4.9 : Finite element model validation with an experimental study ..... 52
4.10(a) : Variation of $A_{m y}$ versus $L$ and $W(D=0.3)$ ..... 54
4.10(b) : Variation of $A_{m y}$ versus $L$ and $W(D=0.4)$ ..... 55
4.10(c) : Variation of $A_{m y}$ versus $L$ and $W(D=0.6)$ ..... 55
4.10(d) : Variation of $A_{m y}$ versus $L$ and $W(D=1.0)$ ..... 56
4.10(e) : Variation of $A_{m y}$ versus $L$ and $W(D=1.5)$ ..... 56
4.11(a) : Variation of $A_{m y}$ versus $L$ and $D(W=0.2)$ ..... 57
4.11(b) : Variation of $A_{m y}$ versus $L$ and $D(W=0.4)$ ..... 57
4.11(c) : Variation of $A_{m y}$ versus $L$ and $D(W=0.6)$ ..... 58
4.12(a) : Variation of $A_{m x}$ versus $L$ and $W(D=0.3)$ ..... 60
4.12(b) : Variation of $A_{m x}$ versus $L$ and $W(D=0.4)$ ..... 60
4.12(c) : Variation of $A_{m x}$ versus $L$ and $W(D=0.6)$ ..... 61
4.12(d) : Variation of $A_{m x}$ versus $L$ and $W(D=1.0)$ ..... 61
4.12(e) : Variation of $A_{m x}$ versus $L$ and $W(D=1.5)$ ..... 62
4.13(a) : Variation of $A_{m x}$ versus $L$ and $D(W=0.2)$ ..... 62
4.13(b) : Variation of $A_{m x}$ versus $L$ and $D(W=0.4)$ ..... 63
4.13(c) : Variation of $A_{m x}$ versus $L$ and $D(W=0.6)$ ..... 63
4.14(a) : Simplified model for estimating $A_{m y}$ in active case ..... 65
4.14(b) : Simplified model for estimating $A_{m y}$ in passive case ..... 66
4.14(c) : Simplified model for estimating $A_{m x}$ in active case ..... 66
4.14(d) : Simplified model for estimating $A_{m x}$ in passive case ..... 67
5.1 : Typical finite element model of an in-filled trench ..... 71
5.2 : Finite element model validation ..... 72
5.3 : Comparative study on vibration isolation by a softer barrier ..... 73
5.4(a) : Effect of backfill shear wave velocity ratio on $A_{m y}$ ..... 74
5.4(b) : Effect of backfill shear wave velocity ratio on $A_{m x}$ ..... 75
5.5(a) : Variation of $A_{m y}$ versus $L$ and $D(W=0.3)$ ..... 76
5.5(b) $\quad: \quad$ Variation of $A_{m y}$ versus $L$ and $D(W=0.5)$ ..... 76
5.6(a) : Variation of $A_{m x}$ versus $L$ and $D(W=0.3)$ ..... 77
5.6(b) : Variation of $A_{m x}$ versus $L$ and $D(W=0.5)$ ..... 77
5.7(a) : Effect of $D$ and $W$ on $A_{m y}$ in active case $(L=1)$ ..... 78
5.7(b) : Effect of $D$ and $W$ on $A_{m y}$ in passive case $(L=5)$ ..... 79
5.8(a) : Effect of $D$ and $W$ on $A_{m x}$ in active case ( $L=1$ ) ..... 79
5.8(b) : Effect of $D$ and $W$ on $A_{m x}$ in passive case $(L=5)$ ..... 80
5.9(a) : Effect of $D / W$ on $A_{m y}$ in active case $(L=1)$ ..... 81
5.9(b) : Effect of $D / W$ on $A_{m y}$ in passive case ( $L=5$ ) ..... 81
5.10(a) : Variation of $A_{m y}$ with $V_{b} / V_{s}$ and $W$ in active case $(D=0.5)$ ..... 83
5.10(b) : Variation of $A_{m y}$ with $V_{b} / V_{s}$ and $W$ in active case $(D=0.75)$ ..... 83
5.10(c) : Variation of $A_{m y}$ with $V_{b} / V_{s}$ and $W$ in active case $(D=1.0)$ ..... 84
5.10(d) $\quad: \quad$ Variation of $A_{m y}$ with $V_{b} / V_{s}$ and $W$ in active case $(D=1.25)$ ..... 84
5.10(e) : Variation of $A_{m y}$ with $V_{b} / V_{s}$ and $W$ in active case $(D=1.5)$ ..... 85
5.11(a) : Variation of $A_{m y}$ with $V_{b} / V_{s}$ and $W$ in passive case $(D=0.5)$ ..... 85
5.11(b) : Variation of $A_{m y}$ with $V_{b} / V_{s}$ and $W$ in passive case $(D=0.75)$ ..... 86
5.11(c) : Variation of $A_{m y}$ with $V_{b} / V_{s}$ and $W$ in passive case ( $D=1.0$ ) ..... 86
5.11(d) : Variation of $A_{m y}$ with $V_{b} / V_{s}$ and $W$ in passive case $(D=1.25)$ ..... 87
5.11(e) : Variation of $A_{m y}$ with $V_{b} / V_{s}$ and $W$ in passive case $(D=1.25)$ ..... 87
5.12(a) : Variation of $A_{m x}$ with $V_{b} / V_{s}$ and $W$ in active case ( $D=0.5$ ) ..... 88
5.12(b) : Variation of $A_{m x}$ with $V_{b} / V_{s}$ and $W$ in active case ( $D=0.75$ ) ..... 88
5.12(c) : Variation of $A_{m x}$ with $V_{b} / V_{s}$ and $W$ in active case $(D=1.0)$ ..... 89
5.12(d) : Variation of $A_{m x}$ with $V_{b} / V_{s}$ and $W$ in active case ( $D=1.25$ ) ..... 89
5.12(e) : Variation of $A_{m x}$ with $V_{b} / V_{s}$ and $W$ in active case $(D=1.5)$ ..... 90
5.13(a) : Variation of $A_{m x}$ with $V_{b} / V_{s}$ and $W$ in passive case $(D=0.5)$ ..... 90
5.13(b) : Variation of $A_{m x}$ with $V_{b} / V_{s}$ and $W$ in passive case $(D=0.75)$ ..... 91
5.13(c) : Variation of $A_{m x}$ with $V_{b} / V_{s}$ and $W$ in passive case ( $D=1.0$ ) ..... 91
5.13(d) : Variation of $A_{m x}$ with $V_{b} / V_{s}$ and $W$ in passive case $(D=1.25)$ ..... 92
5.13(e) : Variation of $A_{m x}$ with $V_{b} / V_{s}$ and $W$ in passive case ( $D=1.5$ ) ..... 92
6.1 : Normalized geometric features of a dual trench barrier ..... 96
6.2(a) : Typical finite element model of a dual open trench barrier ..... 97
6.2(b) : Typical finite element model of a dual in-filled trench barrier ..... 97
$6.3 \quad$ : Variation of $A_{m y}$ and $A_{m x}$ with trench locations ..... 98
6.4(a) : Variation of $A_{m y}$ versus $D_{d}$ and $W_{d}$ in active case ..... 99
6.4(b) : Variation of $A_{m y}$ versus $D_{d}$ and $W_{d}$ in passive case ..... 100
6.5(a) : Variation of $A_{m x}$ versus $D_{d}$ and $W_{d}$ in active case ..... 100
6.5(b) $\quad: \quad$ Variation of $A_{m x}$ versus $D_{d}$ and $W_{d}$ in passive case ..... 101
6.6 : Effect of barrier location on $A_{m y}$ and $A_{m x}$ ..... 103
6.7(a) : Variation of $A_{m y}$ against $D_{d}$ and $V_{b} / V_{s}\left(W_{d}=0.3\right)$ ..... 104
6.7(b) : Variation of $A_{m y}$ against $D_{d}$ and $V_{b} / V_{s}\left(W_{d}=0.4\right)$ ..... 104
6.7(c) : Variation of $A_{m y}$ against $D_{d}$ and $V_{b} / V_{s}\left(W_{d}=0.5\right)$ ..... 105
6.8(a) : Variation of $A_{m x}$ against $D_{d}$ and $V_{b} / V_{s}\left(W_{d}=0.3\right)$ ..... 105
6.8(b) : Variation of $A_{m x}$ against $D_{d}$ and $V_{b} / V_{s}\left(W_{d}=0.4\right)$ ..... 106
6.8(c) : Variation of $A_{m x}$ against $D_{d}$ and $V_{b} / V_{s}\left(W_{d}=0.5\right)$ ..... 106
6.9(a) : Variation of $A_{m y}$ against $W_{d}$ and $V_{b} / V_{s}\left(D_{d}=0.2\right)$ ..... 108
6.9(b) : Variation of $A_{m y}$ against $W_{d}$ and $V_{b} / V_{s}\left(D_{d}=0.3\right)$ ..... 109
6.9(c) : Variation of $A_{m y}$ against $W_{d}$ and $V_{b} / V_{s}\left(D_{d}=0.4\right)$ ..... 109
6.9(d) : Variation of $A_{m y}$ against $W_{d}$ and $V_{b} / V_{s}\left(D_{d}=0.5\right)$ ..... 110
6.9(e) : Variation of $A_{m y}$ against $W_{d}$ and $V_{b} / V_{s}\left(D_{d}=0.6\right)$ ..... 110
6.10(a) : Variation of $A_{m x}$ against $W_{d}$ and $V_{b} / V_{s}\left(D_{d}=0.2\right)$ ..... 111
6.10(b) : Variation of $A_{m x}$ against $W_{d}$ and $V_{b} / V_{s}\left(D_{d}=0.3\right)$ ..... 111
6.10(c) : Variation of $A_{m x}$ against $W_{d}$ and $V_{b} / V_{s}\left(D_{d}=0.4\right)$ ..... 112
6.10(d) : Variation of $A_{m x}$ against $W_{d}$ and $V_{b} / V_{s}\left(D_{d}=0.5\right)$ ..... 112
6.10(e) : Variation of $A_{m x}$ against $W_{d}$ and $V_{b} / V_{s}\left(D_{d}=0.6\right)$ ..... 113
6.11(a) : Dual and single open trench isolation in active case ..... 114
6.11(b) : Dual and single open trench isolation in passive case ..... 115
6.12(a) : Dual and single in-filled trench isolation $\left(V_{b} / V_{s}=0.1\right)$ ..... 116
6.12(b) : Dual and single in-filled trench isolation $\left(V_{b} / V_{s}=0.2\right)$ ..... 116
A. 1 : Basic project properties ..... 137
A. 2 : Selecting basic units and maximum coordinates of the model ..... 138
A. $3:$ Creating model geometry of a half-space with an open trench ..... 139
A. $4 \quad:$ Assigning loads and model boundaries ..... 140
A. $5 \quad$ : Creating material data set for half-space soil ..... 141
A. 6 : Assigning elastic parameters to half-space soil ..... 142
A. 7 : Mesh generation ..... 143
A. 8 : Calculation program ..... 144
A. 9 : Defining parameters for dynamic analysis ..... 145
A. 10 : Defining dynamic load parameters in calculation program ..... 146
A. 11 : Node selection for displacement-time histories ..... 147

## LIST OF FIGURES

| FIGURE | TITLE | PAGE |
| :---: | :---: | :---: |
| 2.1 | Variation of $V_{p} / V_{s}$ and $V_{R} / V_{s}$ against Poisson's ratio (redrawn after Kramer, 1996) | 9 |
| 2.2 | Variation of vertical and horizontal displacement components of R-wave with depth (redrawn after Das, 1990; Das and Ramana, 2011) | 10 |
| 2.3(a) | Active isolation by a circular trench (redrawn after Woods, 1968a) | 14 |
| 2.3(b) | Passive isolation by a straight trench (redrawn after Woods, 1968a) | 14 |
| 3.1 | Coordinate system in PLAXIS | 30 |
| 3.2 | Positions of nodes and stress points in 15 -node triangular elements (after Brinkgreve et al., 2010) | 31 |
| 3.3 | (a) A 2-D schematic of an open trench isolation (b) An axisymmetric idealization of the scheme | 32 |
| 3.4 | Schematic of an axisymmetric model with boundary conditions | 34 |
| 3.5 | Example showing estimation of average amplitude reduction factor | 41 |
| 4.1 | An open trench isolation showing normalized barrier features | 44 |
| 4.2 | Schematic of a model depicting dimensions and boundary conditions | 46 |
| 4.3 | Finite element model of a barrier-free half-space | 47 |
| 4.4 | Displacement-time history of vertical vibration component in a barrier-free half-space (at $x=7 L_{R}$ ) | 48 |
| 4.5(a) | Convergence study to ensure adequacy of model length ( $H_{m}=5 L_{R}$ ) | 48 |
| 4.5(b) | Convergence study to ensure adequacy of model depth ( $L_{m}=35 \mathrm{~m}$ ) | 49 |
| 4.6 | Typical finite element model of an open trench | 50 |
| 4.7 | Displacement-time histories of vertical vibration component with and without barrier (at $x=7 L_{R}$ ) | 51 |
| 4.8 | n | 5 |

A. 12 : Starting calculation phase ..... 148
A. 13 : End of calculation phase ..... 149
A. 14 : Deformed mesh ..... 150
A. 15 : Contour map showing vertical displacement components ..... 151
A. 16 : Contour map showing horizontal displacement components ..... 152
A. 17 : Curve generation at a pre-selected node ..... 153
A. 18 : Displacement-time curve for vertical component of surface ..... 154 displacement at the desired node
A. 19 : Displacement-time curve for horizontal component of surface ..... 155 displacement at the desired node
B. 1 : Peak surface displacement amplitudes with and without ..... 156 barrier measured at different points beyond barrier
B. 2 : Amplitude reduction factors versus normalized distances from ..... 157 barrier

## LIST OF TABLES

TABLE TITLE PAGE
2.1 : Absorption coefficients for different soil types (after Woods, $\begin{aligned} & \text { 1997) }\end{aligned}$
2.2 : Characteristics of body waves (P and S-waves) and R-waves 13
3.1 : Global coarseness settings and mesh elements (after 37 Brinkgreve et al., 2010)
4.1 : Input parameters of material model 42
$4.2:$ Ground motion parameters of half-space soil 43
$4.3: \quad$ Parameters chosen for open trench isolation study 53
$5.1:$ Values of parameters adopted in design charts 82
$5.2:$ Comparison with published results 93
$7.1:$ Simplified design formulae and their applicability 120
C. $1 \quad$ : Estimating average $A_{m y}$ against $D \quad 158$
$\begin{array}{lll}\text { C. } 2 & \text { Fitting regression curve } & 159\end{array}$

## LIST OF ABBREVIATIONS

## ABBREVIATION SIGNIFICANCE

| P-wave | Primary wave |
| :--- | :--- |
| S-wave | Shear wave |
| R-wave | Rayleigh wave |
| 2-D | Two-dimensional |
| 3-D | Three-dimensional |
| BEM | Boundary element method |
| FEM | Finite element method |

## LIST OF SYMBOLS AND NOTATIONS

## SYMBOL/ SIGNIFICANCE <br> NOTATION

| $\lambda$ | $:$ | Lami's constant |
| :--- | :--- | :--- |
| $G$ | $:$ | Shear modulus |

$E \quad: \quad$ Elastic modulus of an elastic medium/half-space soil
$\rho \quad:$ Density of an elastic medium/ half-space soil
$v \quad:$ Poisson's ratio
$V_{p} \quad:$ Primary wave velocity
$V_{s} \quad:$ Shear wave velocity
$V_{R} \quad:$ Rayleigh wave velocity
$K \quad: \quad$ Dimensionless quantity signifying the ratio between R-wave and S-wave velocities
$\alpha \quad: \quad$ Dimensionless quantity indicating the ratio between S-wave and P-wave velocities
$L_{R} \quad:$ Rayleigh wavelength
$r \quad: \quad$ Radial distance of a point from source of excitation
$\beta \quad:$ Absorption coefficient
$f_{1}, f_{2} \quad:$ Excitation frequencies corresponding to $\beta_{1}$ and $\beta_{2}$
$A_{1} \quad:$ Amplitude at distance $r_{1}$ from source
$A_{2} \quad:$ Amplitude at distance $r_{2}$ from source
$n \quad: \quad$ Exponent whose value depends on the type of seismic wave
$B \quad:$ Width of the imaginary footing
$b \quad: \quad$ One-half of the width of imaginary footing
$G_{\max } \quad: \quad$ Maximum shear modulus
$\alpha_{R}$ and $\beta_{R} \quad: \quad$ Rayleigh mass and stiffness matrix coefficients
$f \quad:$ Frequency of excitation
$\xi \quad: \quad$ Material damping (fractional value is termed as damping ratio)
$\omega \quad: \quad$ Angular frequency of excitation
$P(t) \quad: \quad$ Harmonic load
$\phi \quad: \quad$ Phase angle in degrees
Pi : Default input value of harmonic load magnitude

| $M$ | $:$ | Amplitude multiplier |
| :--- | :--- | :--- |
| $P_{0}$ | $:$ | Magnitude of harmonic load |
| $A_{R}$ | $:$ | Amplitude reduction factor |
| $s$ | $:$ | Extent of zone of investigation over which amplitude reduction |
|  |  | factors are estimated |
| $A_{m}$ | $:$ | Average amplitude reduction factor |
| $d$ and $D$ | $:$ | Absolute and normalized depths of an open/in-filled trench |
| $w$ and $W$ | $:$ | Absolute and normalized widths of an open/in-filled trench |
| $l$ and $L$ | $:$ | Absolute and normalized distances of an open/in-filled trench |
|  |  | from source of excitation |
| $\sigma_{n}$ and $\tau_{s}$ | $:$ | Normal and shear stress components of dynamic stress |
| $C_{1}$ and $C_{2}$ | $:$ | Wave relaxation coefficients (associated with absorption of |
|  |  | pressure waves and shear waves respectively) assigned to |

$w_{d}$ and $W_{d} \quad: \quad$ Absolute and normalized widths of each trench in case of dual trench barriers
$d_{d}$ and $D_{d} \quad: \quad$ Absolute and normalized depths of each trench in case of dual trench barriers

