdots X_{r^{\bullet}}\right)\right]=0 \tag{6.11}
\end{equation*}
$$

case (b) if $k=2$ then

$$
\begin{equation*}
N\left[\left(Y_{1}, Y_{2}, \cdots Y_{r^{*}}\right),\left(X_{1}, X_{2}, \cdots X_{r^{*}}\right)\right] \geq 1 \tag{6.12}
\end{equation*}
$$

case (c) if $k \geq 4$ then

$$
\begin{equation*}
N\left[\left(Y_{1}, Y_{2}, \cdots Y_{r} \cdot\right),\left(X_{1}, X_{2}, \cdots X_{r} \cdot\right)\right] \geq 2 \tag{6.13}
\end{equation*}
$$

Proof:

Case (a) If $k=0$ then $X$ and $Y$ are in the same set. Hence, $X_{1}$ and $Y_{2}$ are identical. So, $N\left[\left(Y_{1}, Y_{2}, \cdots Y_{r^{\bullet}}\right),\left(X_{1}, X_{2}, \cdots X_{r}\right)\right]=0$.

Case (b) If $k=2$ then $X$ and $Y$ are in two consecutive sets. According to the Procedure compute_code, crossover between $Y_{i}$ and $X_{i}$ is greater than or equal to one due to either a shift in last group of bit(s) or change of any other group of bits from 11 to 00.
i.e. $W\left(Y_{1}, Y_{2}, \cdots Y_{r^{*}}\right) \geq 1+W\left(X_{1}, X_{2}, \cdots X_{r^{*}}\right)$

Hence, $N\left[\left(Y_{1}, Y_{2}, \cdots Y_{r^{*}}\right),\left(X_{1}, X_{2}, \cdots X_{r} \cdot\right)\right] \geq 1$
Case (c) If $k \geq 4$ then $X$ and $Y$ are in different sets. According to Procedure compute_code, crossover between ( $Y_{1}, Y_{2}, \cdots Y_{r^{*}}$ ) and ( $X_{1}, X_{2}, \cdots X_{r^{*}}$ ) greater than or equal to two, since there is change of bits from ' 11 ' to ' 00 ' for one or more groups(i.e. two or more crossovers).
i.e. $W\left(Y_{1}, Y_{2}, \cdots Y_{r^{-}}\right) \geq 2+W\left(X_{1}, X_{2}, \cdots X_{r^{*}}\right)$

Hence, $N\left[\left(Y_{1}, Y_{2}, \cdots Y_{r^{*}}\right),\left(X_{1}, X_{2}, \cdots X_{r^{*}}\right)\right] \geq 2$
Theorem 6.7 : The code $C^{*}$ constructed using the procedure find_code is a SEC-DEDAUED code.
Proof: As per the theorem 6.4, it is only needed to show that
$\forall X^{*}, Y^{*} \in C^{*} \mid X^{*} \neq Y^{*}$, then

$$
N\left(X^{*}, Y^{*}\right) \geq 2
$$

Consider $X \in C_{2+k}$ and $Y \in C_{2}$. Three different cases are to be considered-

Case a) $k=0$
from (1) and (7), we obtain
$N\left(X^{*}, Y^{*}\right) \geq N(X, Y) \geq 2$
and $N\left(Y^{*}, X^{*}\right) \geq N(Y, X) \geq 2$.
Case b) $k=2$
from (2) and (8), we get,
$N\left(X^{*}, Y^{*}\right) \geq N(X, Y) \geq 2$
and $N\left(Y^{*}, X^{*}\right)=N(Y, X)+N\left[\left(Y_{1}, Y_{2}, \cdots Y_{r^{*}}\right),\left(X_{1}, X_{2}, \cdots X_{r^{*}}\right)\right] \geq 1+1$
i.e. $N\left(Y^{*}, X^{*}\right) \geq 2$.

Case c) $k \geq 4$

```
from (3) and (9) we get,
    \(N\left(X^{*}, Y^{*}\right) \geq 2\)
    and \(N\left(Y^{*}, X^{*}\right)=N(Y, X)+N\left[\left(Y_{1}, Y_{2}, \cdots Y_{r^{*}}\right),\left(X_{1}, X_{2}, \cdots X_{r^{*}}\right)\right] \geq 2\)
```


## The Proposed SEC-DED-AUED Implementation :

The Procedure 'compute_code' ensures that encoding of information bits in one of the SEC-DED-AUED codes is straight forward and simple. The encoder consists of a single error correcting and double error detecting parity check code encoder and a circuit for calculating the values of the check bits $X_{1} X_{2} \cdots X_{r}$. The values of $r^{*}$ check bits depend only on the number of I's in $\mathrm{X}, \mathrm{W}(\mathrm{X})$. Therefore, the circuit for generation of $r^{*}$ check bits accepts $\mathrm{W}(\mathrm{X})$ as the input. Berger code generator can be used to compute $\mathrm{W}(\mathrm{X})$. The circuit to generate values of $X_{1} X_{2} \cdots X_{r}$. can be implemented in two ways:
I) Faster Combinational Circuit-based Implementation (Fig 6.3 88 6.4):

As per the proposed encoding scheme the complexity in the circuit design depends on the value associated with the last group, i.e. $l_{g}$. In 6.3, the circuit for $l_{g}=1$ is presented. The LSB of $\lfloor W(X) / 2\rfloor$ is inverted to generate the last group of one bit, $X_{r}$. The other remaining bits of $\lfloor W(X) / 2\rfloor$ are similarly inverted to generate the remaining 2 -bit groups. In 6.4 , the circuit diagram for $l_{g}=2$ is presented. Here, a high speed Mod 3 divider circuit is used, which takes $\lfloor W(X) / 2\rfloor$ as input. The remainder output-' R ' is fed into a simple combinational logic circuit to generate the all possible 2-bit output (last group), i.e., $X_{r^{*}-1}$ and $X_{r^{*}}$. Every bit of the divider output quotient, i.e. Q is inverted to generate the other remaining 2-bit groups.
II) ROM-based Implementation : Calculation of the values of $X_{1} X_{2} \cdots X_{r} \cdot$ can also be implemented using a ROM (or a RAM) which accepts the value of $W(X)$ as address and the contents of this address are the values of $r^{*}$-bits. $\mathrm{W}(\mathrm{X}) \leq n$, and so a ROM with $n+1$ words will suffice. For a parity check code C with $n=255$, a ROM of 256 words is enough. From Table 6.11, it is clear that the number of extra check bits is 13 . Thus, a $256 \times 13$ bit ROM is required. Except the last group, all other groups has a property that each of the bits in a group has same value, either 0 or 1 . Therefore, instead of storing 2 bits, one can store 1 bit for each group in ROM. Hence, word length of the ROM gets reduced significantly. Thus,
instead of $256 \times 13$ bit ROM, a $256 \times 7$ bit ROM is required. Further reduction can be obtained if one substitute the ROM with a PLA in order to take into account the fact that many different ROM locations contan identical words.


Figure 6.3: Faster Circuit block diagram with $l_{g}=1$

### 6.4.1 Error Detection/Correction Method

Let, $Q=X X_{1} X_{2} X_{3} \cdots X_{r^{-}}$be an error free codeword in the proposed SEC-DED-AUED code,
$Q^{\prime}=X^{\prime \prime} X_{1}^{\prime} X_{2}^{\prime \prime} X_{3}^{\prime \prime} \cdot X_{r}^{\prime \prime}$. be the recerved codeword and
$Q^{\prime \prime}=X^{\prime \prime} X_{1}^{\prime \prime} X_{2}^{\prime \prime} \cdots X_{r}^{\prime \prime}$. be the derived codeword from $Q^{\prime}$.

Step 1: Compute the syndrome $S$ of $X^{\prime}$ in the parity check code. If syndrome $S$ have detectable symmetric error then write 'Detectable errors in codeword' and stop, else correct $X^{\prime}$ using the correction procedure in the parity check code obtaining $X^{\prime \prime}$ as the resulting word. Also, if there is no error in $X^{\prime}$ then take $X^{\prime \prime}=X^{\prime}$ as the resulting codeword.

Step 2: Compute the values of $r^{*}$-bits which correspond to $X^{\prime \prime}$. So, $Q^{\prime \prime}=$ $X^{\prime \prime} X_{1}^{\prime \prime} X_{2}^{\prime \prime} \cdots X_{r^{\prime}}^{\prime \prime}$. If $\mathrm{D}\left(Q^{\prime}, Q^{\prime \prime}\right) \leq 1$ then the word $Q^{\prime \prime}$ is a correct codeword in $C^{*}$ and stop, else a detectable error (i.e.unidirectional) with multiplicity greater then one has occurred.


Figure 6.4: Faster Circuit block diagram with $l_{g}=2$

Example 6.3 We consider the SEC-DED-AUED code of Example 6.1. The parity check matrix $H$ corresponding to the generator matrix G is given by,

$$
H=\left[\begin{array}{llllllll}
1 & 1 & 0 & 1 & 1 & 0 & 0 & 0 \\
1 & 0 & 1 & 1 & 0 & 1 & 0 & 0 \\
0 & 1 & 1 & 1 & 0 & 0 & 1 & 0 \\
1 & 1 & 1 & 0 & 0 & 0 & 0 & 1
\end{array}\right]
$$

consider the following codeword belonging to the above mentioned SEC-DED-AUED code

$$
Q=\underbrace{10001101}_{X} \underbrace{1100}_{X_{1}}
$$

a) Let us assume that one symmetric error has occurred in the above codeword in position marked with ${ }^{\wedge}$ in the received word noted below.

$$
Q^{\prime}=\underbrace{1 \hat{1} 001101}_{X^{\prime}} \underbrace{1100}_{X^{\prime}}
$$

By step 1: We compute the syndrome $S$ of $X^{\prime}$ in the parity check code

$$
S=H \cdot X^{T}=[1011]^{T}
$$

The weight of syndrome $S$ is odd and it is equal to the second column of the parity check matrix $H$. We conclude that a single error has occurred in the second position of $\lambda^{\prime}$. The error is corrected and resulting word is $X^{\prime \prime}=10001101$
By step 2: We consider the value of $X_{2}^{\prime \prime}$ which corresponds to $X^{\prime \prime}$. Since, $W\left(X^{\prime \prime}\right)=4$ we can find $X_{i}^{\prime \prime}$ by procedure find_code as $X_{2}^{\prime \prime}=1100$ Then,

$$
Q^{\prime \prime}=\underbrace{10001101}_{X^{\prime \prime}} \underbrace{1100}_{X_{2}^{\prime \prime}}
$$

Since, $\mathrm{D}\left(Q^{\prime}, Q^{\prime \prime}\right)=1$, the word $Q^{\prime \prime}$ is the correct word Q .
b) Next, let us consider the occurrence of a symmetric error with multiplicity two in the same word Q . Let, the received word be

$$
Q^{\prime}=\underbrace{10 \hat{1} 010001}_{X^{\prime}} \underbrace{1100}_{X_{1}^{\prime}}
$$

By step 1: We compute the syndrome $S$ of $X^{\prime}$ in the parity check code

$$
S=H \cdot X^{T}=[0011]^{T}
$$

Since, the weight of syndrome S is even and it is not equal to any column of $H$, so double error is detected in $X^{\prime}$ and hence in Q .
Therefore, the error is only detectable.
c) Finally, we consider the occurrence of an unidirectional error with multiplicity greater than two in the same word $Q$. Let the received word be

$$
Q^{\prime}=\underbrace{1000 \hat{0} \hat{0} 0 \hat{0}}_{X^{\prime}} \underbrace{10 \hat{0} 0}_{X^{\prime}}
$$

By step 1: We compute the syndrome S of $X^{\prime}$ in the parity check code

$$
S=H \cdot X^{\prime T}=[1101]^{T}
$$

Since, the weight of syndrome $S$ is odd and it is equal to the first column of the parity check matrix $H$, we conclude that a single error has occurred in first position of $X^{\prime}$. The error is corrected and the resulting word is

$$
X^{\prime \prime}=00000000
$$

By step 2: We compute the value of $X_{2}^{\prime \prime}$ which corresponds to $X^{\prime \prime}$. Since $W(X)=0$, as per the Procedure compute_code, $X_{2}^{\prime \prime}=1111$
Then,

$$
Q^{\prime \prime}=\underbrace{00000000}_{X^{\prime \prime}} \underbrace{1111}_{X_{i}^{\prime \prime}}
$$

Since, $\mathrm{D}\left(Q^{\prime}, Q^{\prime \prime}\right)=4$, we conclude that only detectable unidirectional error has occurred

### 6.4.2 Experimental Results and Comparison with Existing Codes

Experimental results and comparison with other codes (1.e. SEC-AUED codes) are tabulated in Tables 6.11, $6.12 \& 6.13$. Table 6.11 shows values of extra bits for different ranges of $k$. From a detail experimental study on different ranges of $k$, it is observed that only for higher values of $k$, the results cited in [Blaum89] may be better than ours. Further, the codes proposed in [Blaum89] is a SEC-AUED code and the encoding/decoding algorithms of [Blaum89] are more complex than those algorithms presented in this paper. The major advantage of the proposed scheme is that its encoding/decoding algorithm can be implemented with a simple and faster circuit. In case of ROM based implemen-

Table 6.12: Proposed SEC-DED-AUED codes

| k range | n range | $r^{*}$ (size) |
| ---: | ---: | ---: |
| $4-6$ | $8-11$ | 4 |
| $7-10$ | $12-15$ | 5 |
| $11-17$ | $16-23$ | 6 |
| $18-25$ | $24-31$ | 7 |
| $26-40$ | $32-47$ | 8 |
| $41-56$ | $48-63$ | 9 |
| $57-87$ | $64-95$ | 10 |
| $88-119$ | $96-127$ | 11 |
| $120-186$ | $128-195$ | 12 |
| $187-246$ | $196-255$ | 13 |

Table 6.13: Comparing the Results of [Nikol86] and [Blaum89] with Table 6.11

| $k$ range | $\begin{gathered} \hline \hline \text { SEC-AUED } \\ \text { codes } \end{gathered}$ |  |  |  | SEC-DED-AUEDcodes |  | gain in extra check bits over |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | given in [Nikol86] |  | given in [Blaum89] |  |  |  |  |  |
|  | $n$ range | $r^{*}$ | $n$ range | $r^{*}$ | $n$ range | $r^{*}$ | [Nikol86] | [Blaum89] |
| 8-10 | 12-14 | 6 | 12-14 | 6 | 13-15 | 5 | +1 | $+1$ |
| 12-17 | 17-22 | 8 | 17-22 | 7 | 18-23 | 6 | +2 | +1 |
| 19-25 | 24-30 | 8 | 24-30 | 8 | 25-31 | 7 | +1 | +1 |
| 27-40 | 33-46 | 10 | 33-46 | 8 | 34-47 | 8 | +2 | 0 |
| 42-56 | 48-62 | 10 | 48-62 | 9 | 49-63 | 9 | +1 | 0 |
| 65-87 | 72-94 | 12 | 72-94 | 10 | 73-95 | 10 | +2 | 0 |
| 88-119 | 95-126 | 12 | 95-126 | 10 | 96-127 | 11 | +1 | -1 |

tation, word-length of ROM for this scheme (tabulated in Table 6.13) is significant and the reduction in word-length varies with $k$.

### 6.5 Conclusion

In this chapter, two efficient schemes have been introduced to construct $t$-EC/ $d$ ED/AUED and SEC-DED-AUED systematic codes respectively. The major advantage of these codes are that they can be implemented with simple and faster hardware. In case of $t$-EC/ $d$-ED/AUED, the detailed experimental study reveals that the results noted in

Table 6.14: Reduction of ROM word length for the proposed code

|  | ROM Word length (in bits) |  |
| ---: | ---: | ---: |
| $r^{*}$ | reqd. | gain |
| 4 | 3 | 1 |
| 5 | 3 | 2 |
| 6 | 4 | 2 |
| 7 | 4 | 3 |
| 8 | 5 | 3 |
| 9 | 5 | 4 |
| 10 | 6 | 4 |
| 11 | 6 | 5 |
| 12 | 7 | 5 |
| 13 | 7 | 6 |

[Nikol91] are better than the proposed codes, only in a limited number of cases. However, for larger value of $t$, in the majority of cases, the proposed scheme needs lesser number of check bits. Similarly, in case of the SEC-DED-AUED codes, from an exhaustive experimental study on different ranges of $k$, it has been observed that only for higher values of $k$, the results noted in [Blaum89] are better. Further, the encoding/decoding algorithms presented in both the schemes are simpler than most of the existing schemes. In case of ROM based implementation, both the schemes significantly reduce the ROM word-length.

The study carried out so far and the schemes developed for authentication, data security and error correction/detection suggest that these could be applied appropriately to several application areas such as distributed database applications, authenticated ker exchange, etc (as discussed in Chapter 1). Some of the areas where these schemes also could be applied successfully are image and multimedia database applications. Such investigations and applications might lead to enhancement of knowledge not only in the areas of authentication, data security and error control coding, but also to look into the factors such as : design of appropriate means for representations e.g. data model, systems' architecture etc. The following chapters highlight the findings of such applications into the areas of hypermedia application development and image database systems design.

## Chapter 7

## RMDM and Its Drawbacks

### 7.1 Introduction

The investigations reported in the previous chapters (Chapters 2, 3,4,5 \& 6) indicated that one of the major applications of authentications, data security and error correction/detection schemes is in multimedia database. However, an integral and essential part of the multimedia database design is to model the real-world application domain in a conceptual manner using a suitable data model. A data model is an abstraction of a portion of real-world situation. It is a group of concepts that help us to specify the structure of a database and a set of associated operations for specifying retrieval and updates on the database [Hughe91]. Basically, one can have two types of data models: high level or conceptual or object-based data model, and low-level or physical or record-based data model. High level data models e.g. E-R model [Chen76] provides concepts that are close to the way many users perceive data, and it uses the concepts such as entities, attributes and relationships. Whereas, low-level data models e.g. Relational, Hierarchical or Network data models provide concepts that describe the detail of how data is stored in the computer. E-R model is popular and often used in representing database schema for any business and industrial database applications. However, with the enormous growth of database technology and in the context of several special database applications, such as C.AD/CAM, Cartographic, Geological, hypertext \& hypermedia applications, it has been observed that E-R model is not sufficient enough to model their complex objecttypes and association patterns, in a conceptual manner. In this background, several other semantical data models, including the Object-Oriented and Functional data models have been proposed to meet those complex modelling requirements. However, from
the experience it is felt that in the context of the hypermedia applications, which bear a peculiar behaviour, particularly from the navigational aspects, their modelling requirements demand a separate class of data models, which may be capable enough in modelling these complex navigational patterns for any scale of hypertext/hypermedia applications in a conceptual manner. RMDM (Relationship Management Data Model) [Isakw95] is one, which belongs to this class of data models and has been proposed for a class of hypermedia applications exhibiting regular and static structure and which require frequent updating due to its volatile nature of data. Apart from RMDM, several other data models for hypertext/hypermedia systems also have been proposed in this regards. Next subsection presents a brief review of the existing data models.

### 7.1.1 Reviewing Hypermedia

The terms "hypertext" and "hypermedia" are often used quite interchangeably. Hypertext in the strict sense only applies to text-based systems; hypermedia is sumply the extension of hypertext to include multimedia data. The invention of both the terms is credited to Ted Nelson in 1965. Nelson presented a rision of the type of knowledge management environment that hypertext can help to support. The inspirations behind his ideas were due to V. Bush and D. Englebart. Bush proposed à theoretical design for a system, which he called as Memex (Memory Extender) that is known as a hypertext system. Douglas Englebart is credited with the invention of word processing, screen windows and the mouse and thus inspiring the developments in graphical user interfaces that have taken place over the last twenty years. By the end of the 1980s, the state of the art in hypertext systems was best represented by intermedia, but the research community had recognized the need for a hypertext reference model for some while [Wendy96]. Campbell and Goodman [Cmpbl88] suggested a three layered model for hypertext systems essentially consists of the presentation level (user interface), the hypertext abstract machine (HAM) level (nodes and links) and the database level (storage, shared data, network access etc.). The HAM was used by both the Neptune and C.AD systems [Desle86] and the dynamic design [Biglw88] for providing the hypertext object layers. In December 1989, in the hypertext standardization workshop, conducted by NIST (National Instt of Standard and Technology), several new models were proposed. The standard that emerged was Dexter reference model ([Halas90, Halas94]). This model attempted to capture the important abstractions found in a range of hy-
pertext systems that existed at the time, such as Augmented, Intermedia, Hypercard, Hyperties, KMS, Neptune and Notecards, Sun's Link Service [Pearl89] etc. Like the HAM model, the Dexter model divides the hypertext systems into three layers. The runtime layer contains the basic hypertext functionality, the storage layer contains the network of link and nodes specifications that represent the structure of the particular hypertext. The within component layer is the content of the particular component, node, document or frame. Dexter sensibly made no attempt to model the structure of the component leaving this to other modelling tools such as ODA [Wendy96]. Gronbaek and Trigg [Grnbk92] criticized Dexter model and they pointed out that: (i) It should not possible with Dexter to create dangling links made for restrictive interfaces to link creation and addition; (ii) these are multiple orthogonal concepts directionality of links (such as the directionality of a 'supports' typed link and the direction of traversal) ; (iii) it is necessary to extend the Dexter model to support the long term transaction, locking and event notification so that a co-operative hypermedia systems could be designed.

Legett and Schnase [Leget94] point to the shortcomings of using Dexter as an interchange standard, particularly its incomplete specifications of multi-headed links, the problem with a dangling link creation when importing partial hypermedia and the failure of the model to distinguish between separate webs as implemented in Intermedia. They also point out that the model has no concept of the semantics of arrival and departure when following links and that the notion of the composites and their consistencies is complete, as also has been noted by others [Grnbk92]. They suggested that anchors belonging the link services domain rather than within the applications (or components) domains.

A further problem of the Dexter model is that it contains no specifications of how to deal with temporal event specifications, which is well covered by the Hytime standards [Wendy96], and partly for this reason it is probable that Hytime will be seen as a more complete hypertext interchange standard. In October, 1992 and in November 1993; two other workshops held with the motivations behind that the current generations of hypermedia systems would not scale to deal with very large information. Repositories such as those that would be found in digital libraries and the purpose was to separate the area of the research that concentrates on hypermedia systems implementation issues from other issues, such as user interfacesm, evaluations and usability studies. The area of concentrations were : models and architectures, node. link and structure management, version control, concurrency control, transaction management and notification control.

As an outcome, it was considered hypermedia systems architecture to consist of three layers : storage (that provides persistent storage for the data model abstractions (nodes, links, anchors, contexts, etc.)), hyperbase (that provides the hypermedia data model to the application) and application layer (contains typical applications such as text and graphics editors, mail tools and multimedia presentation tools). However, there was a majority agreement that the Dexter model could not provide the flexibility or richness required by the hypermedia community. In this background, several other systems have been evolved, such as : GMD-IPSI's CHS and CoVer [Schut90], SP3 and HB2 [Leget94, Kacmr91, Schns93a], ABC and DGS [Shklf93, Smith91], Hyperform [Wiil92], DHM [Grnbik92], DHT [Nol191], HB3 [Schns93b], Trellis [Stots89], HDM [Garzo93a], HDM2 [Garzo93b], RMDM [Isakw95] etc. HDM [Garzo93a] is appropriate for describing the structure of the application domain and HDM2 [Garzo93b] is a successor of it. HDM and HDM2, both describe representation schemes but provide little information on the procedures for using these representations in the design process; that is they do not describe a hypermedia design and development methodology. RMM [Isakw95] is an extension work of [Balas94], which focus on developing a graphical representation based step-by-step procedure for hypermedia design and development. RMM describes RMDM as an application data model which is the cornerstone of RMM methodology. The objective of the RMDM techniques is to represent data at a higher level of abstraction. It is basically an extension of the popular object-based E-R model where the narigation approach is based on the HDM and its successor, HDM2. The extended part of E-R modelling is very well defined and a strong set of modelling notations is provided. To study RMDM, several specific application domains have been selected for implementation. It has been observed that RMDM is not exactly fulfilling the implementation of some of those complex application domains. This chapter projects one of such applications where RMDM fails to express some of the situations conceptually. To overcome these drawbacks, some remedial suggestions have been put forth, which ultimately indicates towards extension of the present RMDM. The implementation results based on the extended RMDM also have been reported in this chapter. Next section discusses an example multimedia application to study the RMDM.

### 7.2 Multimedia Example : A Real Life Ecosystem

Several specific hypermedia application domains were chosen to investigate the expressiveness of RMDM. One of such applications is a real-life Ecosystem from Keoladeo National Park, Rajasthan, India [Shukl96]. A common nature of any ecosystem is that they undergo succession and aging process accompanied by significant changes in their structure and function. This natural process of succession could be accelerated by unusual changes in the environment due to which some of the species may die out or eliminated from the habitat. It leads to uncontrolled growth rate of a certain harmful species that had been otherwise kept in check by eliminated species. In the aquatic enrironment, a typical example of growth rate of noxious weeds (Eichhornia, Salvina), which is harmful to other species, has been pointed out by many investigators [Salim86] Similar situations also exist in the wetland area of Keoladeo National Park, at Bhataratpur (Rajasthan) in India where habitat is degrading due to uncontrolled growth of some wild grasses such as Paspalum Distichum. This leads to decrease in the growth rates of other valuable species (e.g. migration of Siberian Cranes, other birds, etc) which are unable to compete. To control the situation, it becomes very important for the ecologists to collect, store and present realistically - an up-to-date statistic of the huge number of raluable Species, Vegetations and other Ecological entities - their attributes and features, such that necessary preventive measures may be taken. Thus, it could be an ideal multimedia application to study the proposed RMDM data model. Besides, the other reasons behind the selection of this case for illustration are :

R1 It has numerous classes and sub-classes of entities, definable relations which exhibit a regular structure.

R2 It requires regular updating.
R3 It includes some recursive structure-based, generalized entities.

### 7.3 Modelling the Ecosystem using RMDM

RMDM is a hypermedia application data model that provides a language for describing the information objects and the navigation mechanisms of any regular and static
structure-based hypermedia application. To model the information about the application domain, RMDM provides three types of primitives: $E-R, R M D$ (Relationship Management Domain) and Access domain primitives. To represent and describe the physical or abstract ecological objects, e.g. species, vegetation etc. and their attributes as well as their associations among the entity types- the $E-R$ domain primitives can be used. Among the large set of attributes associated with an entity, for natural and practical representation, this model suggests to slice those attributes into several meaningful logical groups, which are here termed as RMDM Slices. To access those slices, the RMD domain primitives are provided. To navigate through and access the slices, RMDM supports six types of access primitives, such as : untdirectıonal link, bi-directional link, groupıng, condıtional-indexed, condıtıonal guided and conditional indexed guided tour. The appropriateness of the use of these primitives is based on the type of attributes associated with the RMDM slices, its uniqueness and dependencies among the other attributes. Unless mentioned otherwise, the notations used in this chapter are identical to [Isakw95].


Figure 7.1: A Partial RMDM Diagram for the Ecological Application
Figure 7.1 shows a partial RMDM diagram of the concerned ecological application. It represents the navigation mechanism from the hypermedia users' point of view in the concerned domain. In the diagram, for simplicity and to avoid cluttering, slices of each entity are not included, only the key attributes are shown. Accesses to various entities are provided via the access primitives selected to associate the slices. For example, to access the large collections of uniquely addressable VS (Valuable Species), a conditional indexed-guided-tour is made possible with predicate affects_gr_of(VG,VS) from VG (Vegetation) entity as shown in Figure 7.1. Similarly, the reciprocal index
gr_affected_by (VS,VG) accessible from VS is of type conditional guided. These two indices are representing a many-many relationship. Similarly, from the VS there will be accesses of type conditional indexed tour to the entity MM (Management Method) with the predicate gr_mnged_by (VS, MM) and through this access, the users can detect the suitable method(s) for management of the species. Appropriateness of an access primitive to a specific entity type entirely depends upon the nature of entity type and their associated attribute slices. To access the management method details, from the main menu (the grouping mechanism on the top of the figure) conditional indexed tour is provided and accordingly, to access the set of vegetation affecting the growth of the valuable species, conditional guided tour has been found to be suitable.

The user will navigate the application through the various entrty-slice-heads (i.e. a distinguished slice used as a 'default' to anchor links coming into the entity). Access to and presentation of the entity domain entirely depends on how slices are designed and organized into a hypertext network. In Figure 7.2, slices of the species entity are shown. Numeric Codes (appeoring in the subsequent figures) associated with the directed edge represent various types of associations between the connecting attribute slices.


```
1 Abund_&_Var_of(Species) 2 Eco_Comp_of(Species) 3 Hab_Utlzn_of(Species)
4 \text { Br_Bio_of(Species) 5 Video_of(Species) 6 Graphical_of(Species)}
7 \text { Abund_Stat_pf(Species) 8 HAb_Utizn_of(Species) 9 Br_Bıo_of(Species)}
```

Figure 7.2: Slice Diagram for 'Speczes' Entity
Figure 7.3 shows the E-R diagram (an abstract representation with presenting the attributes) for the Ecological application. The various entities such as, Limnology (LM), Physical Environment (PE), Valuable Species (VS), Management Method (MM) and Vegetation (VG) are shown in rectangles. The relationship bears, possesses, managed_by,


| 1 : bears (PE, LM), | 2 : possesses (PE, VS) | 3 : possesses (PE, VG) |
| :---: | :---: | :---: |
| 4 : managed_by (PE, MM) | 5 : supp_gr_of (LM, VS) | 6 : results (LM, MM) |
| 7 : controls_gr_of (LM, VG) | 8 : is_a_result_of (MM, LM) | 9: effective_to (MM, VS) |
| 10 : concerns_to (MM, PE) | 11 : controls (MM, VG) | 12 : can_contr_by (VG,MM) |
| 13 : gr_contr_by (VG, LM) | 14 : affects_gr_of (VG, VS) | 15:gr_affected_by (VS, VG) |
| 16 : managed_by (VS, MM) | 17 : found_in (VS, PE) |  |

Figure 7.3: ER Diagram for the Ecosystem, Keoladeo National Park
supp_gr_of, results, and so on, are shown by directed line.
In the context of the above application domain- it has been found that the proposed RMDM fails to express some of the situations conceptually. To model those situations, either, some extra identifications (for entities) have to be introduced or some relationships that are not relevant to the concerned domain have to be made, which ultimately results in overspecification [Hofst93]. The three main drawbacks that RMDM suffers from : firstly, the application domain has numerous additional sub-groupings of its entities that are meaningful and need to be represented explicitly because of their significance to the concerned application. The present RMDM does not provide sufficient modelling constructs to model the situation in an adequate manner; secondly; the concerned domain includes some complex object-types. which are composed of according to some specific recursive rules and to model these recursively composed objects special modelling constructs are essential. However, the present RMDM does not provide any scope to model these objects naturally; therdly, a major step in RMDM modelling is to slice each entity based on the logical relationships exist among the attributes of it. However, it does not provide any guidelines; how to handle composite entity-based presentations (i.e presentations with multiple slices from different entities) as also detected
in [Balas95]. Thus the drawbacks of RMDM can be summerised as:

D1 Lack of modelling capabilities to naturally model those objects that have many subtypes defined according to some specific Subtype Defining Rules.

D2 Lack of powerful constructs to model those complex objects constructed based on some specific rules of recursive nature, such as multimedia document (On line documentation is one of the important aspects of any multimedia application development).

D3 Lack of modelling guidelines to represent composite slices combined from slices of different entities.

Next section discusses some of the necessary remedial measures to be taken against these drawbacks in details.

### 7.4 Modifications in the RMDM

The concerned application domain has numerous additional sub-groupings of its entities that are meaningful and need to be represented exphcitly because of their significance. For example, the entity 'species' has numerous collections of sub-classes as shown in the Figure 7.4 and sometimes, it is necessary for some instances of sub-classes to be navigated through their certain slices only. Thus, in other words, in case of some special entities, the navigation mechanisms are governed by some specific Subtype Defining Rules [Bomel91]. But with the present RMDM modelling constructs, it is difficult to model such situations conceptually. Appropriate utilization of specialization concept (as an analogous presentation found in the extension of NIAM model [Hofst93]) with additional modelling notations for it, can solve this problem.

### 7.4.1 Modelling with Specialization

In case of those specific instances of an object type belonging to a huge subtype hierarchy, when only some particular shces have to be navigated- to avoid 'loss in hyperspace' as well as violation of the 'conceptualization principle', it is very essential to organize the


Figure 7.4: Subgroup Collections of 'Specres' Entity
objects as per the subtype defining rules. The axioms relevant to it have been reproduced here, from [Hofst93] for the clear understanding of the concept:

S1. Specialization is a partial order (asymmetric and transitive) concept, which prevents occurrences of cycles in the structure. (Axioms (2,3)).

S2. Only atomic object types can occur as-subtypes and each subtype inherit their identification from their pater familias ${ }^{1}$. (Axioms $(4,5)$ ).

S3. Subtype hierarchies for label types and entity types do not interfere (Axıom (6)), where, label types are speciesindex, name, etc. of entity type species.


Figure 7.5: A Specialisation Hierarchy from the Ecological Domain

[^1]Figure 7.5 shows an application of specialization. In this figure, the dotted directed edge is representing the specialization relationship. Properties in a specialization hierarchy are inherited 'downward' (refer S1) e.g. Aquatic subclass inherits their identification from Ornithology, but the reverse is not true (refer S1) and each of these subtypes is not interfering (refer S3). Thus, during RMDM modelling, applying the concept of Specialization and by utilizing the Subtype defining Rules [Bomel91], the first drawback could be overcome.

The second drawback mainly related with some entities that are complex in nature due to their nested composition structure. One such entity very common to any hypermedia database application is multrmedia document (not covered in the Figure 7.1818 .3 ), which has its own layout structure. The layout structure of a document precisely defines where information is to appear on a plane surface when displayed on a terminal or printed on paper and also organizes it to aid in understanding. Document structure is most often expressed in terms of the abstract objects, hierarchical links between them, ordered and unordered objects and shared components. One can describe and represent this organization graphically by using a tree structure. For the sake of understanding, a systematic representation (layout structure) of a multimedia document analogous to one reported in [Karmc96] has been reproduced in Figure 7.6.


Figure 7.6: A Partial layout structure of the Multimedia Document

Current research on document representations are carried out in two areas : one focusing on passive documents; the other on active documents. In passive documents, the author integrates continuous media simply by representing them in a static visual form, later activated by the user. For example, the static visual form of a video sequence is a frame and the static visual form of audio is an icon. These can be embedded into traditional document type (i.e. those containing only static media type) and are played only upon user activation. In case of actrve document - since it requires to integrate the continuous media in the document itself, each media item has to be treated as an object to be presented in time for a duration. Basically, the structure of such multimedia document provides a set of rules for creation, manipulation and representation of this logical tree-shaped structure. As stated in [Karmc96], representing such document structure in terms of levels of hierarchies of abstract objects, has several purposes :

- to facilitate integration of diverse media types.
- to organize the document so that one can easily understand and manipulate it.
- to permit advanced queries based on attribute values and object types etc.

In general, such entities are modelled according to some specific rules. To model such entity with the present RMDM, it requires some additional modelling constructs with appropriate utilization of generalzzation concept. The next section describes the modelling of complex nested structure using generalization concept.

### 7.4.2 Modelling with Generalization

Generalization is a mechanism that allows for the creation of new object types by uniting existing object types. The following axzoms and lemmas [Hofst93] provide the basis of generalization :

G1 Generalization is a partial order (asymmetric and transitive) concept, which prevents occurrences of cycles in the structure. (Axioms (7,8)).

G2 Only atomic object types can participate in generalization and each generalized object type requires the identification from its instances (Axioms $(9,10)$ ).

G3 If $\alpha$ is a generalization of $\beta$ or $\beta$ is a generalization of $\gamma$ then $\alpha$ is not a specialization of $\beta$, i.e., $\alpha$ Gen $\beta \vee \beta$ Gen $\gamma \rightarrow \neg \alpha \operatorname{Spec} \beta$.

Thus, during construction of the 'hypertext network' with the present RMDM, by appropriate utilization of the aforesaid axioms and lemmas, one can easily overcome the second drawback. In Figure 7.7, the modelling of multimedia document based on generalization concept has been depicted. Here, the generalized object-type document is covered by its abstract object types :title(i.e. stream of characters), Section (i.e. stream of characters), Audio type (i.e. icon), Raster Graphics(i.e. cluster of pixels) and Geometric graphics(i.e. shape definitions), which are atomic object types in nature and the document type borrows the identifications from these atomic object types (refer G2). In generalization, each generalized object is covered by its constituent object types or specifiers. Hence, a decision criterion as in the case of specialization (the subtype defining rule) is not necessary. Furthermore, properties in a generalization hierarchy are inherited 'upward', but the reverse is not possible, i.e. properties of Section will not be inherited from Document (refer G1) which is the case of specialization. Finally, Section is a Generalization of Characters and at the same time Sectoon is a Specialization of Document, but Character is not a Specialization of Document (refer G3). In most of the data models, it is seen that generalization is treated as an inverse of specialization. However, it is contradictory, as they are originating from two different axioms in set theory and they have a different expressive power. For the sake of validity, an illustration is given in in Figures 7.887 .9 .


Figure 7.7: Modelling Multimedia Document using Generalisation


Figure 7.8: Specialisation instead of Generalisation


Figure 7.9: Modelling using Generalisation
Consider, a navigation problem for listing all female Species, in the concerned Ecological domain. A Species is either an instance or a set of instances of Ornithology or Mammals. An instance of Ornithology is identified by an 'Ornithology Index', whereas, a Mammal is identified as a 'Mammal Index'. In this case, Species is the generalization of Ornithologies and Mammals. Species have attributes 'Gender' and each of its instances has attributes 'Habit_Utlzn', 'Breed_Bio' and 'Index'. With the present RMDM, based on the 'specialization' concept such a situation could be modelled as shown in Figure 7.8, where, the dashed directed line represents the specialization relationship and the oval shapes are used to represent the attributes associated with each entity. But, such a modelling results in overspecification, due to the following reasons:

- It introduces an extra attribute 'Species Index' to identify the Species.
- Differentiating both the types of Species instances as total and disjunct, it necessitates a special attribute 'Type', to determine the type of the Species.

However, this situation could be modelled in an appropriate manner by utilizing the 'generalization' concept (as shown in Figure 7.9). In the figure, the directed solid lines
are used to represent the generalization relationship and the double-outlined rectangle is used to represent the entities of 'generalized type'. As Species inherits their identification from its sub-species, such as, Ornithologies and Mammals (refer G2) and as these instances are expressed as total and disjunct (as per the 'Generalization rule'), both of the attributes 'Species Index' and 'Type' are no longer required. Hence, in some specific cases, instead of specialization, only the generalization concept is applicable and appropriate.

The third drawback deals with modelling of multiple slices from different entities to be appeared in the same window. In most of the hypermedia applications, it is often necessary to compose multimedia scenes based on multiple slices (possibly with minimized information) from different entities. Such slices with minimized attributes (referred here as 'representative slice') may be used as an 'window' to the corresponding head-slice for accessing the entity detail. Similarly, considering the all slices from different entities composing a multimedia scene may togetherly be defined as a 'composite slice' for better organizing the 'hypertext network'. However, the present RMDM does not provide any guidelines - how to handle such situations. As such, these two additional slices (i.e representative \& composite slices) have been introduced in the present RMDM to model any complex navigation pattern in a better manner. The composite slice used in the extended RMDM is analogous to the 'cross-entity' slice found in [Balas95]. The representative slice is defined to be the summarized attribute information, to represent all the slices of an entity. Thus apart from the 'head slice', the modified RMDM includes one more additional slice for each entity to be used as an anchor to help in determining the appropriate of information to be displayed and hence by increasing the local coherence.

For the verification as well as for validation of the extended RMDM, a prototype Multimedia Information System (MMIS) has been developed based on this model as well as the MMIS architecture reported in [Bhatt96b]. A brief overview of the implementations is reported in the next section.

### 7.5 Overview of the Extended-RMDM Implementation

A prototype software has been developed based on the extended RMDM, and implemented in HTML and Visual Studio Platform. A partial view of the high level access structure mechanism utilized in the proposed software is reported in Figure 7.10. Access Structures are designed by grouping the items according to their nature and types of interest. Basically, the hypermedia end-users can select any of the six menu options to access the application database. In case of Species entity, accesses are organized into further subgroups according to the 'Index' and 'group type' associated with each instance of the Species as well as the 'name' and 'habitat type' attached with each Species. Similarly, also in case of the large set of Vegetations, sub-menu structures are provided.


Figure 7.10: Partial view of the High Level Access Structure Mechanism
The HTML implementation shows the hypermedia presentation of the material collected in the Keoladeo National Park Project [Salim86]. This collection includes textual, sraphical and image data about the species, vegetations, limnological and environmental
statistics etc. The application is intended to present the material of the project in two modes: contextual reference based and graphical RMDM based. Figure 7.11 shows the introductory screen, also serves as the main-menu, where user has a choice of viewing the materials- topic wise either from the textual content (by selecting any anchor) or from the graphical presentation (as shown in the upper-right corner, where each entity or relationship box serves as an anchor). Each screen may contain references to documents and photographs that are part of collections. For instance, by clicking on the contextual topic 'Ornithology', one can find out more information about the species belong to the 'Ornithology class', about their population, habitat-utilization, breeding biology, etc. Figure 7.12 shows information about the Siberian crane. Clicking on the photograph of the crane, a larger view can be obtained; in the textual part, the brightened word gives contextual information regarding the population, breeding biology, Food and feeding habitats, etc.

### 7.6 Conclusions

In this chapter, a hypermedia application data model, called RMDM has been studied and analyzed in the context of a real-life ecological application. From the analysis, it has been found that the above model fails to express some of the situations of the concerned application domain conceptually. This chapter projects the drawbacks of the RMDM and subsequentlj; the necessary remedial measures have also been suggested. With the proposed remedies, the present RMDM has been extended and the extensions are validated by several example hypermedia domains. A prototype software for the Keoladeo National Park, Rajasthan, India, has also been developed based on the extended RMDM and it has produced satisfactory results.

With the tremendous growth of multimedia technology, image and video databases have consequently become the central component of many future applications. The efficiency of an image or video database system mainly depends on its performance in answering the queries. To handle the complex queries over the large repository of image or video databases, a suitable and user-friendly database system architecture is essential. The next chapter presents a new image database systems architecture which would cover a wide variety of applications.


Figure 711 RMM based prototype implementation of Keoladeo Park


Figure 712 A screen showing information about Siberian Crane

## Chapter 8

## Image Database System

## Architecture

### 8.1 Introduction

The advances in multimedia technology (as reported in Chapter 7) basically centers around new ways to store, retrieve as well as transmit digital information. Consequently; image and video databases have become the central component of many future applications. An appropriate image database system (IDS) architecture would aid in providing convenient and efficient access to the data contained in an image database.

Information relevant to an image application, may need to be stored in multiple formats. Answering a user-query typically requires handling of such information in multiple forms and representations. Correlating these information at the physical level by pre-analysis is not an attractive option. For example, there could be thousands of images, and each image can have several 'objects of interest', thus during query processing, retrievals and matching of all these objects at the physical level would be very time consuming and un-rewarding process. Therefore, it is believed that to support the quicker query processing activities, it is quite necessary to represent as well as process the digital data in a semantic level (referred here as metadata). However, in general humans are more capable of abstracting information efficiently from images, displayed on the computer. This enables them to correlate and match information of a queried object at a higher semantic level with the stored objects' representations such as the symbolic representation of data in structured databases. This semantical correlation
and matching of information in an efficient manner, across various representations is lacking in the current IDS architectures and has been characterized as a "semantic bottleneck" [Subra96]. To overcome this limitation, this chapter introduces a threelayered metadata-based IDS architecture, which rather than processing the complex queries at the 'physical level', prefers to handle it at the 'logical' or meta-level for more economic and quicker responses. For the sake of validity, the various implementation issues of the proposed architecture in the context of a museum-cum-archival application has also been reported in this chapter. The next Section reports a brief review of the existing image retrieval systems and metadata based architectures.

### 8.1.1 Reviewing the Image Database Systems

There is a multitude of application areas that consider image retrieval as a principal activity [Gudv96]. Tamura and Yokoya provide a survey of image database systems that were in practice around the early 1980s [Tamur84]. Chock also provides a survey and comparison of functionality of several image database srstems for geographic applications [Gudv96]. Recently, Grosky and Mehrotra [Grosk88, Grosk92] and Chang and Hsu [Chang92] discuss the recent advances, perspectives and future research directions in image database systems. More recently, [Gudv95] provides a comprehensive survey and relative assessment of Picture Retrieval Systems. The survey reveals that to support quicker query processing activities, it is essential to represent as well as process the digital data in a metadata-level, which would enable the users for better correlation and matching of information of a queried object. However, from the perspective of query solving, in a metadata based architecture, the metadata should be capable enough for representing the contents of the image data in an appropriate manner. Semantics of an image and its objects include both the "meaning" and "use" of an object [Kashp96]. The metadata level represents the level at which the information from the various media formats shall be viewed and compared. Some of the significant recent work in developing metadata for digital media can be found in [Subra96, Klaus94]. Bohm and Rakow have provided a classification of metadata in the context of multimedia documents. Jain and Hampapur have characterized video metadata and its usage for content-based processing. Kiyoki et al. have used metadata to provide associate-search of images for a set of user-given keywords. Anderson and Stonebraker have developed a metadata scheme for management of satellite images. Grosky et al. have discussed a data model
for modelling and indexing metadata and to provide the definition of higher abstraction. However, the level of abstraction at which the content of the images is captured and represented, is very important.

From the survey, it appears that in the context of the diverse application areas, the characteristics of most of the existing image database systems have essentially been evolving from domain specific considerations, and hence, a very little consensus exists among these systems. It is strongly felt that there is a lack of a standard IDS architecture, which would be 'easy to use' and would cover a wide variety of applications. The nex' Section describes the design of the proposed metadata' based three-layered architecture.

### 8.2 Image Database System (IDS) Architecture

Tin ust important characteristics of an Image Database System are :

- it supports image data which are conceptually semi-structured in nature. The semantics of an image entity is a function of the semantics of its components;
- it supports multiple user views, and
- each image entity possesses basically two types of attributes and relationships : content-based and content-independent, where the content-based attributes and relationships are required to undergo appropriate decoding procedures, whereas the others do not

To enable the users for better handling of the complex, storage-intensive image data pertaining to an IDS, the designer is to emphasize two aspects : the extraction of content-based and text-based features for each image and its logical components; and secondly the generation of metadata from the extracted 'raw' features. For the purpose of feature-extraction and for better representation of the visual semantics in a conceptual manner, it introduces a data model, referred here as Visual Semantic Model (VSM). Next subsection discusses the importance of image data model in the context of complex query processing and it also presents the proposed VSM.

### 8.2.1 Image Data Modelling

The objective of an image data model is to represent the semantics of a scene such as the image entities, their attributes, associatzons among the entities and the logical organzzatrons of each entity, in order to determine the view(s) of the content of an image. Thus, an image data model should be capable enough for expressing these semantics at desired level(s) of abstractions in a conceptual manner. However, due to the diverse nature of image database applications, it is intrinsically difficult for the designers to conceive a general image data model. A standard formalization of an image data model, which can serve as a platform on which other aspects of image database systems, such as query processing, retrieval etc. can be realized, has been a major 'bottleneck' for long time. As found in [Gudv96], in an advanced image database systems, one can find four categories of data : formatted, structured, complex and unformatted. Formatted data are most commonly found in traditional databases. Structı data are heterogenous types of data about an object that need to be stored and . :eved together. When the structured data possess variable number of components, tiey are referred to as complex data. Unformatted data are usually the 'string data' (also referred to as byte string, long field, Binary Long Object Box (BLOB)), whose structure is not understood by the database management system. To understand the semantics of the unformatted data types, special procedures/methods are essential. In this background, several data models can be found in the traditional DBMSs, e.g. relational, hierarchical, network, etc, where the data to be managed are of formatted type. However, though these traditional DBMSs based on the relational data model, have also been used for image database management, they are not "true" IDBMS (Image DBMS) [Gudv96]. For, the level of abstraction offered by these data models for representing the images is too high; and the data model, the query specification language and the retrieval strategy are essentially those of the traditional DBMSs. However, to overcome the limitations faced with the traditional DBMS, there has been a great interest in providing several extensions to the relational data models to overcome the limitations imposed by the flat tabular structure of relations for geometric modelling and engineering applications [Gudv96]. The resulting data model is characterized by the addition of applicationspecific components to an existing database system kernel. They include nested relations, procedural fields, a query-language extension for transitive closures, among others. The primary objective of all these extensions is to overcome the fragmented representation of the geometric and complex objects in the relational data model. Image data is stored
in the system as formatted data. However, to a database user this view of data is made transparent through these extensions.

In this background, several other data models have also been proposed in [Chen76, Bomel91, Hofst93, Grifn93]. Some systems perform 'spatzal reasonıng' as a part of the query processing while other systems have attempted cognitive approaches to query specifications and processing [Chang88, Chang91, Sisla94, Sisla95, Tanaka88]. However, in the context of complex content-based image information, the existing image data models still have been found to be inappropriate and the level of abstraction at which the image information is represented is too low. Next subsection presents a suitable, semantically rich image data model, based on the concept available in [Gudv96].

### 8.2.2 The Visual Semantic Data Model : VSM

The proposed VSM provides scopes to represent the semantical information of any image scene at a desired level of abstraction as per the application requirements. In Figure 8.1, an rmage-level representation of a scene based on the VSM notations and conventions, has been shown. The rectangle shape symbolizes the abstract amage class, the double bordered rectangle represents the abstract classes of image entzties identified from the image. The oval shapes represent the objects of interest associated with the image as well as its entities, such as the features or attributes, positional constraints, logical compositions, semantical associations etc. It supports almost all types of associations often necessary in a complex scene representation. A solid line with Double headed arrow represents the 'multi-valued' attributes, a single-headed arrow represents 'single-valued' attribute, a dotted directed line represents the 'part-of' relationship and a line with thick headed arrow represents the 'depends on' relationship etc. As the proposed VSM helps in modelling an image at various levels of abstractions, to provide supports in modelling the entity-level relationships, it includes an additional class of notations and symbols. An abstract class of interface is provided to facilitate the model-information-acquisition process. Interfaces are designed based on the concept available in [Gudv96, Jack83, Flick95]; the underlying 'Object-based' concept in the interface helps in identifying the 'image-objects' (i.e. the entities) and their relationships; the 'query-by-example' environment assists the user in providing relevant features for each entity and a 'background/foreground'model-based interface provides the necessary tools to derive the shape-features for the image and its entities. The various components and
relevant 'objects of interest' of the proposed VSM are described below.


Figure 8.1: Modelling an Image using VSM
Image and Its Entities : The proposed VSM provides a distinct set of modelling constructs to represent the image, its entities and their relationships. Identification of the entities are made through a semi-automatic process at the time of image insertion as well as query solving. The interface is designed based on a object-based approach [Jack83] which accepts a set of domain-specific key-sentences from the user and based on a 'filtration' and 'identification' procedure, it separates out the entities. The existence of entities in an image scene, entirely depends on the angle of interpretation used by the: designers. As for the same content of an image, there can be multiple interpretations. So, the entities located by a user for a specific scene may not be expected for another user.

Shape outline and Features for Image and its Entities : The shape outline of an image basically provides the boundary sketch of the raw image, and the entity shape provides the outline for each individual entity. To derive the shape outline of the image and its entities, a model-based [Flick95] interface with a set of tools, is provided. Finding the outline of an image is rather easier and simpler than finding its entities. However, many efficient shape-detection tools have evolved during the current decade [Gudv95] in order to support this activities. The interface also provides a database of 'textures' and 'color-palates' to provide necessary supports in the appropriate identification of the shape features associated with the derived 'boundary-sketch'.

Content-based and Content-Independent Features: Due to the richness of the information content in the images, there can be many interpretations for the same image, and the interpretations depend entirely upon the requirements from information retrieval point of view. The interpretation of the content of a 'painting' made by an artist may be different from its interpretation made by common people. Both image and its entities may have some attributes derived externally or based on the content of the image or image-entities. The attributes or features based on the content are known as 'content-based' attributes and the others (i.e. derived externally) are referred to as 'content- independent' attributes. For example, the shape-features of an image-object, stroke-patterns in a painting, etc are content-based, whereas, the date_of_acquisition, image-index, etc are content-independent features.

Entity-Relationships : The proposed VSM supports various semantical relationships among the entities of the image, such as spatial, actions, overlapping and other conventional semantic associations. Among the spatial or positional relationships, specifically the relationships, such as left_of, right_of, in_front_of, behind, above and below are used. The overlapping relationships include left_overlaps, right_overlaps, bottom_overlaps, top_overlaps etc. Relationships which describe the various actions (or, role) played by an entity are belonging to action-relationships group, e.g. shaking_hand, moving_to, smiling_at, holding etc. A detailed discussion on these three types of relationships can be found in [Sisla94, Sisla95]. Other semantic relationships includes the conventional associations among the entities, such as consists_of, inherits, abstraction_of etc. These relationship information are extracted a priori (by a combination of both algorithmically 'as well as by manually).

Thus, the construction of VSM can be summarized as a sequence of three basic transformations, as noted below :

1 : the transformation in which the image-level content-based and text-based attributes (e.g. type, class, shape etc.) are derived.

2 : the transformation which deals with the relationships among the objects of interests from compositional, spatial as well as semantical associations point of view.

3 : the transformation, where the entity-level content-based features (e.g. shape, textures etc) are extracted and derived.

The model information are, used as input to a conversion mechanısm to generate the corresponding metadata for each image-object, and the proposed architecture (will be discussed next) utilizes the metadata in answering the various queries.

### 8.2.3 The Proposed Architecture

The proposed three-layered, metadata based architecture supports all the common characteristics of an IDS. It is designed based upon the concepts available in [Gudv96. Kashp96, Bhatt96b]. The various layers of the architectures are :

- Database layer, to store the physical images as well as the associated logical data in an easily manageable form. To manage properly and to provide quicker database responses, the database layer is further sub-divided into two sublaycrs namely, logıcal or meta-sublayer, and physıcal or dıgıtal-sublayer;
- Systems or processing layers, to provide necessary supports for better utilization of the precious image-data stored in the physical layer. It consists of the various application modules, where each module is designed, in order to achieve some pre-specified objectives;
- Applıcatıon or interface layer, to provide better and realistic presentation support against the IDS requests, made by the 'end-user'. It is basically a collection of several abstract interface classes, each of which corresponds to an application processing module.

The main objective of this architecture is to provide a 'means' for easy mapping the real-world problem domain into an image database application domain. The various layers of the proposed architecture are discussed next.

## Database Layer

The physical data in an image database may need to be stored in multiple formats as per the applications requirements. During query processing, it is often essential to manipulate these digital data across the different storage formats, ether at the 'imagelevel' or at the 'component-object level'. However, for easy manipulation, it is essential
to treat them at the 'semantic' or 'meta-level' [Gudv96]. During new object capturing or insertion process, or during query processing, relevant features of each object are extracted, filtered and then utilized in the construction of a corresponding VSM. Finally, the model-information is transformed into the respective 'metadata', based on a conversion procedure (analogous to [Rishe93]). These metadata related to each of the physically stored image-objects are collectively stored as a 'meta-sublayer' (as shown in Frgure 8.2). 'The two sub-layers of the database layer are discussed next.


Figure 8 2: The proposed three layered IDS architecture

## Physical Sub-layer

This sub-layer contains the actual (raw) data which might be stored in any of the image data formats Images may be of different modalities like Paintings, Legal Photographs, X-Ray, MRI scan etc.

## Logical or Meta Sub-layer

This sub-layer holds information referred here as 'mctadata', which can be described as the summary of the information content about the 'images' of the physical data layer in an intentional manner. These metadata are the representation of both the content-based and content-rndependent features of the physical images and their component objects. The content-based metadata includes the attibute information about each of the 'ob-
jects of interest' (e.g. the physical characteristics of the object, etc.), as well as the -information about the relationships which exist among the objects or entities. Relatzonships are categorized, based on their nature of occurrences, into three: spatzal, actions, overlapping and other conventional semantical assocıatıons. Besides the content-based, the proposed architecture also incorporates metadata representing the text-based content descriptions (such as location, date, time_of_creation, etc.) for each of the objects. For the purpose of extraction of these features, a class of user-friendly interfaces are used, and these raw features are finally 'filtered' by using a converszon procedure (which assigns appropriate 'weigtages' (in 10-point scale) to each feature) the corresponding metadata (i.e. a $k$ - dimensional feature tuple, where $k$ is the number of features) are generated. These metadata are associated with the digital media through the 'internal disk-addresses' maintained for each physically stored object.

To enhance the performance of an IDS, implementation of an appropriate indexing 'mechanism is very essential. The current literature [Subra96, Gudv95] reveals that for optimal utilization of the content-based information in retrievals, a content-based indexing mechanism is always preferable. The proposed architecture also uses an indexing mechanism based on the nearest-nezghbour-search concept, as available in [Chiuh94]. Before serving any query requests, the $k$-dimensional feature vectors i.e the metadata collections are indcxed using a $k-d$ search tree method based on an $n$-ary partutional approach. If the ranked list of images located from the indexed database, is still found to be not browsable, then it kecps provision for a finer-entzty level sequential searching mechanism to identify the most, minimum set of 'desired' images.

## Systems or Processing Layer

This laycr basically comprises a set of processing modules, designed based on objectoriented concept. Each module performs some pre-specified activities or operations defined for a conccrned application domain, such as : insertion \& composition, fcature extraction \& representation, metadata generation, query processing \& browsing support, presentation, etc. Each of the modules is bricfly described below.

## Image Insertion \& Composition Module

This module helps insert a new 'object' into the database as well as compose a new object from the existing objects, based on some pre-defined constructor operators. Since,
lhe image database applications are generally insertion-and-query-intensive in nature, lhis module has an important role in the creation of image database. It supports a strong set of tools and techuiques (as found in [Flick95]) for capturing and composing new objects to the database.

## Feature Extraction/Representation and Metadata Generation Module

As the extraction \& representation of 'features' and subsequently the 'metadata' generation are inter-related processes in an IDS application, they may be discussed together in the same sub-scction In this architecture, metadata are at the most critical level and as it is generated entioly depending on the feature-cxtraction and representation pocesses, this module has a significant role. The extraction / representation process occuns basically in thice phases as shown in Fegure 8.3. Each of these phases is discussed below:


Figure 8.3. Feature extaction and metadata gencration
[ $\Lambda$ ] Image Feature Extraction Phase: This phase basically deals with the acquisition of vaions content-- ansed and content-independent altributes and relationships for cach of the intages and its objects-of-interests. During new object insertion or at the time of query solving, this phase invokes a class of user-friendly interfaces, de-
signed based on query-by-example principle, to acquire the various image-level and entity-level attributes (e.g. the physical characteristics, shape features, contentindependent description information, etc) their compositional, spatial as well as other semantic relatiouships information etc. To provide necessary supports at the various levels of extractions, this module also includes a strong set of tools for the purpose of feature selection (such as texture database, color wheel, etc.), shape drawing etc.
[B] VSM Construction Phase : The proposed extraction/representation module also supports a graphical tool for presentation of the captured object-relationship information in an understandable form, based on the notations defined with the proposed VSM. The model is constructed in a semi-automatic manner. The main objectives of this model is: (a) to understand and represent the complex semantics of an image scene, and (b) to assist in solving complex queries. Figure 8.1 shows representation of a typical image scene based on the proposed VSM notations.
[C] Fine Feature Extraction Phase : This phase deals with some special tools and techniques (for example, an object-outliner with transformation utility, colour composition detector, etc.) to extract the finer features of each entity, such as entityslape, lexture-variations, intensity-distribution, etc. A class of interfaces are designed to assist; in this extraction process. The feature extraction tools are utilized in scveral passes for finer property detection and subsequently a set of 'filters' are used to eliminate the redundant information. Due to the complex nature of entity-types, it has been found that in some situation, the appropriate extraction becomes possible, only when there are manual interventions. After extraction, the features information are transformed in order to generate the corresponding metadata.

Once the model information comprising both the content-based and text-based feature information for each image as well as its 'objects of interest' are transformed (bascd on a conversion mechunism analogous to [Rishe93]), the next step is to construct a $k$ dimensional feature vector, to represent each image as a point in a $k$-dimensional space. Such a $k$-dimensional vectors or Seuture-points for each image, together constitute the logical mela layer for the physically stored image data layer. The feature-vectors are exploited in an indexing mechanism to facilitate especially, in the content-based searching mechanism. The indexing mechanism used in the proposed architecture is a variant of

## [Chinh94]

## Query Processing and Browsing Support

The activities of the query processing and browsing support modules are inter-related to some cxtent In case of both the modules, accession of image database, its retricval as woll as filtcring techniques would be same. So, both these modules could bo discussed together. The query processing in an IDS takes place in a similar way as in other database systems. Duc to the possibilitics of multiple interpretations for the content of the same image for different users, the logic in querying an image database would not be straight-fon ward and simple. Thus, it is essential to be careful enough, in finding an appopiate ques $y$-solving appioach. The proposed architecture employs a query-solving method based on a unified approach. It, attempts to utilize both the content-based and content-sndependent information for the imput 'candidate object' at vanious levels, and based on these information, similatities with the stored features of 'prototype objects' are computed using a set of puc-defincd rules [Sisla94, Sisla95, Gudv95]. For faster query responses though optimum utilization of the content-based features, a $k-d$ seatch tree hased mdexing mechanism is used, analogous to [Chiuh94].

In Fugue 84, the schematic of the query-processing mechanism has been shown, which includes a set of processing modules. Initially, for the query-object, through an interactuve session, all possible image-level featues along with the relevant entityıclationship information are extsacted as woll as derived. The redundant information are climmated based on a set, of scmanluc filters. With the 'refined' entity-relationship features, using the defned VSM notations, a consesponding data model for the query-image scenc is constructed To support the construction as well as for better presentation, a graphical tool is designed, which works semi-automatically. Later, the text-based and conteut-based model-information are input to a conver szon procedure to assign appopriate weightage for cach of the features to ultimately generate the corresponding metadata, 1 e the $k$-dimensional feature vector

An entity-level fince-feature based sequential matching mechanisn has also been defincd (optionally) with this query processing and browsing mechanism, which may be moked, if the users are not, satisfied with the size of the ranked Jist derived due to the above indexing mechanism However, the complexity in the query processing logic depends upon the complexity of the featues to be handled for the image entities.

## Application or Interface Layer

The user interface layer is designed to let users easily select content-based and text-based features, allow these features to be combined with each other, and let users reformulate queries and generally navigate the database. For better presentation of the queried results, it also helps by providing an interactive presentation tools.


Figure 8.4: Qucry processing mechanism

### 8.3 Implementation Issues

The proposed architecture was tested in the context of a real-life archival and museum application. The application is a database for managing the various archives and musemm items found in North-East, of Infa, collected and preserved by the Traditional

Culture and Ait Forms (TC $\wedge \mathrm{F}$ ) Department of Tezpur University, India The intended users of this system are the sturdents, faculty members and other visitons to the TCAF Depatment The collection contams around 2000 full-colour photogiaphs of the various haditıonal dances, beauty and costume 1 tems, anound 650 black \& white photographs of the prumitive cultual tems, 400 coloufful paintings (acquired in the form of coloured photographs) and photogiaphs of some ienowned personalities related the culture and at torm of this part of country A prototype system called "Archival and Muscum Database Systen (ARMUDS)" has been developed using Visual Studuo utilities in a Pontum-Pio platifom The systom has generated some of the test icsults, which are found to be satisfactory The software is still under acfinement

### 8.4 Conclusion

A now, thice-laycred, metadata-based Image Database System architecture, designed leased on modnlanty, code-sensahnlaty and abstataction mechanisms has been introduced in this chapter The architecture handles the physically stored digital data, at meta-level lo provide easy manipulation and quickeı query ıesponses For better understanding of the complex queues as well as to repiesent the image semantics at a desired level of abstraction, it also proposes a visual semantic data model. To justify the usefulness of the auchutectuce, a prototype software has also been developed and the responses are found to be satisfactory

Next, chapter summanzes the contibutions of the work and indicates the future expersions of the work

CHAPTER 8. IMAGE DATABASE SYSTEM ARCHITECTURE

## Chapter 9

## Conclusion and Future Work

This chapter summatizes the main contributions of the work and provides directions for future extensions Some studics on characterization on additive CA based on matiox algebia have been 1 cported in this 1 escanch work. We have extended the characterization of ENCAs to some cxtent. Some of the significant jesults of ENCA can be summarized as Collows :

1. Hacre exists a class of gioup ENCAs (maximum-length and non-maxımum-length) which validates the propertics of 3-neighbouhood additive group CAs reported in [Nandi94a].
2. Hene exists a chass of mon-gıoup ENCAs, which validates all the prope ties of 'IPMA CAs, as ieported in [Nandi94a].

Ciyptogaphy has become an essential requitement for protecting pivate information agdiust unauthonized access. It is the only practical means for sending infomation over an insecure chamel. The increasing use of electonic media for data commmotation, compled with the phenomenal growth of computer usage, has significantly aised the necessity of constructing suitable schemes for authentication, data security and authenhicated key exchanges In this context, using CA as a basic building block, new schemes for message anthentication and data security have been established. Based on these proposed CA based schemes, a new password-only authenticated key exchange scheme has also been established for user anthentication.

Reliable communication and reproduction of data is desirable in a distributed as well as stotage systems With the emergence of lange-scale, high-speed data networks
for exchange, processing aud storage of digital information in the military, governmental and private spheres, the demand for such reliable systems has been increasing. In this background, we have proposed a $t$-EC/d-ED $(t<d$ and AUED codes to control errors, so that reliable reproduction of data can be obtained. Based on even-parity check logic using odd-weight column matrix, a SEC-DED-AUED symmetric code has also been proposed. It has been established that both the schemes show significant results by reducing the ROM word-length.

With the proliferation'of the various heterogenous form of media data (such as image, video, audio, graphics, text, etc.) as well as the proliferation of a number of commercially available tools to manipulate these data, an explosion of interest has been noticed in liypermedia application developments. However, a standard, easy to use data model for conceptual modelling of any scale of hypermedia application domain is still lacking. We have studicd, analysed and extended a data model, referred as RMDM to enable the modellers to represent the semantics of any complex hypermedia domain naturally.

With the enormous growth of information technology and the presentation technique, in particular, there has been a great demand for high quality image processing and faster retrievals- that require a suitable image database systems (IDS) architecture. In this thesis, a new architecture for image database processing and retrieval has been proposed, which utilizes both the content-based and text-based features for the physically stored digital images. For the better understanding of the complex queries, as well as to represent the content-enriched semantics of the image scenes at a desired level of abstraction, a visual semantic data model has been proposed too. The implementation aspects of the proposed architecture in the context of a real-life case has also been described.

### 9.1 Future Works

In the following, some of the possible directions of future works in the field of Cellular Automata, data security, autheutication, error control coding and image database systoms are outlined:

- The characterization of group and uon-group ENCAs (Extended Neightourhood CA) has been repotted in this thesis. Such study can be extended for complete and more generalized characterization of ENCAs.
- The one-way hash-function and enciphering scheme reported in this thesis can be extended to hardwired implementation of the schemes.
- The non-group, non-linear MACA properties can be further studied for its utilization in Stegenography.
- The ENCA based block cipher system reported in this thesis can be further extended to the design of a compact hardware-based unified scheme, which operates both in block and stream cipher mode.
- the work on $t$-EC/d-ED/AUED code construction can be further enhanced to reduce the overall code-length.
- The work on Image Database System reported in this thesis can be further enhanced by incorporating an improved version of content-based indexing mechanism.


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## Biodata

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[^0]:    ${ }^{1}$ using parity check generator matrix

    $$
    G=\left[\begin{array}{llllllllllllllll}
    1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\
    0 & 1 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 1 \\
    0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1
    \end{array}\right]
    $$

[^1]:    ${ }^{1}$ A specialization hierarchy is in fact not a hierarchy in the strict sense, but an acyclic directed graph with a unique top. The top is referred to as the 'pater famalias'

